

# **Spatial Statistics for Public Health and Safety**

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***ESRI***  
***Geoprocessing, Spatial Statistics***

# Spatial Data Analysis

- Traditional GIS Analyses
  - Spatial/temporal queries
  - Buffer analysis
  - Overlay analysis
- Spatial Statistics Toolbox
  - Identify, analyze and respond to incident hot/cold spots
  - Summarize spatial pattern over time
  - Identify anomalous spatial patterns

# Objectives

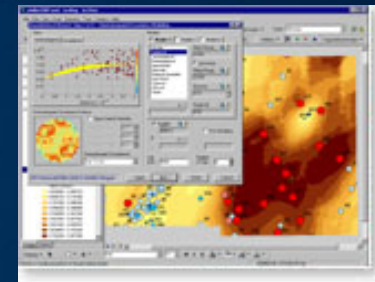
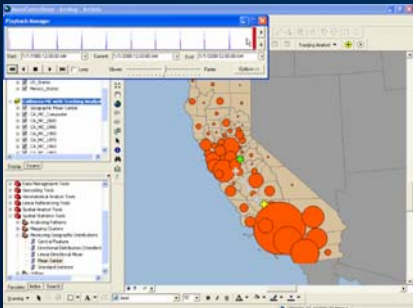
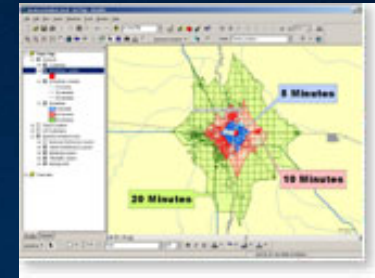
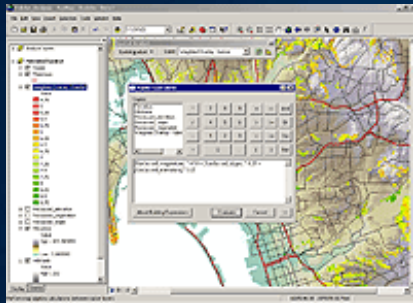
- Introduce core spatial statistics tools available in ArcGIS 9
- Provide examples for how these tools might be used in Public Safety and Public Health
- Be sure you know where to go for additional information

# Presentation

- Basics: What are spatial statistics and why do we care?
  - Maps can lie
- Overview of Spatial Statistics Toolbox
  - Measuring Geographic Distributions
  - Analyzing Spatial Patterns
  - Mapping Clusters and Outliers
    - 911 Emergency Call Analysis Demo
    - SAS/ArcGIS Mortality Data Analysis
- Resources

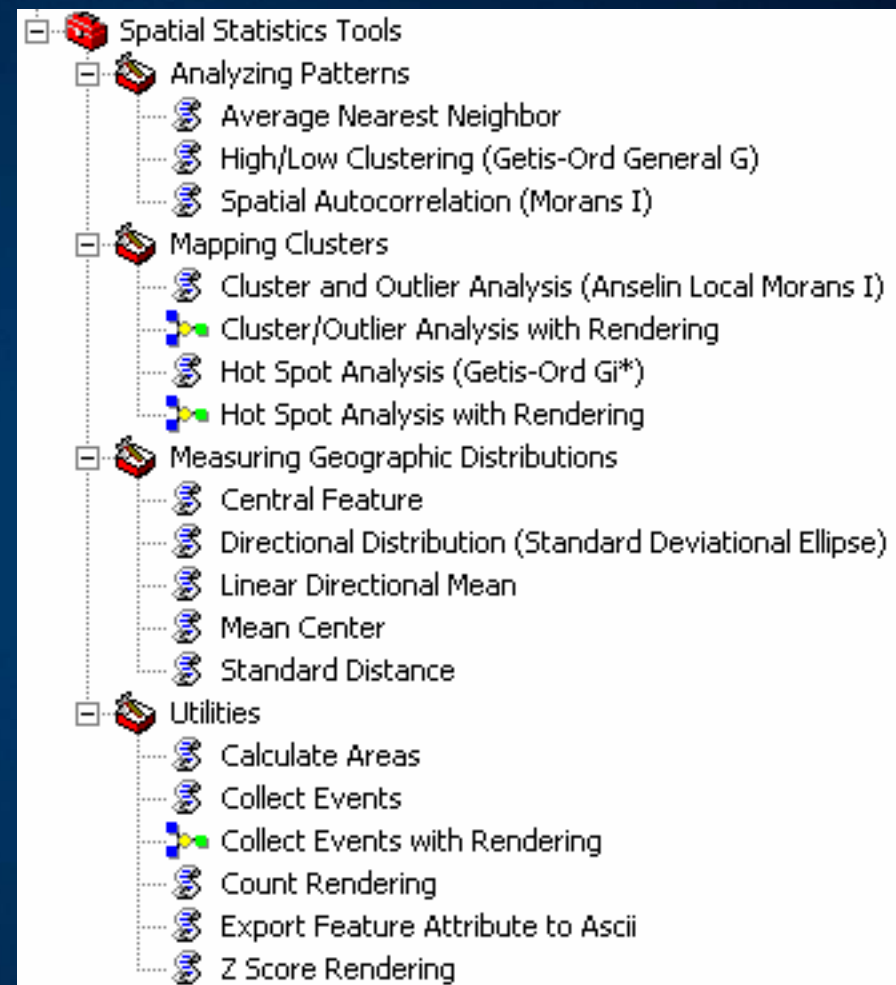
# ESRI software and Statistics

- Business Analyst
- Spatial Analyst
- Geostatistical Analyst
- SAS Bridge
- Spatial Statistics Tools



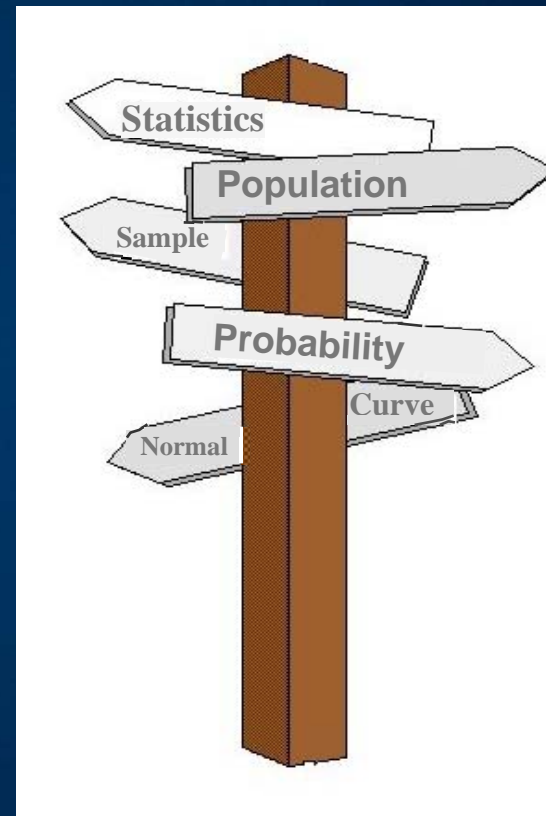
# Toolsets and tools

- Core functionality with ArcGIS 9 (not an extension)
- Available with all ArcGIS licenses
- Source code provided
- Use ArcGIS 9.1 with Service Pack 1 or 2
- *The ESRI Guide to GIS Analysis, Volume 2*



# What are spatial statistics?

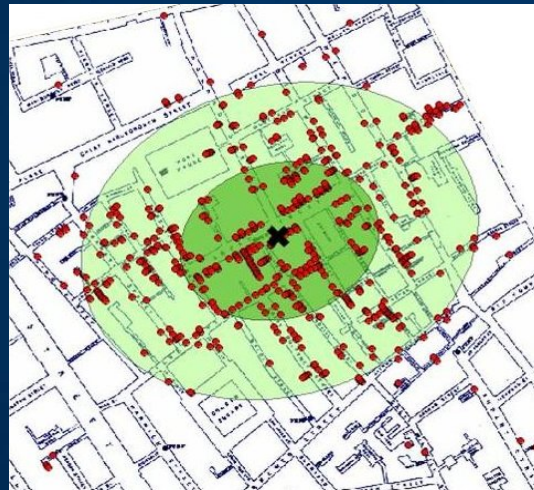
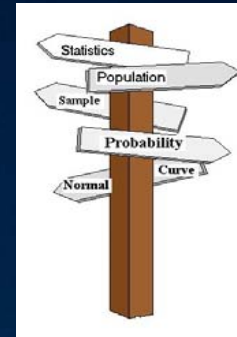
- A measure of what's going on spatially
  - Not the same as traditional (a-spatial) statistics





# What are spatial statistics?

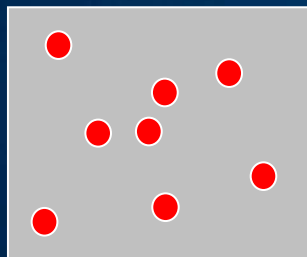
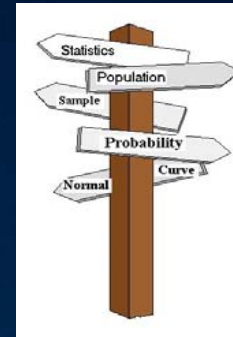
- A measure of what's going on spatially
  - Not the same as a-spatial stats
- Two categories of spatial measurements
  - 1) Identifying characteristics of a distribution



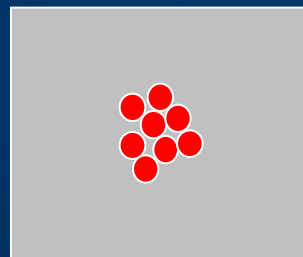


# What are spatial statistics?

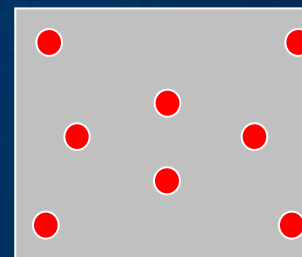
- A measure of what's going on spatially
  - Not the same as a-spatial stats
- Two categories of spatial measurements
  - 1) Identifying characteristics of a distribution
  - 2) Quantifying geographic pattern



**Random**



**Clustered**



**Dispersed**

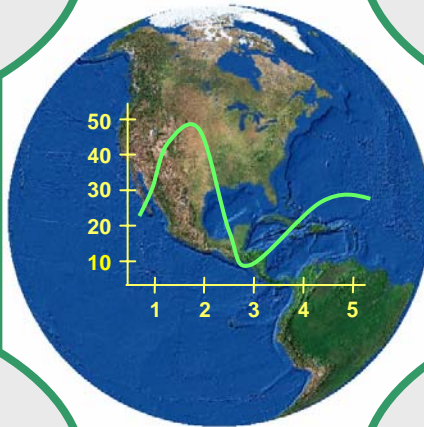
# Why use spatial statistics?

**Better understand behavior  
of geographic phenomena**

**Make decisions with higher  
level of confidence**

**Pinpoint causes of specific  
geographic patterns**

**Summarize the distribution  
in a single number**

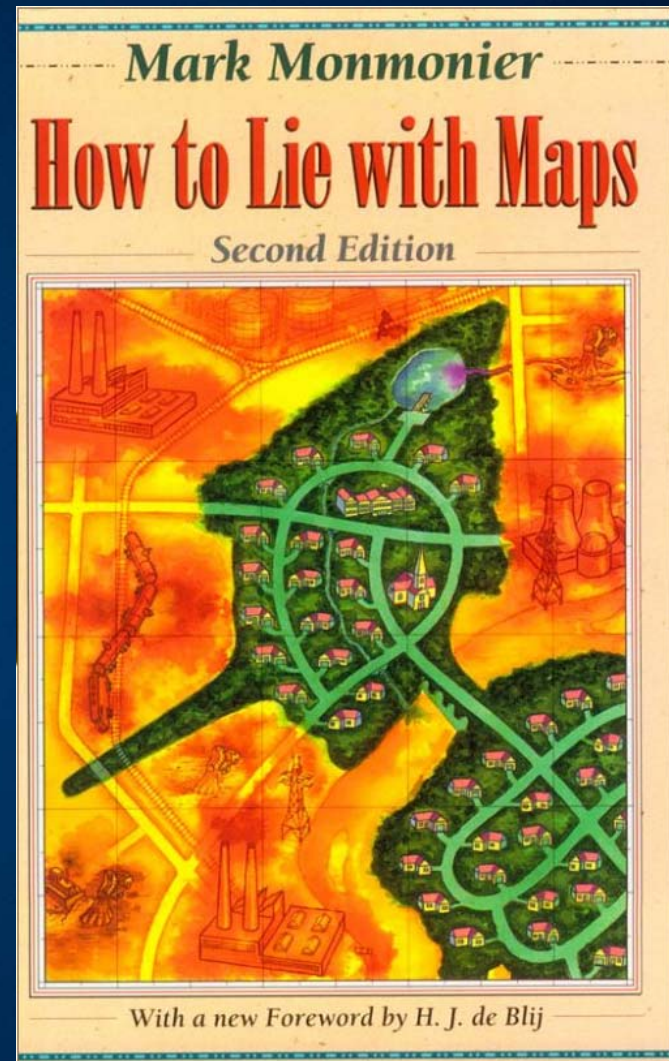


# Why Use Spatial Statistics?

**Spatial Statistics help us assess:**

- Patterns
- Relationships
- Trends

How we present/map our results (colors, classbreaks) can either enhance or obscure communication



# Crime Analysis Demo

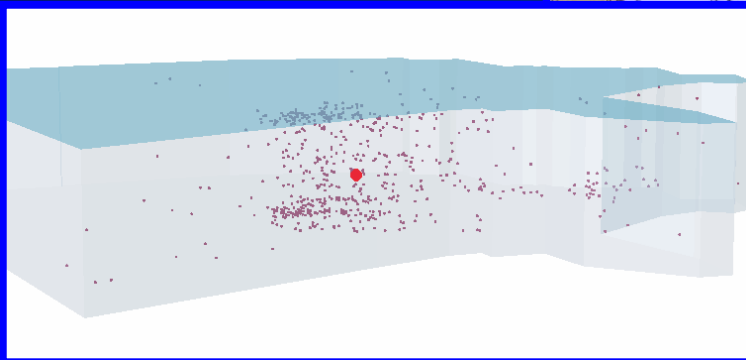
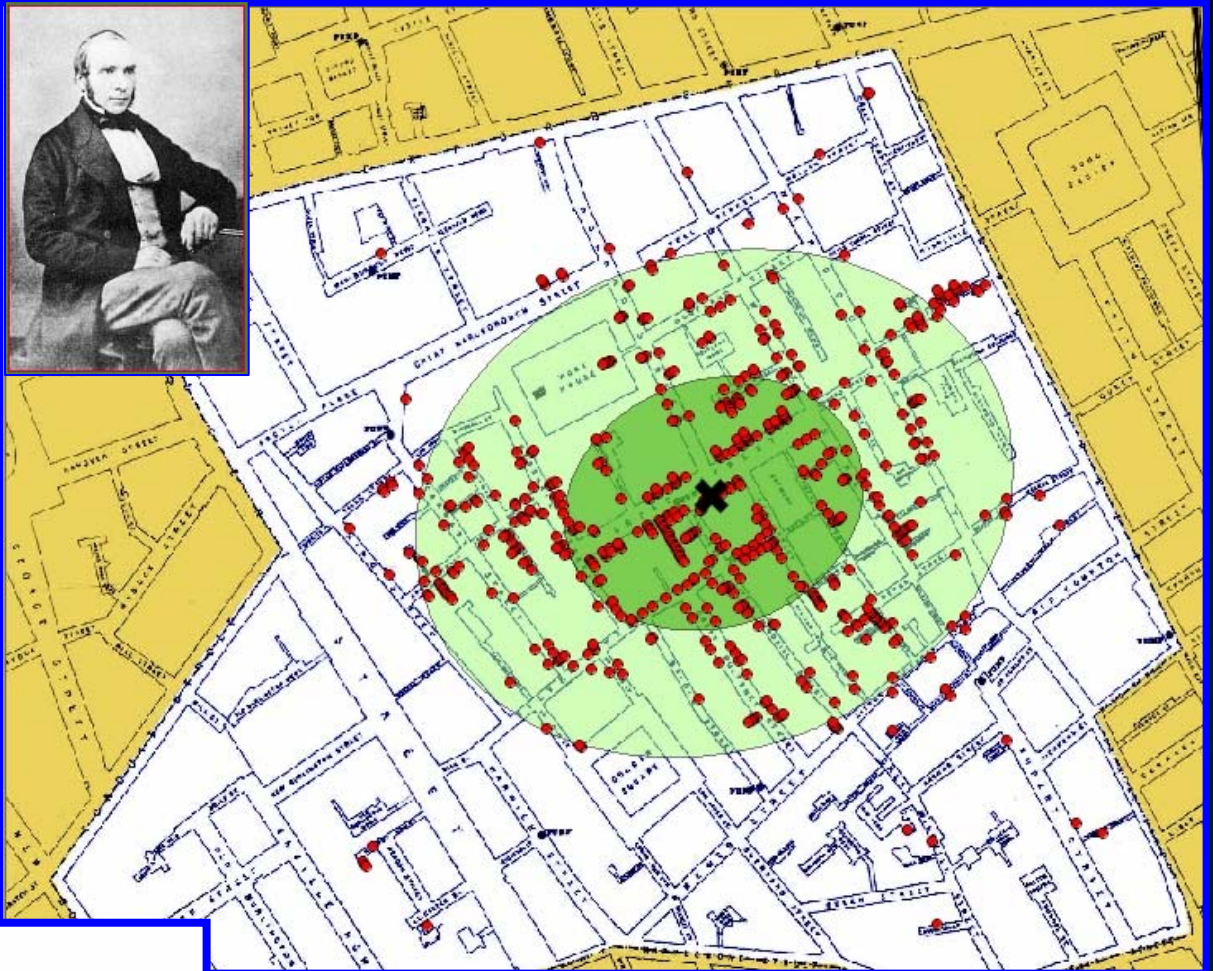
# Measuring Geographic Distributions toolset

- Identify spatial characteristics of a distribution
    - Where is the center?
    - What is most central?
    - How dispersed are features around the center?
    - Are there any directional trends?
  - Often used to:
    - Compare different feature categories
    - Examine changes over time
1. Central Feature
  2. Mean Center
  3. Linear Directional Mean
  4. Standard Distance
  5. Standard Deviation Ellipse



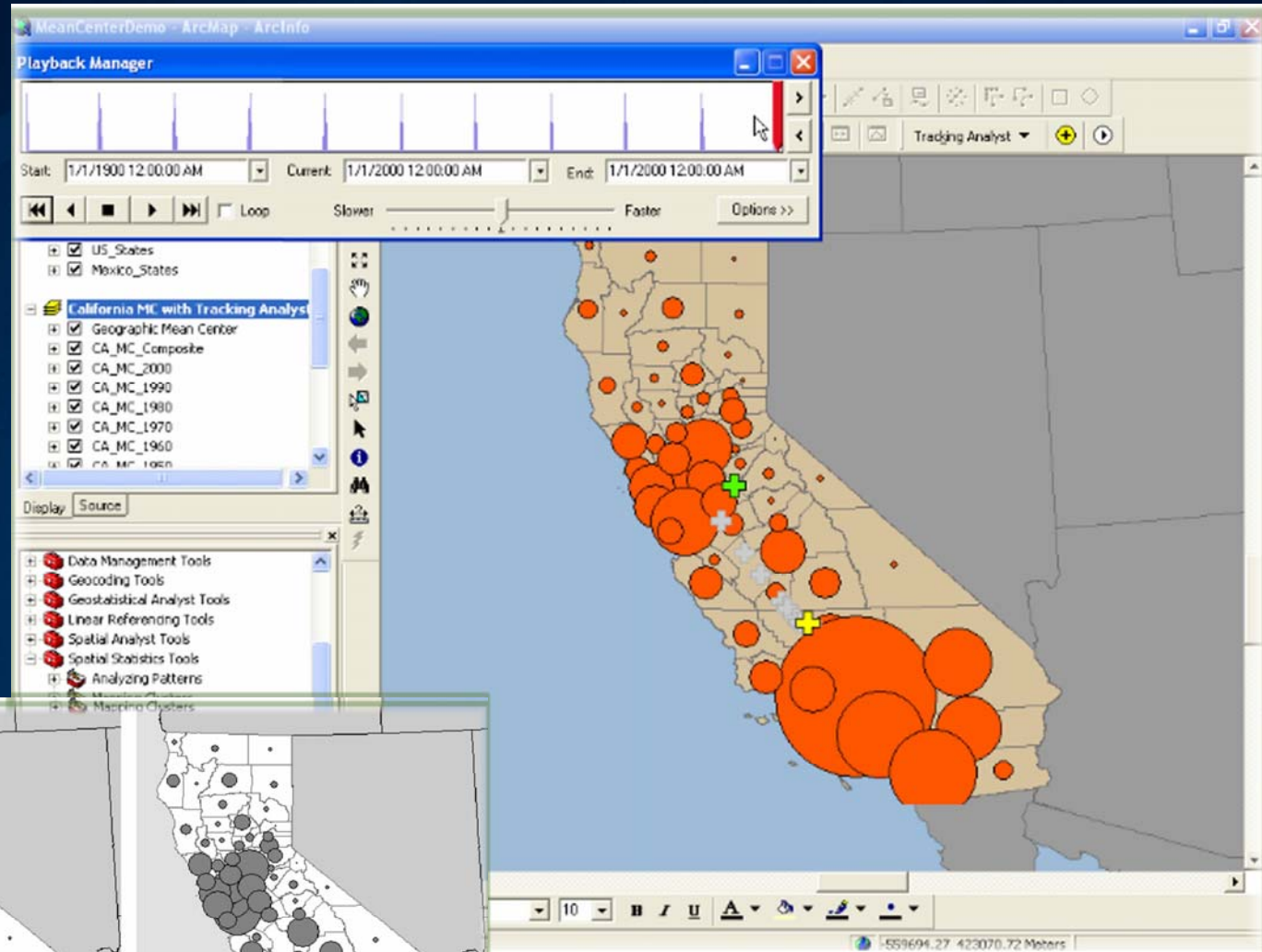
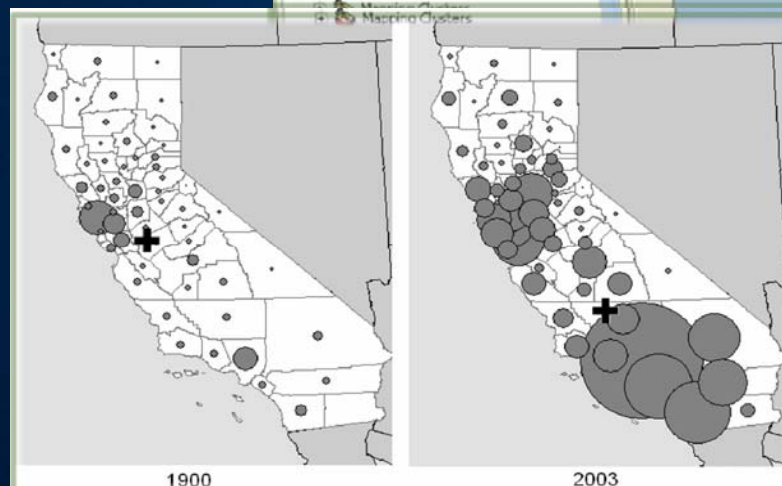
# Mean Center

Computes the average x and y coordinate, based on all features in the study area





# Spatial Statistics Tools Mean Center



Mean Center of Population  
California

# Mean Center Demo

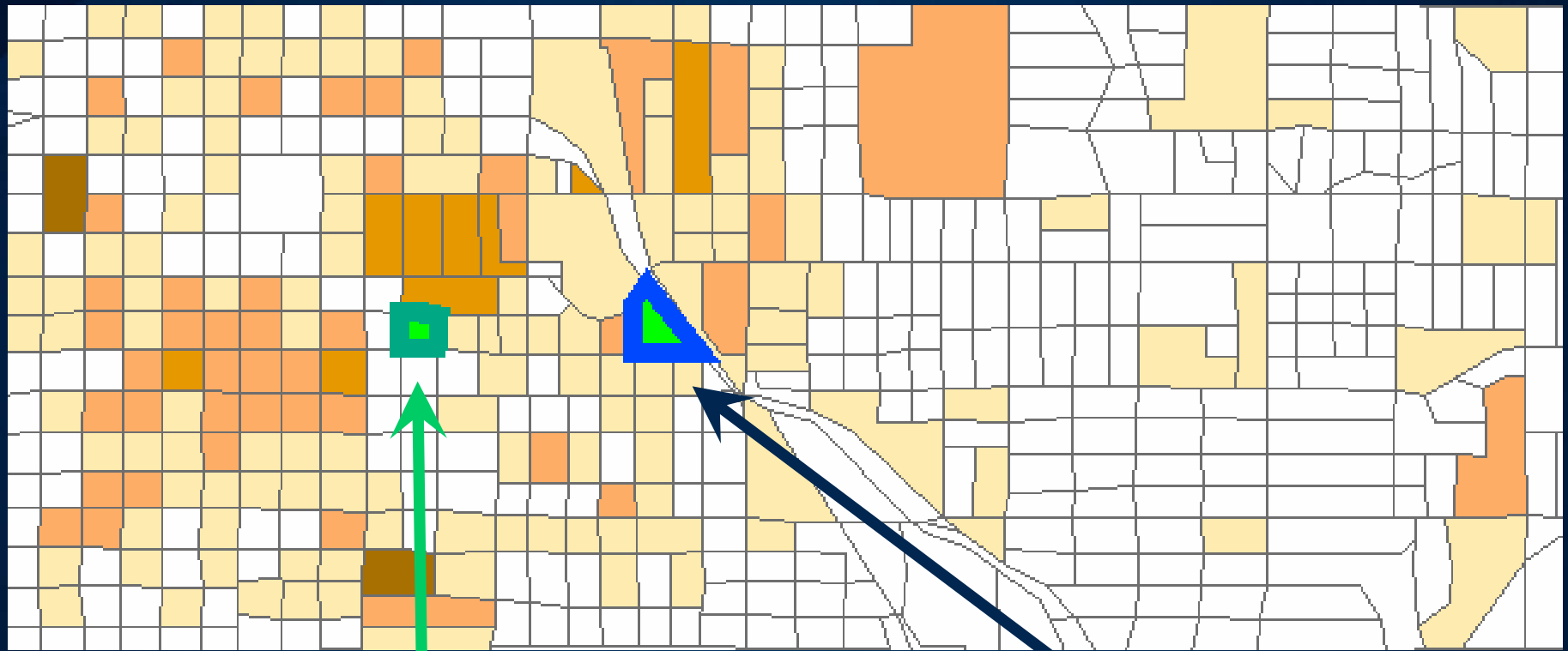
# Central Feature

- Identifies the most centrally located feature
  - Feature with the lowest total distance to all other features
- Uses:
  - Finding the most accessible existing feature

**What is the best location for a new service center?**



# Locating services for victims of domestic crime



**New Service**  
(most central with weighting)

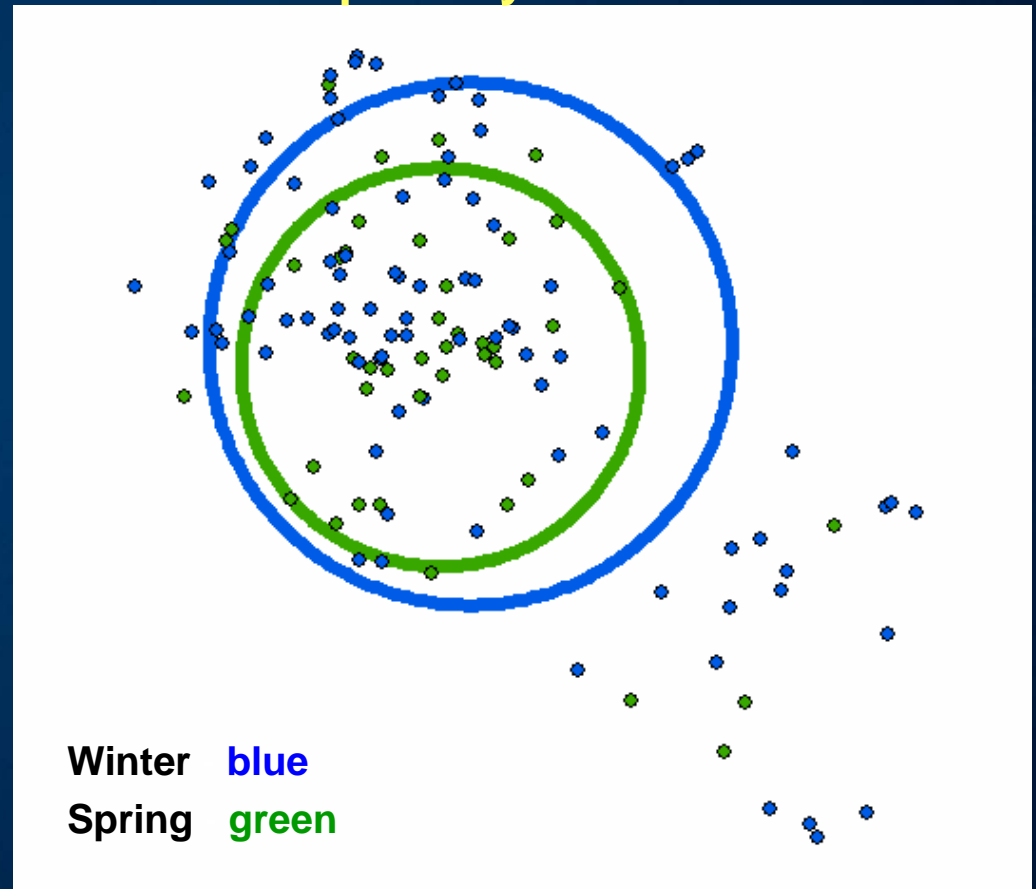
**Most Central Tract**

# Measuring feature distribution

## Standard Distance tool

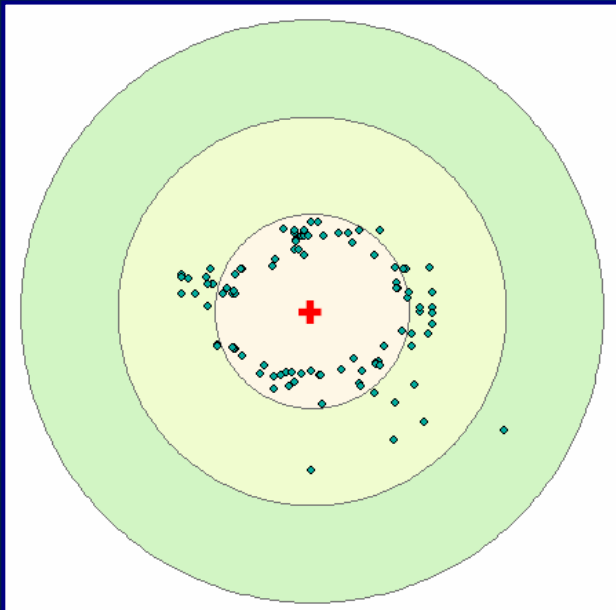
- Measures distribution of features around the mean
- Result is a summary statistic representing distance

### Seasonal effects of childhood respiratory diseases



# Interpreting results... standard distance

- Standard distance deviation is the radius of the standard distance circle
- 1, 2, or 3 standard deviations?
- Problem distributions



**Standard Distance**

Input Feature Class

Output Standard Distance Feature Class

Circle Size

1 Standard Deviation

2 Standard Deviations

3 Standard Deviations

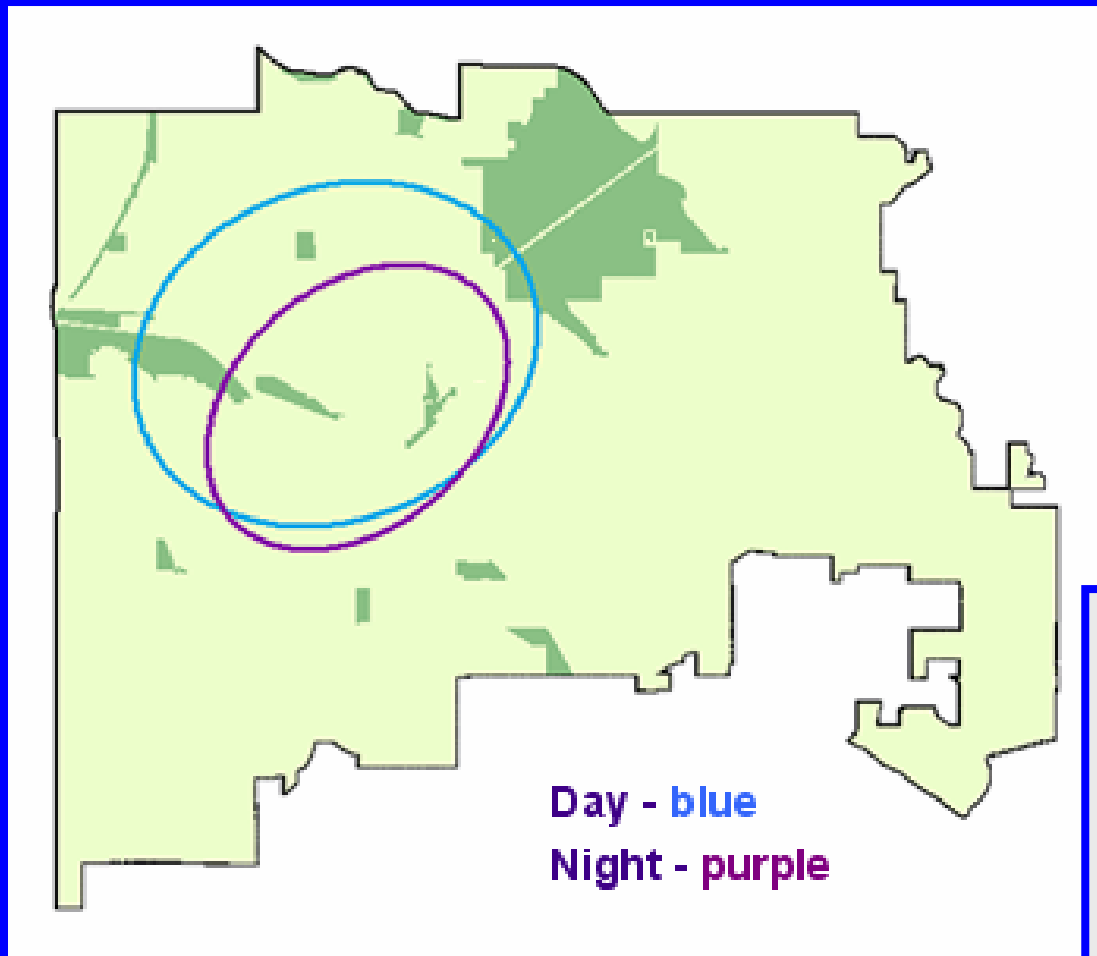
Case Field (optional)

- **1 standard deviation = 68% of features**
- **2 standard deviations = 95% of features**
- **3 standard deviations = 99% of features**



# Directional Distribution (Standard Deviational Ellipse)

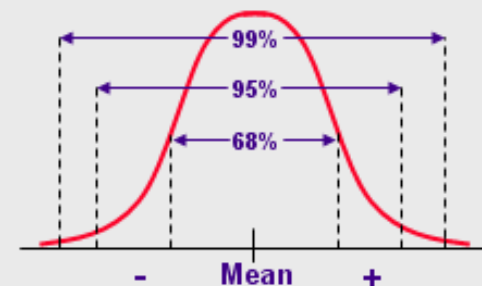
- Abstracting spatial trends in a distribution of features



- Uses:
  - Comparing distributions
  - Examining different time periods
  - Showing compactness and orientation

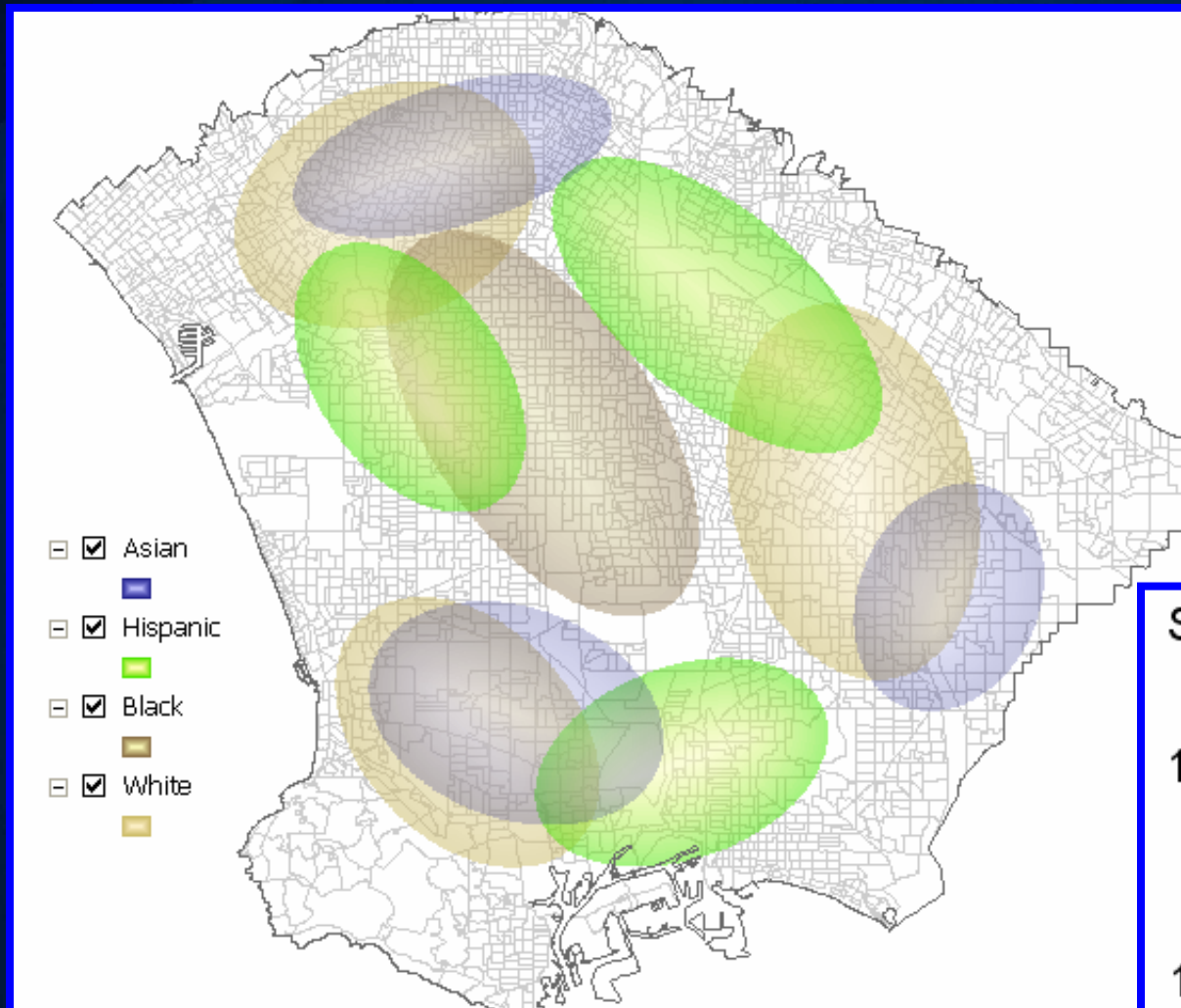
## Standard deviation

### Normal Distribution



# Directional Distribution (Standard Deviational Ellipse)

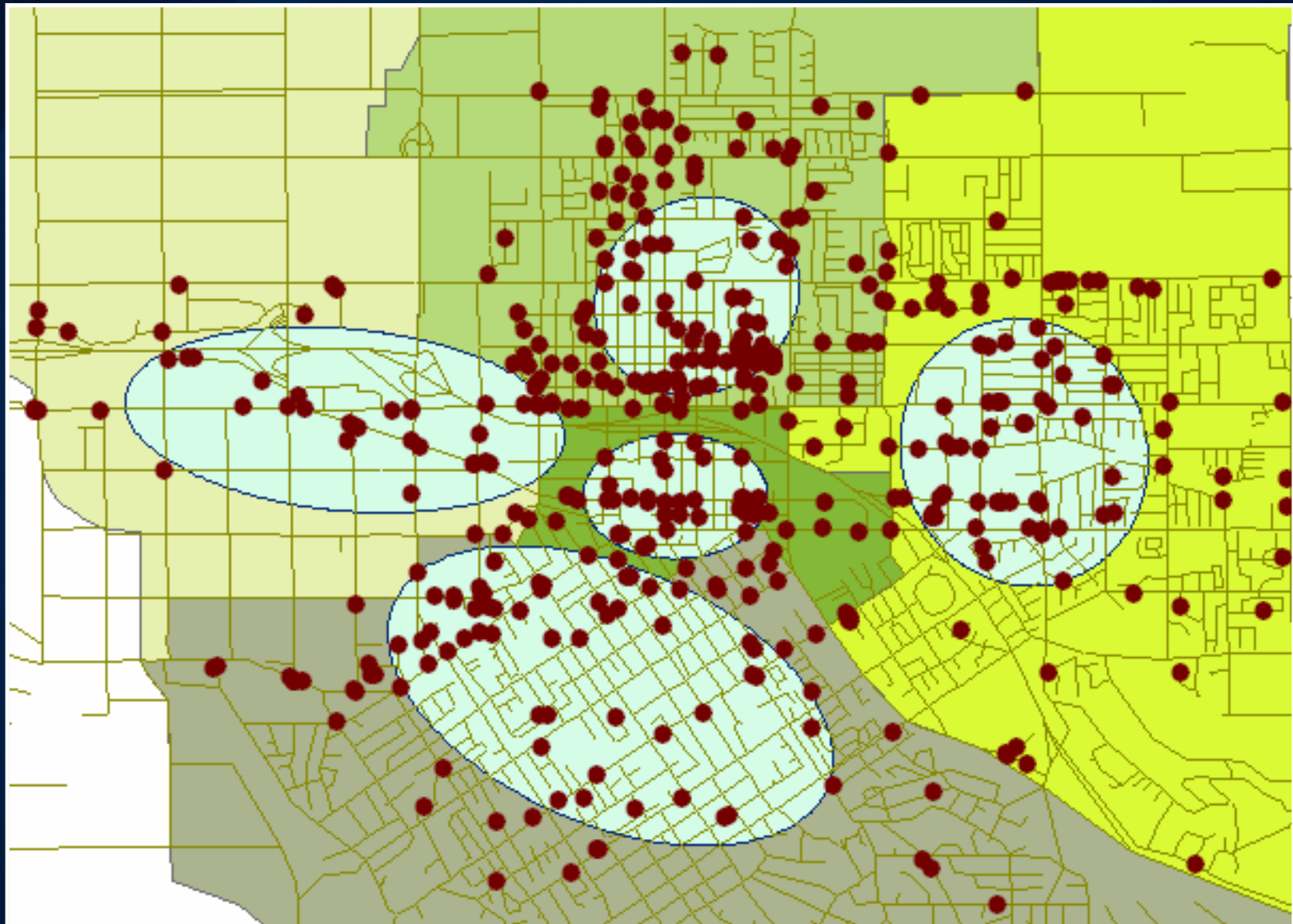
- Abstracting spatial trends in a distribution of features



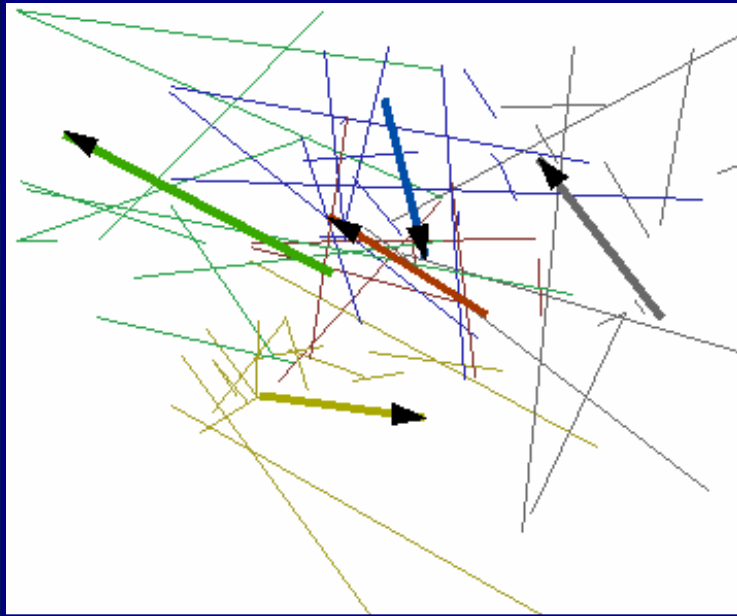
Segregation Index =

$$1 - \frac{E_1 \cap E_2 \cap E_3 \cap \dots E_n}{E_1 \cup E_2 \cup E_3 \cup \dots E_n} =$$
$$1 - \frac{2931680545.83}{7994760004.92} = 0.63$$

## Another example... standard deviational ellipse



# Linear Directional Mean



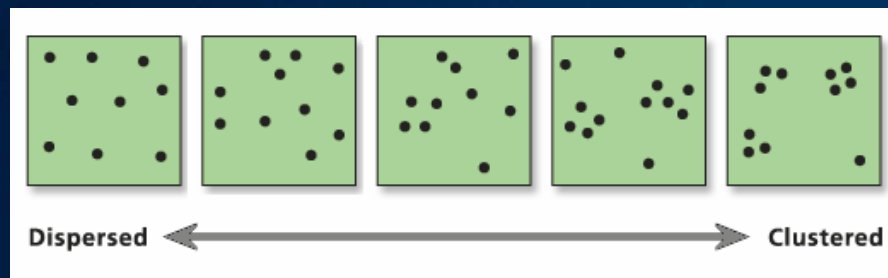
Angle of a line representing mean direction (or orientation) based on all lines in a dataset



# Analyzing Patterns toolset

- Determine the extent to which features are clustered, dispersed, or random across study area

1. Average Nearest Neighbor
2. High/Low Clustering (Getis/Ord General G)



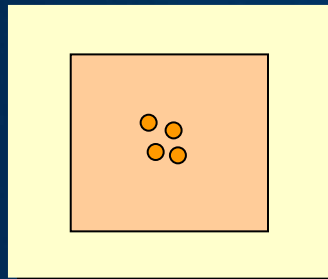
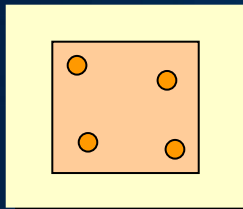
- Global analysis
- Useful for:
  - Gaining a better understanding of feature distribution
    - Degree of clustering or dispersion across study area
  - Comparing different sets of features
  - Tracking changes in patterns (over time)

3. Multi-Distance Spatial Cluster Analysis (Ripley's K Function)
4. Spatial Autocorrelation (Global Moran's I)

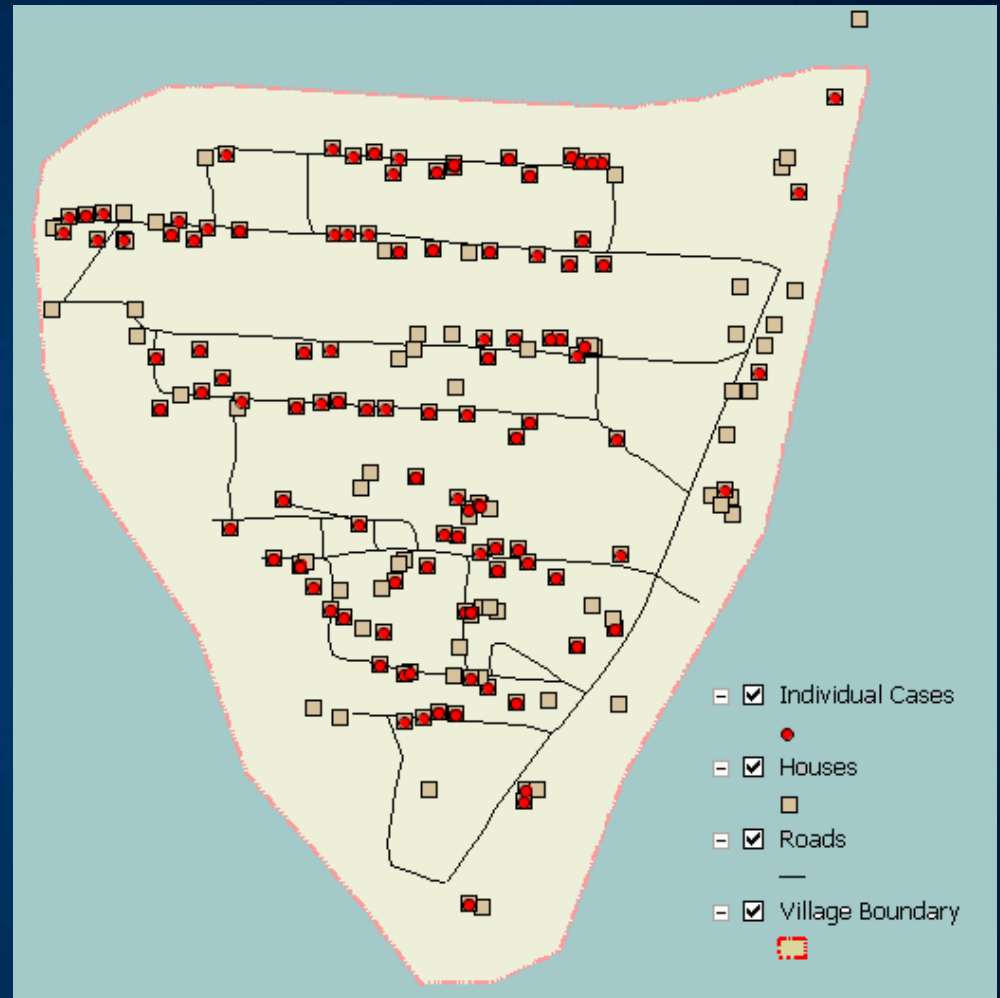


# Average Nearest Neighbor

- Calculates the average distance between each feature
  - Considers arrangement and distance of features
- Based on area



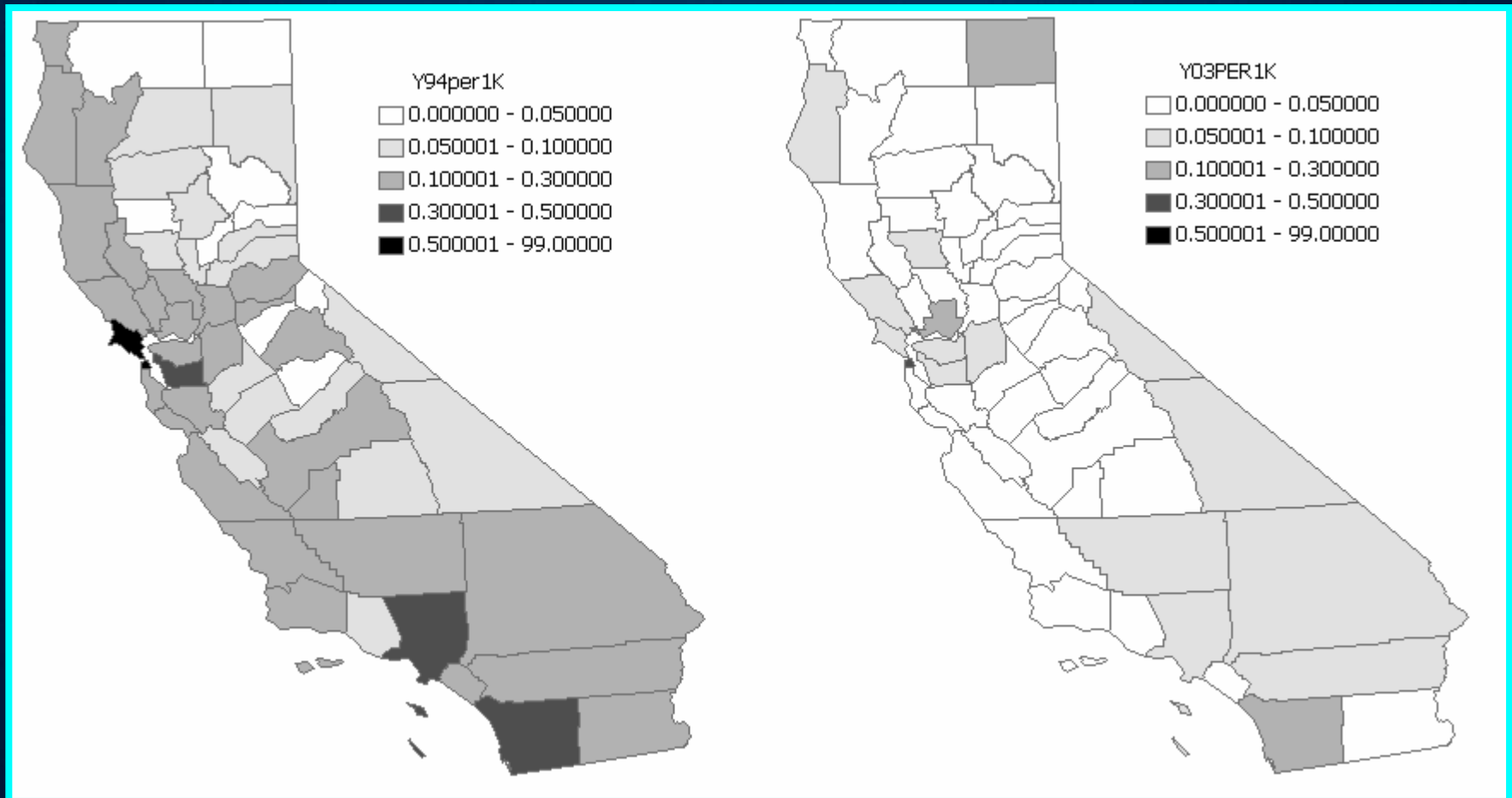
Nearest Neighbor Ratio	Pattern
Ratio = 1	Random
Ratio < 1	Clustered
Ratio > 1	Dispersed





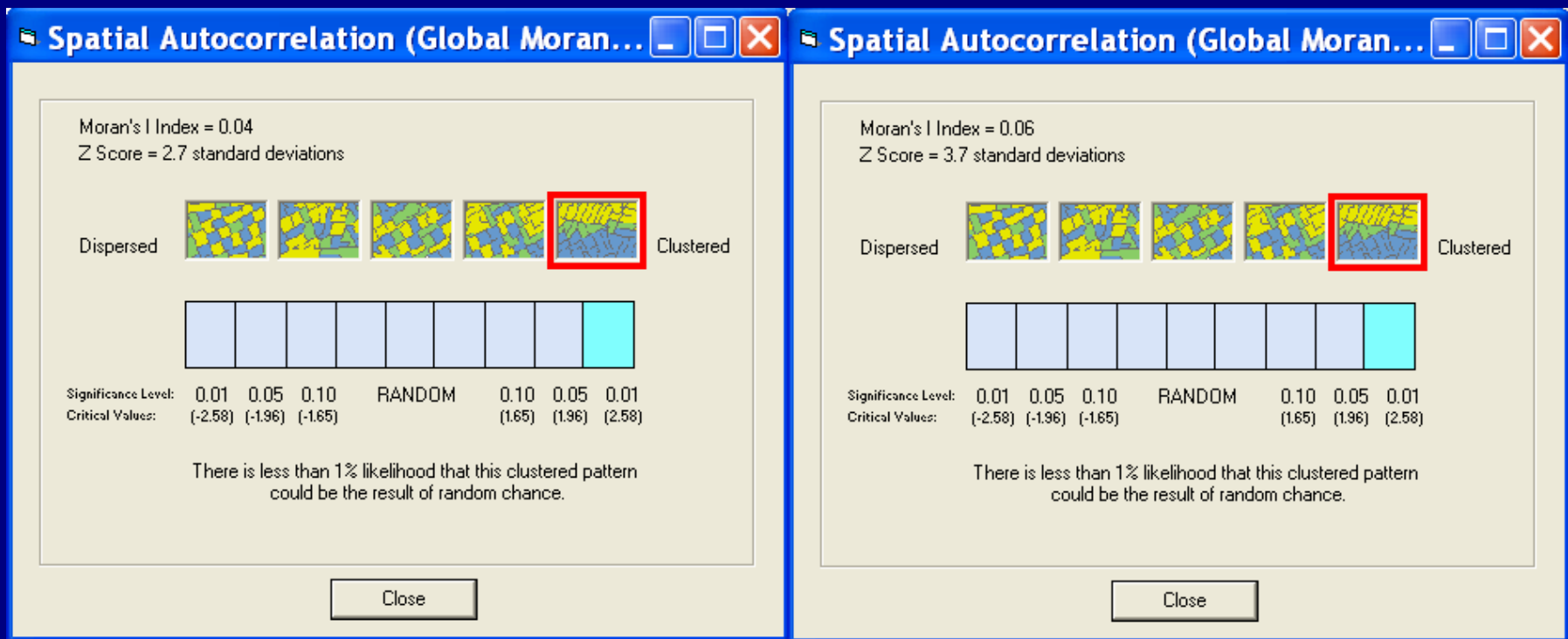
# Spatial Autocorrelation (Global Moran's I)

- Measures similarity of neighboring features
  - Things closer are more alike than things that are not
- Based on both feature locations and attribute values



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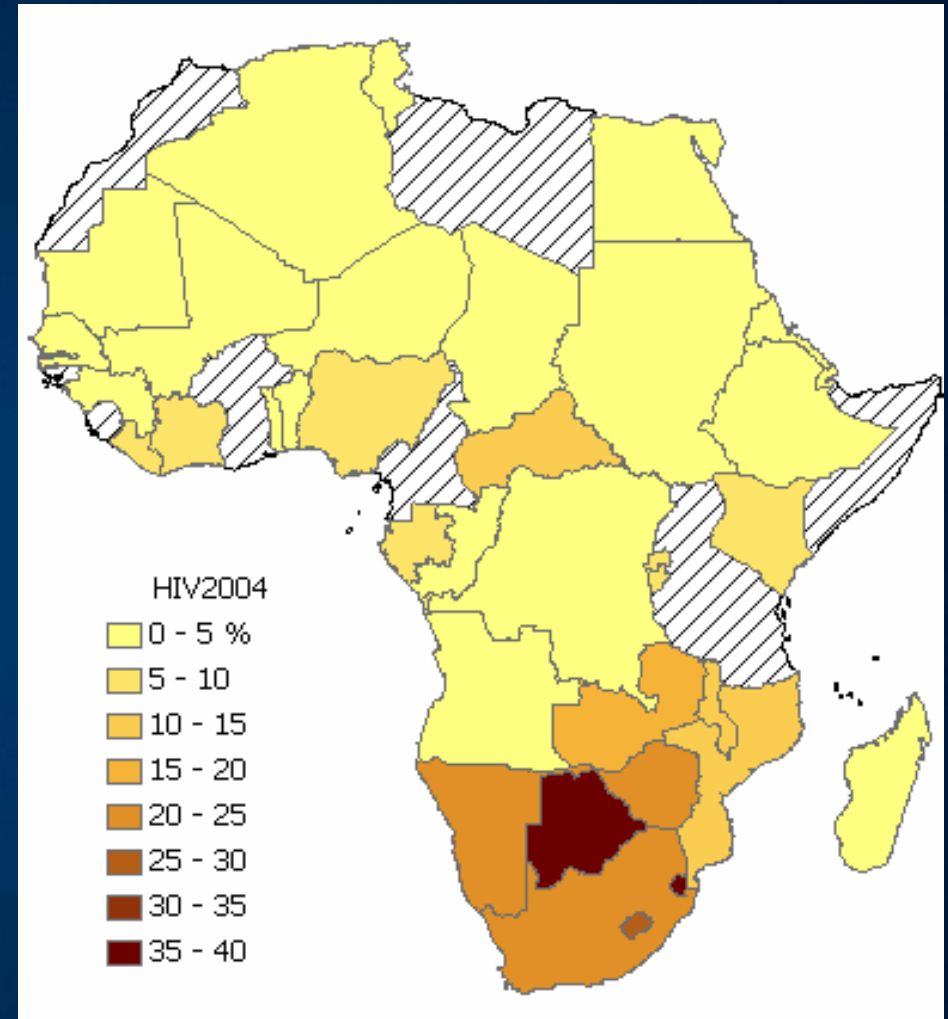
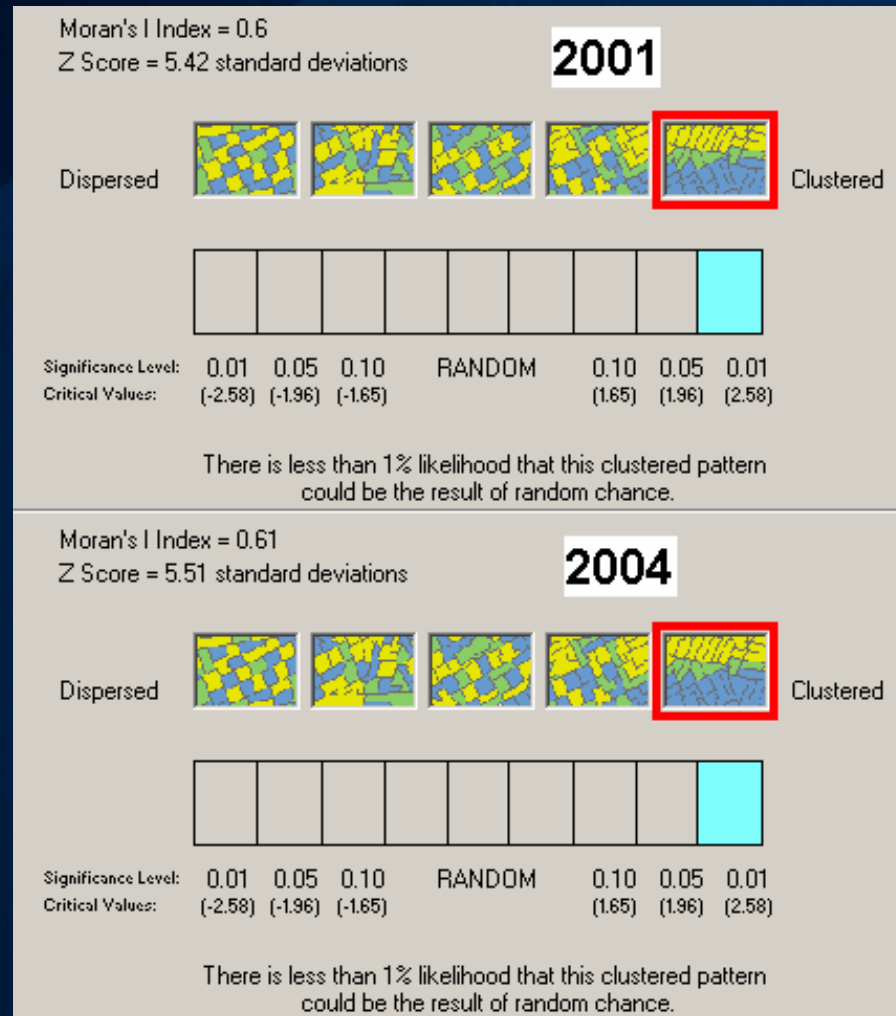


Z Score = 2.7 standard deviations

Z Score = 3.7 standard deviations

# Spatial Autocorrelation (Global Moran's I)

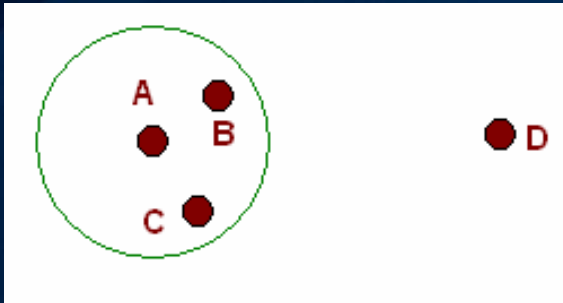
Z Score = 5.4 standard deviations



Z Score = 5.5 standard deviations

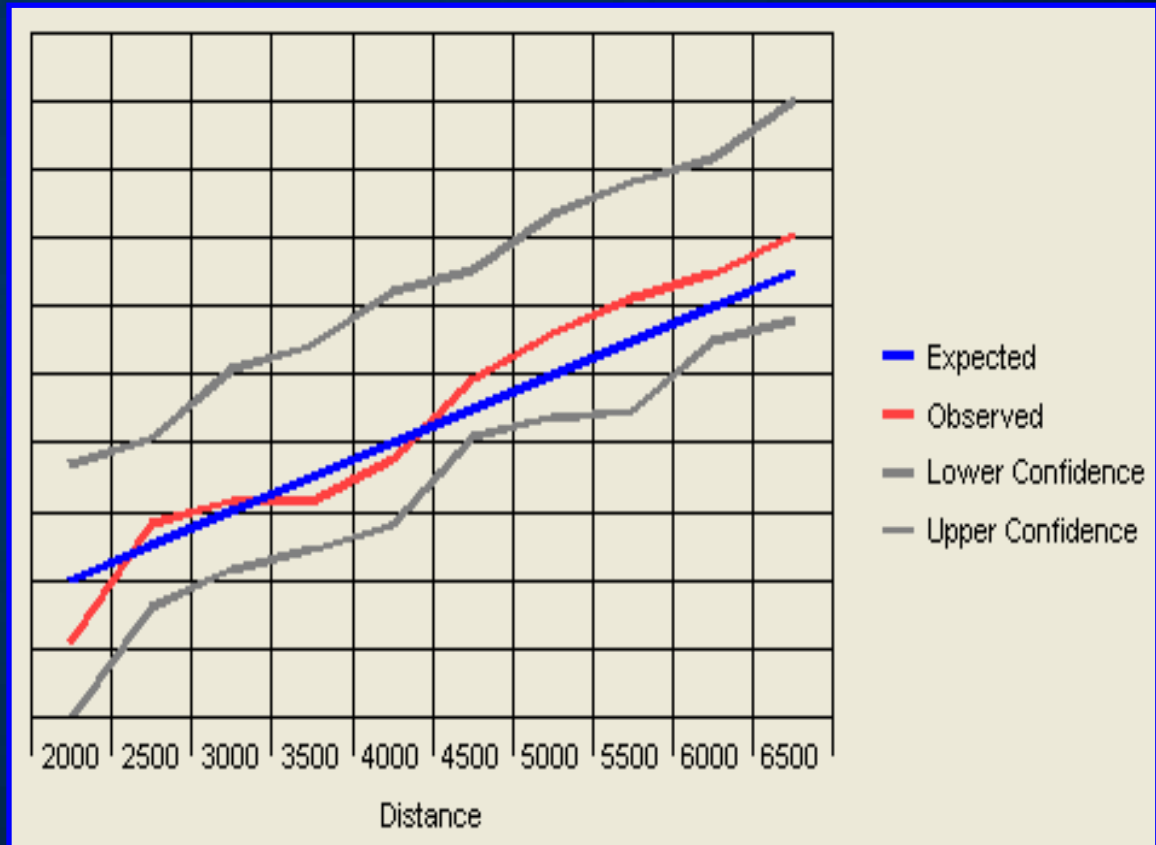
# K Function

- Counts number of pairs within distance  $d$  of each feature



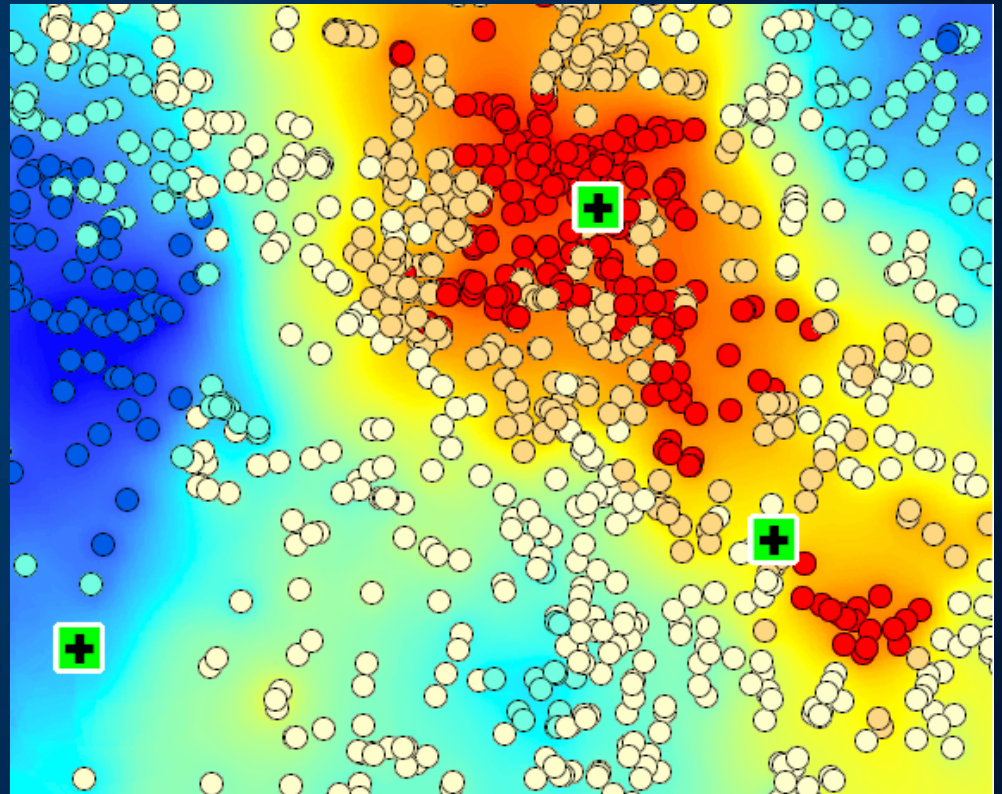
- Interpreting results

A, B  
A, C  
B, A  
B, C  
C, A  
C, B  
= 6 pairs for A



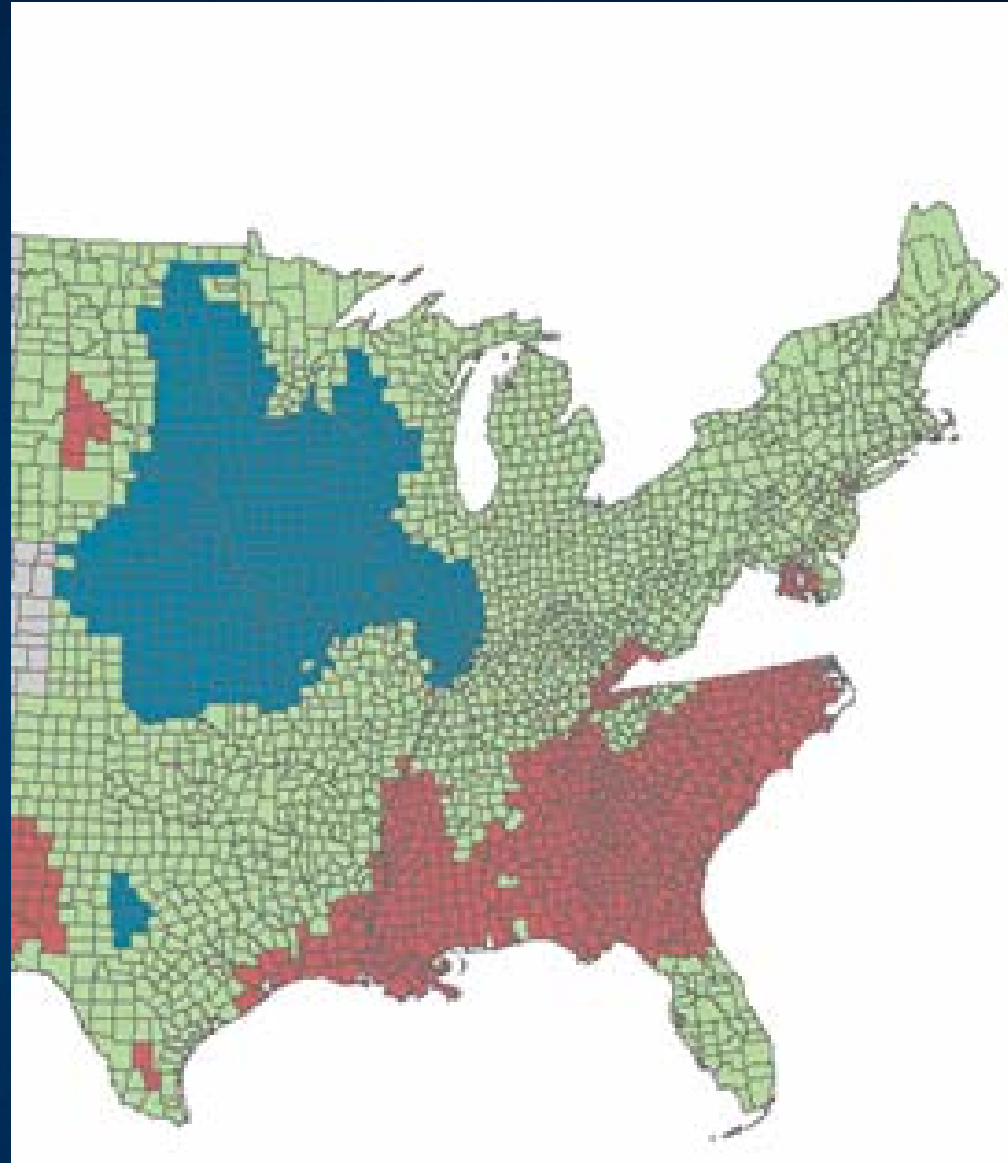
# Mapping Clusters toolset

- Comparing clusters to locations of other features can help to better understand why clusters occur
  - Reveal clustering and/or outliers within a study area
  - Local calculations
    - Considers each feature
    - See differences across the study area
    - Explore how patterns change with changes in spatial scale
1. Hot Spot Analysis (Getis/Ord  $G_i^*$ )
  2. Cluster/Outlier Analysis (Anselin Local Moran's  $I$ )



# Hot spot analysis

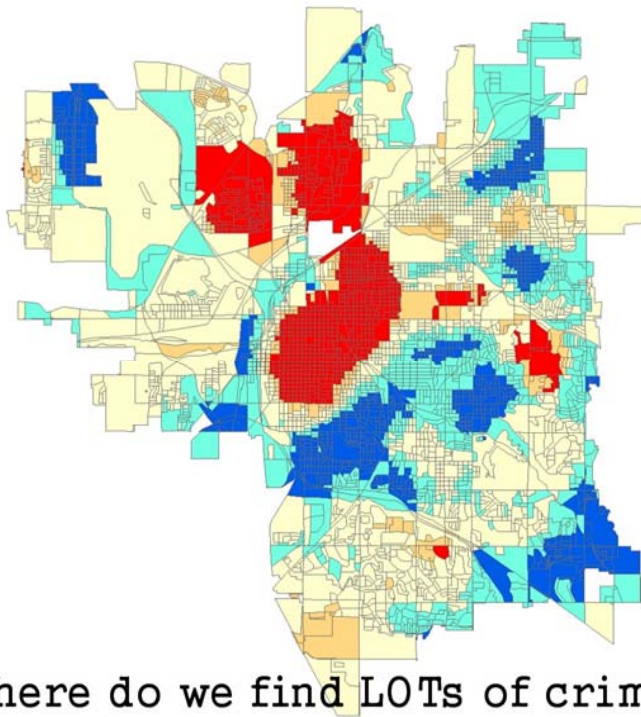
Gi8000
3.36996
-1.28478
-1.1748
-0.53801
-1.9605
0.817222
-1.20506
-2.69827
-0.17904



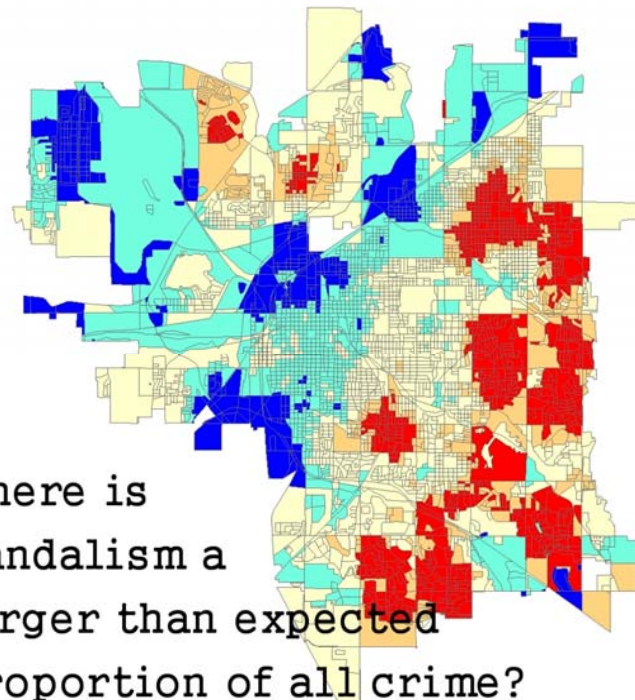


# Hot Spot Analysis (Getis-Ord $G_i^*$ )

- Identifies where clusters of high values and clusters of low values exist in study area
- Calculates a z score for each feature



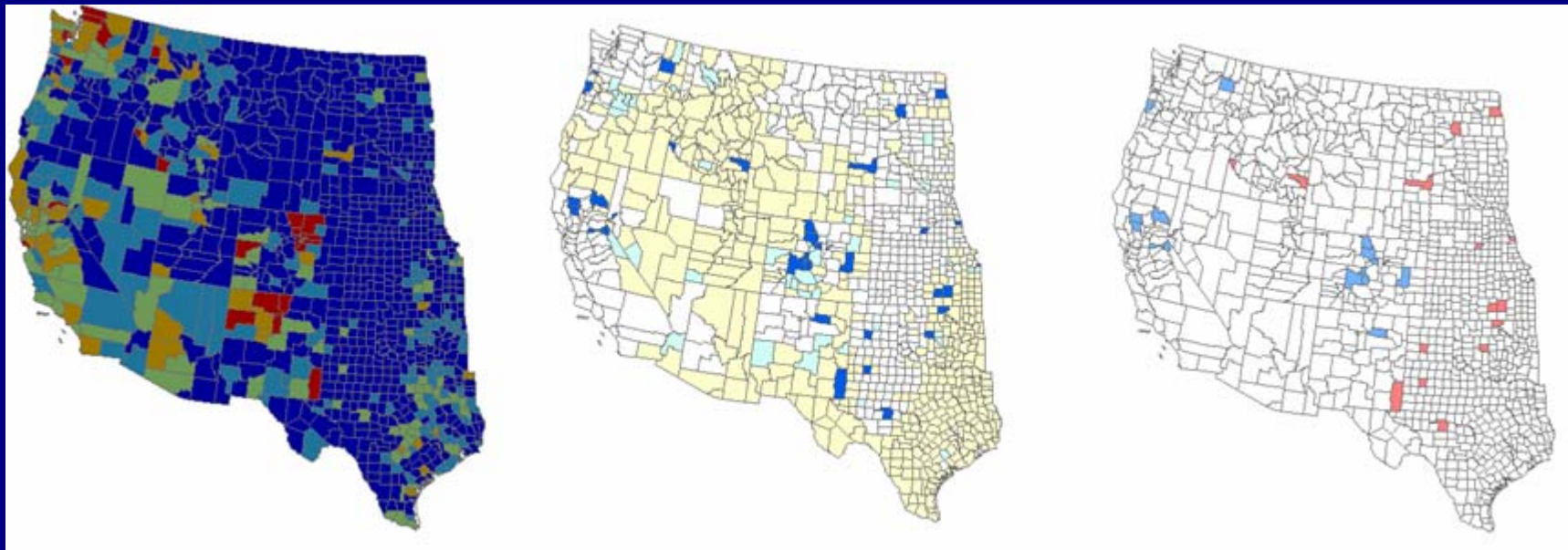
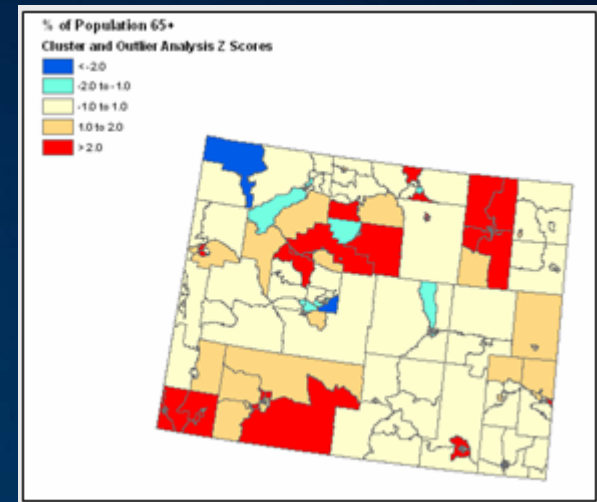
Where do we find LOTs of crime?



Where is  
vandalism a  
larger than expected  
proportion of all crime?

# Cluster and Outlier Analysis (Anselin Local Moran's I)

- Feature location and feature attributes
- Emphasizes how feature values differ in the study area
- Helps identify outliers and errors in data
- Calculates index value and z score



# 911 Emergency Call Demo

# Key Concepts

## 1. What is the weight field?

- a) Collect Events
- b) Aggregate

## 2. What is the scale of analysis?

- a) Sometimes you know
- b) Not too big, not too small
- c) Find the distance where the underlying spatial processes promoting clustering are strongest/most pronounced
- d) Multi-scale exploratory analysis

## 3. What is the question?

- a) Where do we have LOTS of <blap>?
- b) Where do we have a higher than expected *proportion* of <blap> ?

# Health Demographics Analysis

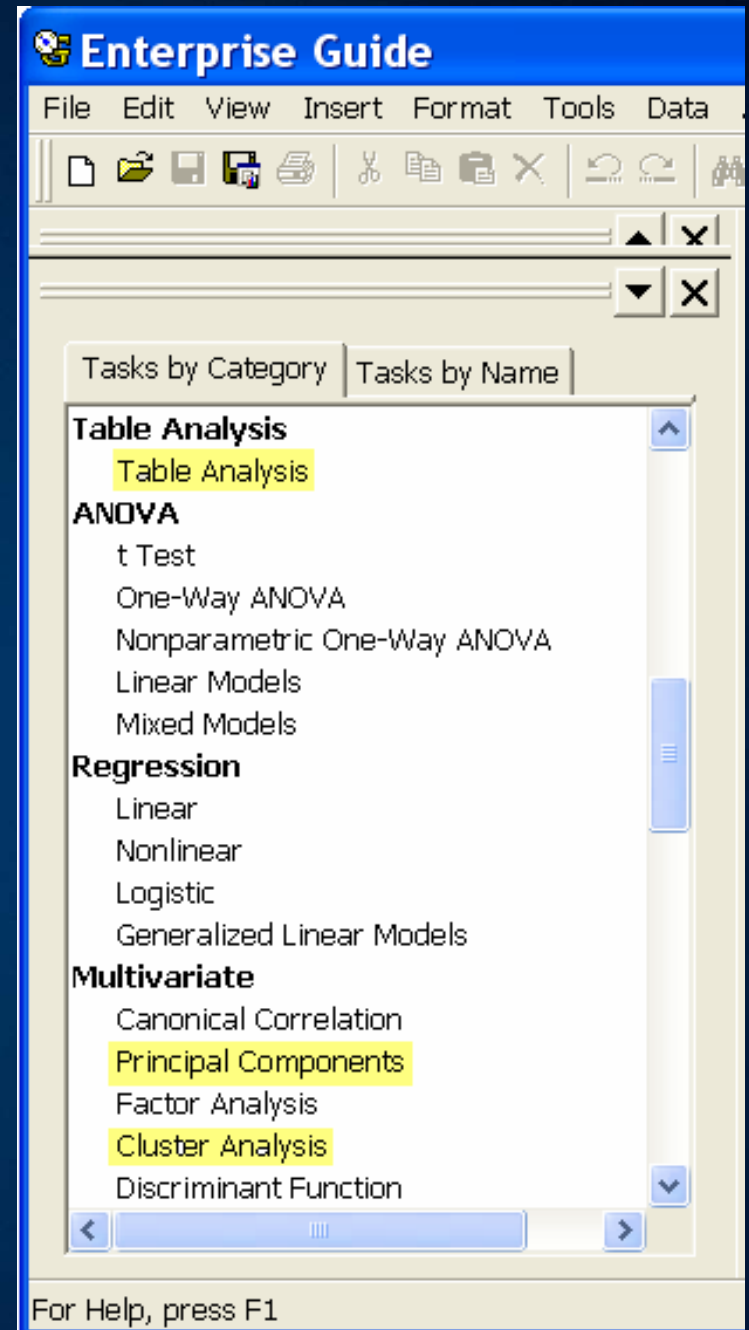
## Goals:

- Analyze US mortality data. Are there regions where the average age at death is persistently younger than expected?
- Explore characteristics of these persistent early death regions. Are there specific factors contributing to early death?



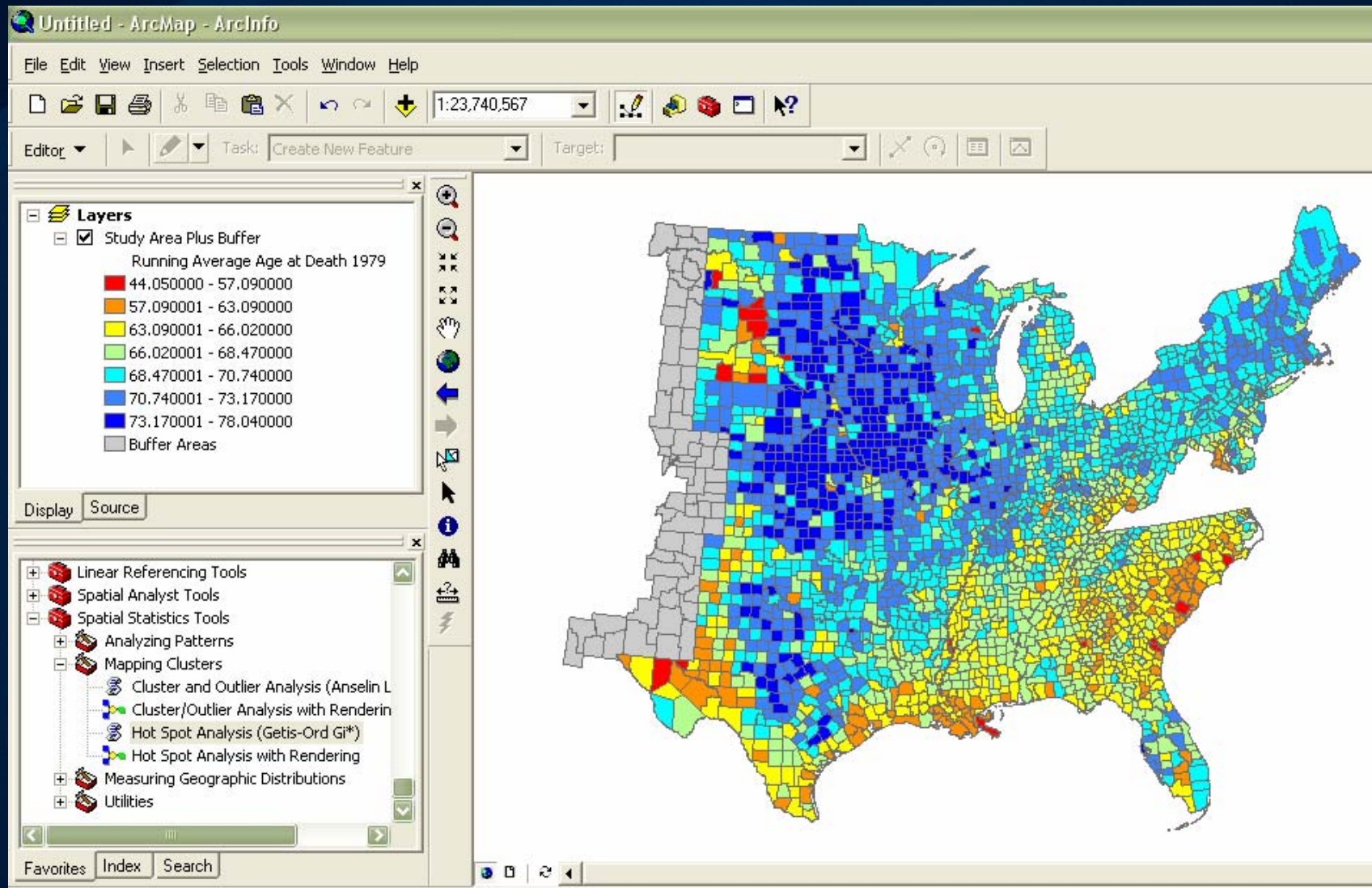
# SAS Statistical Tools

SAS provides traditional (a-spatial) statistics such as Cluster Analysis, Principal Components Analysis and Chi<sup>2</sup>

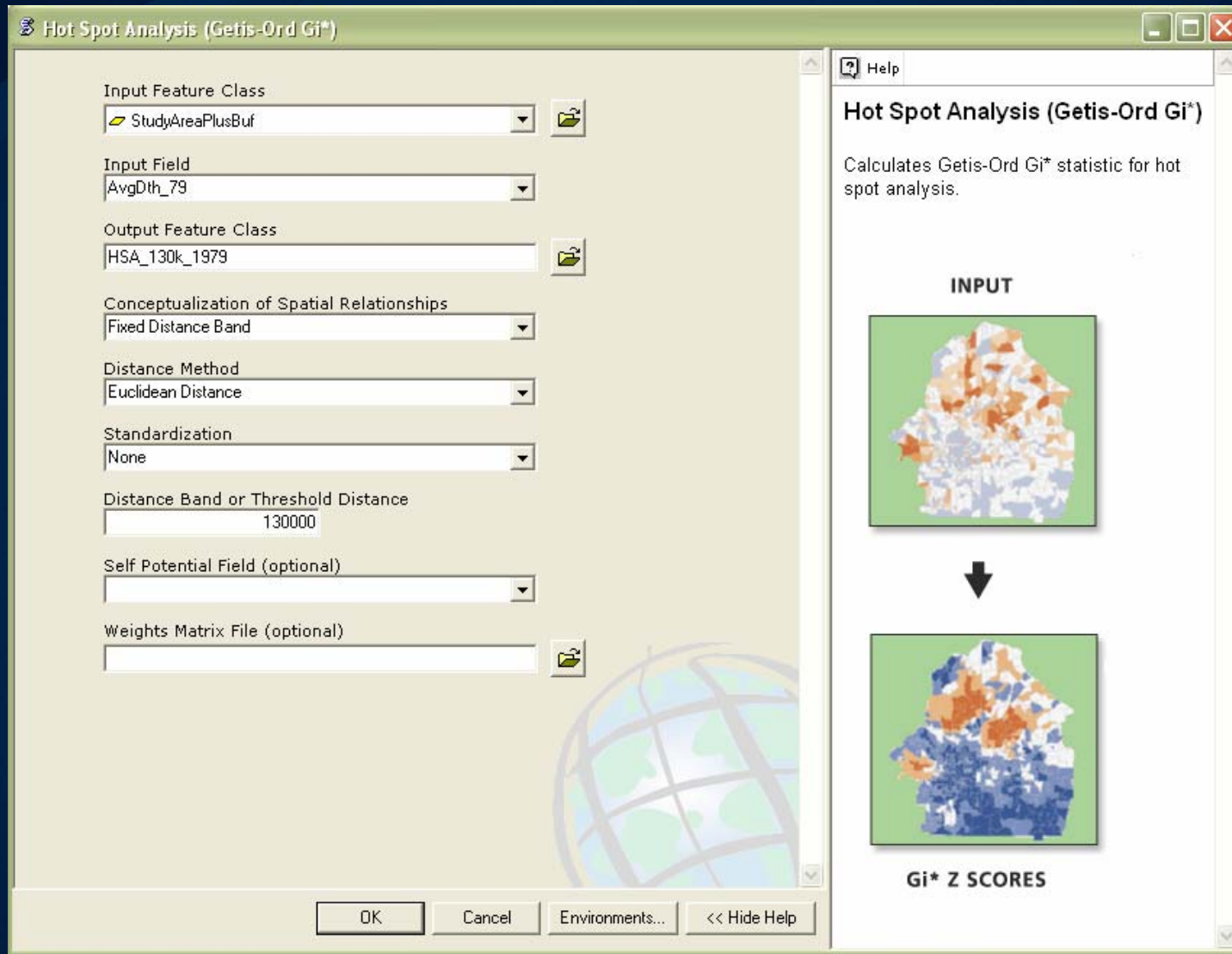




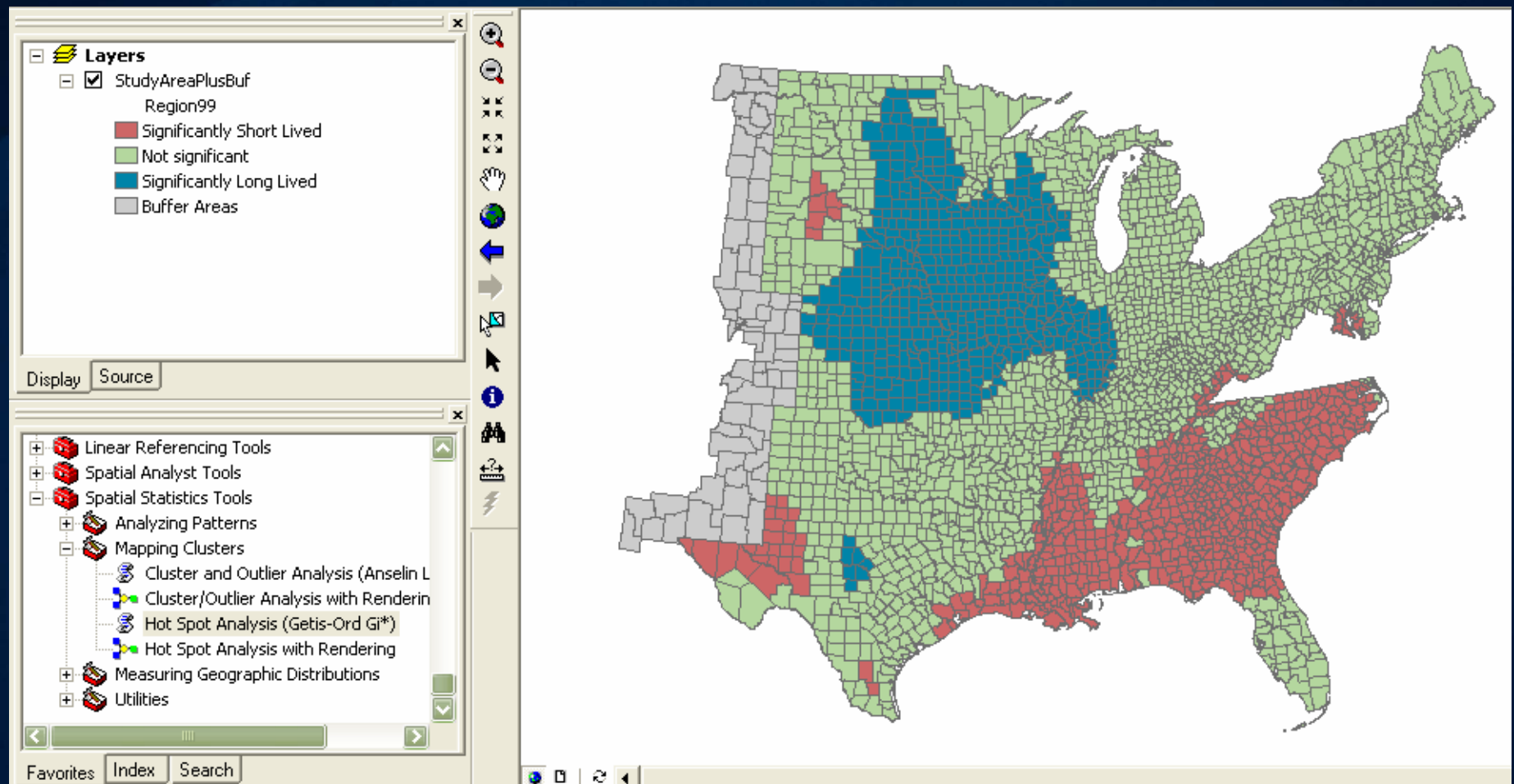
# Average Age at Death in 1979



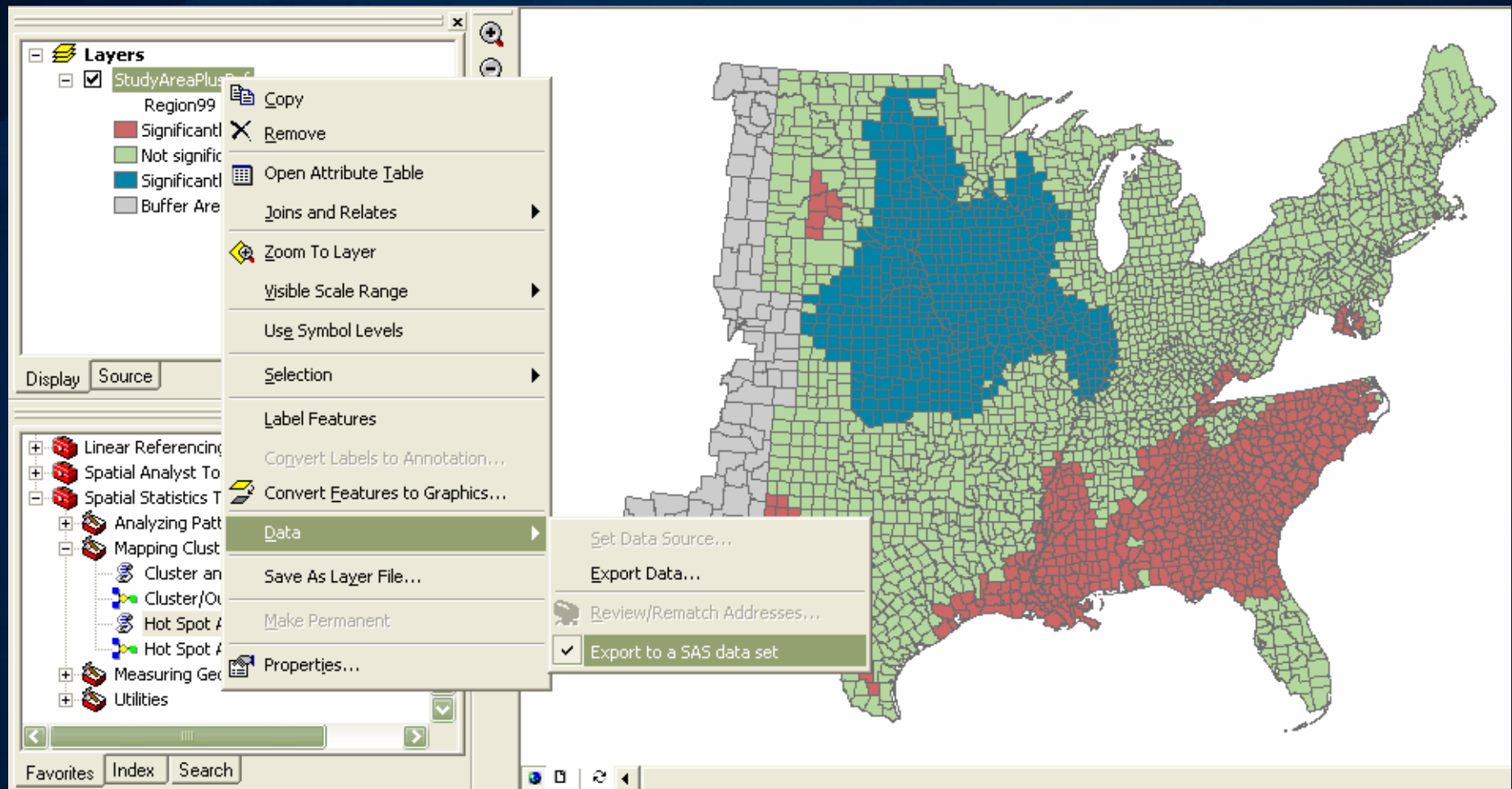
# Identify Hot Spots



# Results from ArcGIS Hot Spot Analysis

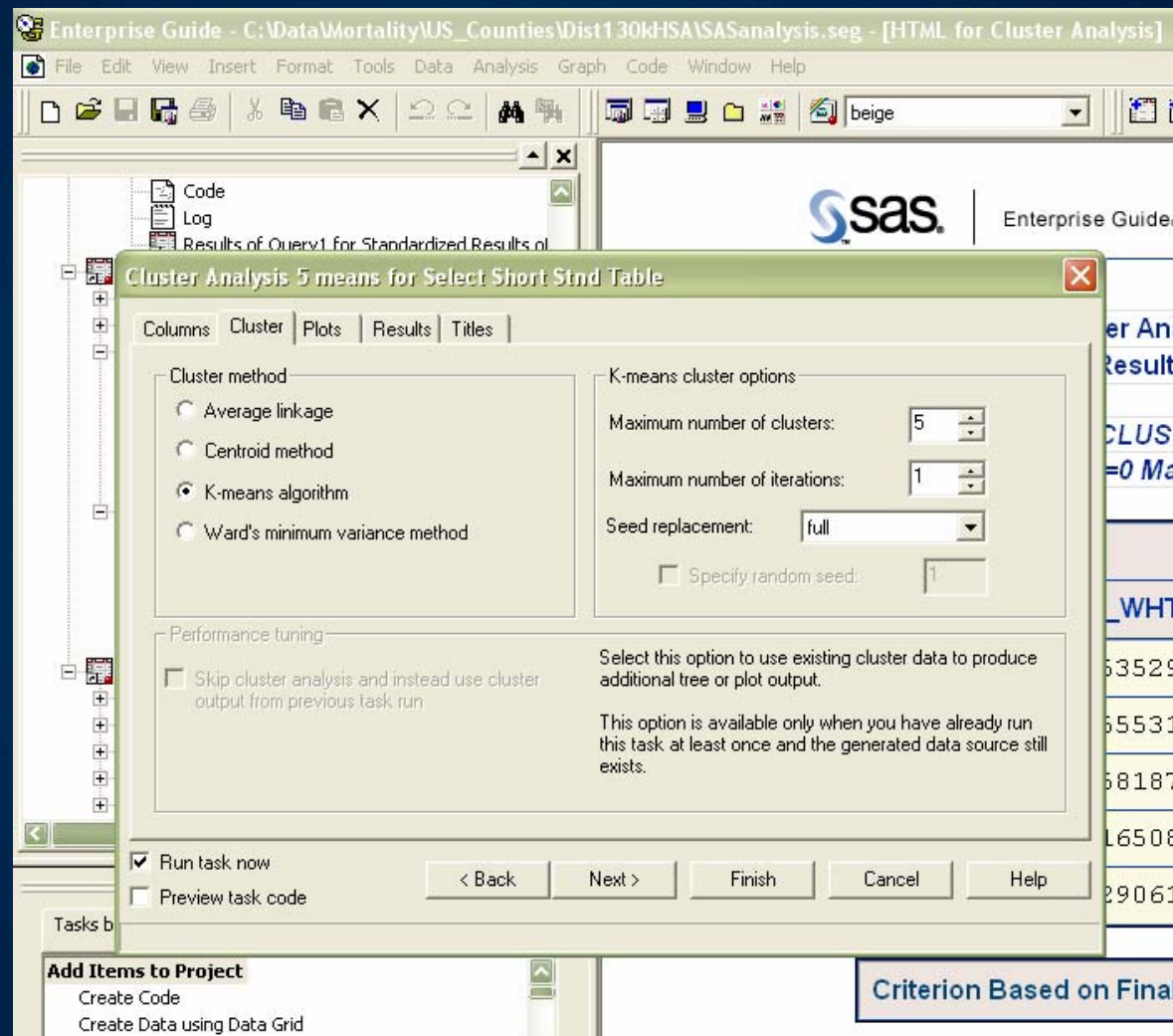


# Export Hot Spot Data to SAS



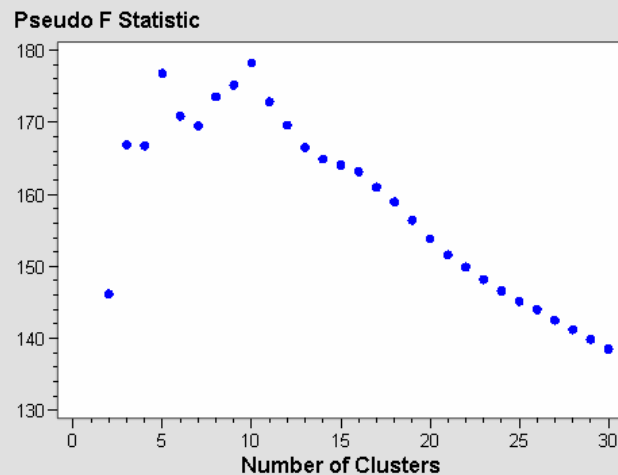


# Cluster Analysis in SAS

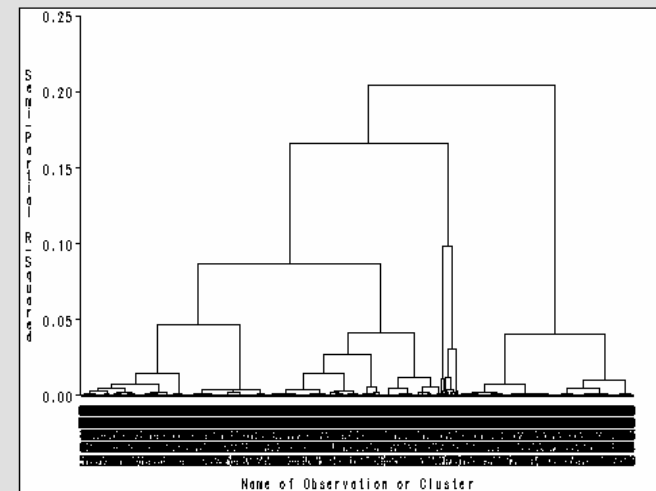


# Exploring Clusters

**Cluster Analysis  
Plots**



**Cluster Analysis  
Tree Chart**



**Correlation**

Pop Density	Docs per 100K	Crime	Asian	Urban	PCI	Med Inc	Med House Inc	Farmland	Beds	White	Black	Amer Ind	Latin
1	0.38168	0.3779	0.34074	0.32043	0.29355	0.23565	0.21367	-0.1553	0.07876	-0.07075	0.06815	-0.02103	-0.01223
	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	0.0002	0.0602	0.0915	0.1041	0.6163	0.7707
Urban	Crime	Asian	Med Fam Income	Doc per 100K	Med House Inc	PCI	Pop Density	Latin	Beds	Amer Ind	Farmland	Black	White
1	0.69104	0.5865	0.49051	0.45674	0.44445	0.43311	0.32043	0.22046	0.21843	-0.09025	0.05491	-0.04648	0.01343
	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	0.0312	0.1905	0.2679	0.7491
White	Black	Med House Income	Med Fam Income	PCI	Farmland	Laint	Amer Ind	Pop Density	Beds	Docs per 100K	Urban	Asian	Crime
1	-0.96071	0.41256	0.37378	0.35357	-0.21944	0.10272	-0.09225	-0.07075	-0.06973	-0.01479	0.01343	0.01009	0.00823
	<.0001	<.0001	<.0001	<.0001	<.0001	0.0141	0.0276	0.0915	0.0963	0.7245	0.7491	0.8101	0.8446



# Chi<sup>2</sup> Analysis

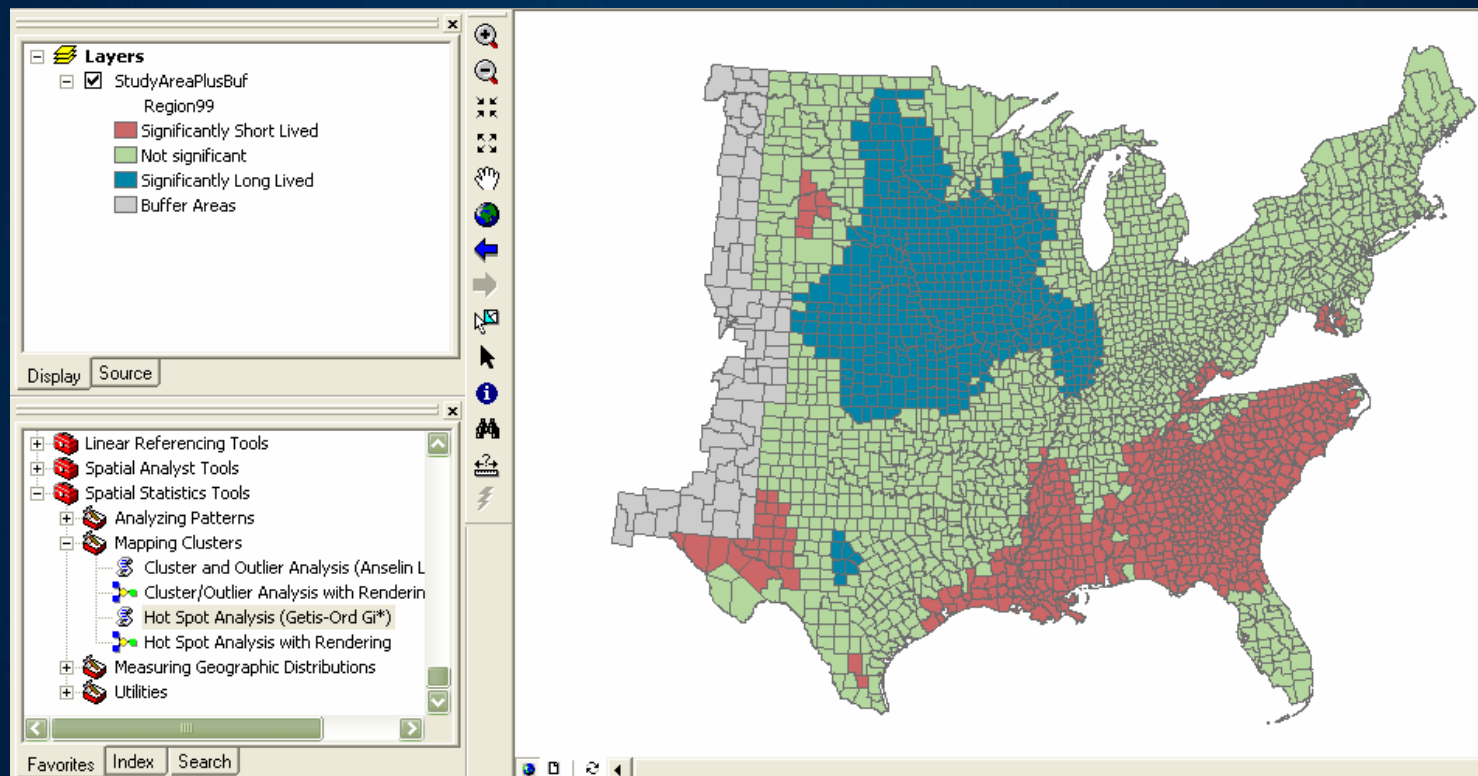
**Chi2 Analysis: Test Relationship between Income and Age at Death**

Household Income	Age At Death		Total
	Younger	Older	
Low	364 63.86	236 43.95	600
High	206 36.14	301 56.05	507
Total	570	537	1107

# Analysis Findings

# Are there regional trends for average age at death?

- Yes, there are persistent statistically significant regions in the US where average age of death is either younger or older than expected



## **Are there specific demographic factors for early death “hot spots”?**

- Lower incomes
- Fewer physicians and hospital beds

## **Are there specific demographic factors for late death “hot spots”?**

- Low crime rates

# Is median income significant?

<b>Average</b>	63.86	43.95	
<b>Above Average</b>	206	301	507
<b>Total</b>	570	537	1107

<b>Square</b>	1	44.4402	<.0001
<b>Continuity</b>			
<b>Adj. Chi-Square</b>	1	43.3645	<.0001
<b>Mantel-Haenszel Chi-Square</b>	1	44.1231	<.0001
<b>Phi Coefficient</b>		0.1997	
<b>Contingency Coefficient</b>		0.1959	
<b>Cramer's V</b>		0.1997	

# Is number of physicians significant?

Chi2 Analysis			
Doctors per 100K	Age at Death		Total
	Younger	Older	
Fewer than Average	301 52.81	254 47.3	555
More than Average	269 47.19	283 52.7	552
Total	570	537	1107

Statistic	DF	Value	Prob
Chi-Square	1	3.3545	0.067
Likelihood Ratio Chi-Square	1	3.3562	0.067
Continuity Adj. Chi-Square	1	3.1378	0.0765
Mantel-Haenszel Chi-Square	1	3.3515	0.0671
Phi Coefficient		0.055	
Contingency Coefficient		0.055	
Cramer's V		0.055	



# Summary

1. Are there persistent hot/cold spots? Where are they?  
(Explore data spatially)
2. Do those hot/cold spots have similar characteristics?  
(Explore the attribute data... a-spatial data analysis)
3. Identify a set of hypotheses
4. Test those hypotheses

# Resources

- 911 emergency call analysis demo:  
<http://www.esri.com/software/arcgis/arcinfo/about/demos.html>
- Virtual campus free seminar  
<http://campus.esri.com/>
- Articles  
[http://www.esri.com/news/arcuser/0405/ss\\_crimestats1of2.html](http://www.esri.com/news/arcuser/0405/ss_crimestats1of2.html)
- Online help (“Modeling Spatial Relationships”)
- Instructor-led ESRI training
- The ESRI Guide to GIS Analysis, Volume 2 by Andy Mitchell

# The ESRI Guide to GIS Analysis

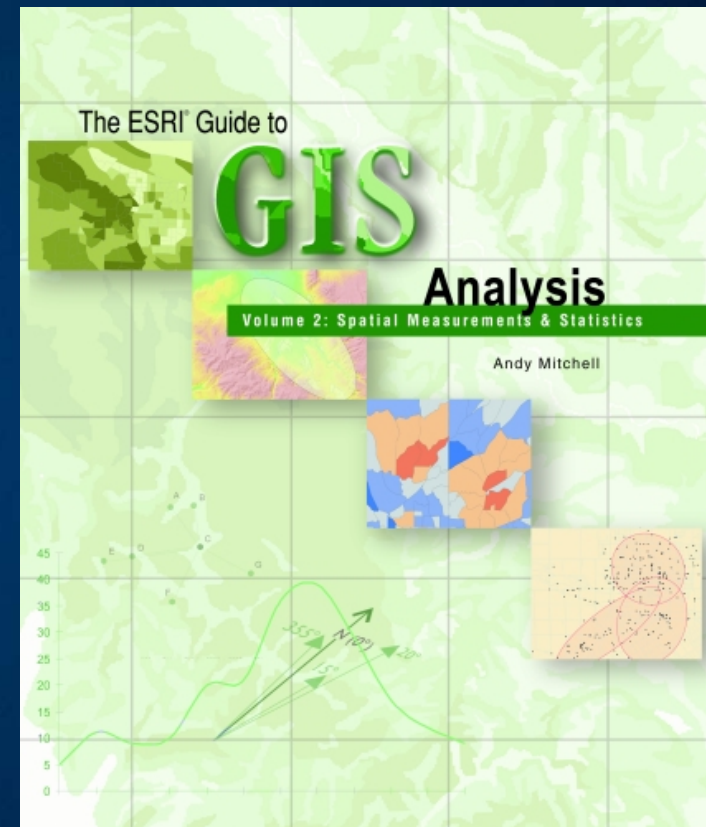
## Volume 2

**Chapter 2: Measuring  
Geographic Distributions**

**Chapter 3: Analyzing patterns**

**Chapter 4: Mapping clusters**

**Chapter 5: Analyzing  
relationships**



# Questions?

**LScott@ESRI.com**