



# Means & Medians to Machine Learning: Spatial Statistics Basics and Innovations

Lauren Bennett, PhD

Ryan Ruthart

Flora Vale

[esriurl.com/spatialstats](https://esriurl.com/spatialstats)

GIS  
INSPIRING  
WHAT'S  
NEXT

What are  
Spatial  
Statistics?

**Spatial Statistics are a set of exploratory techniques for describing and modeling spatial distributions, patterns, processes, and relationships.**

coincidence

area connectivity

proximity

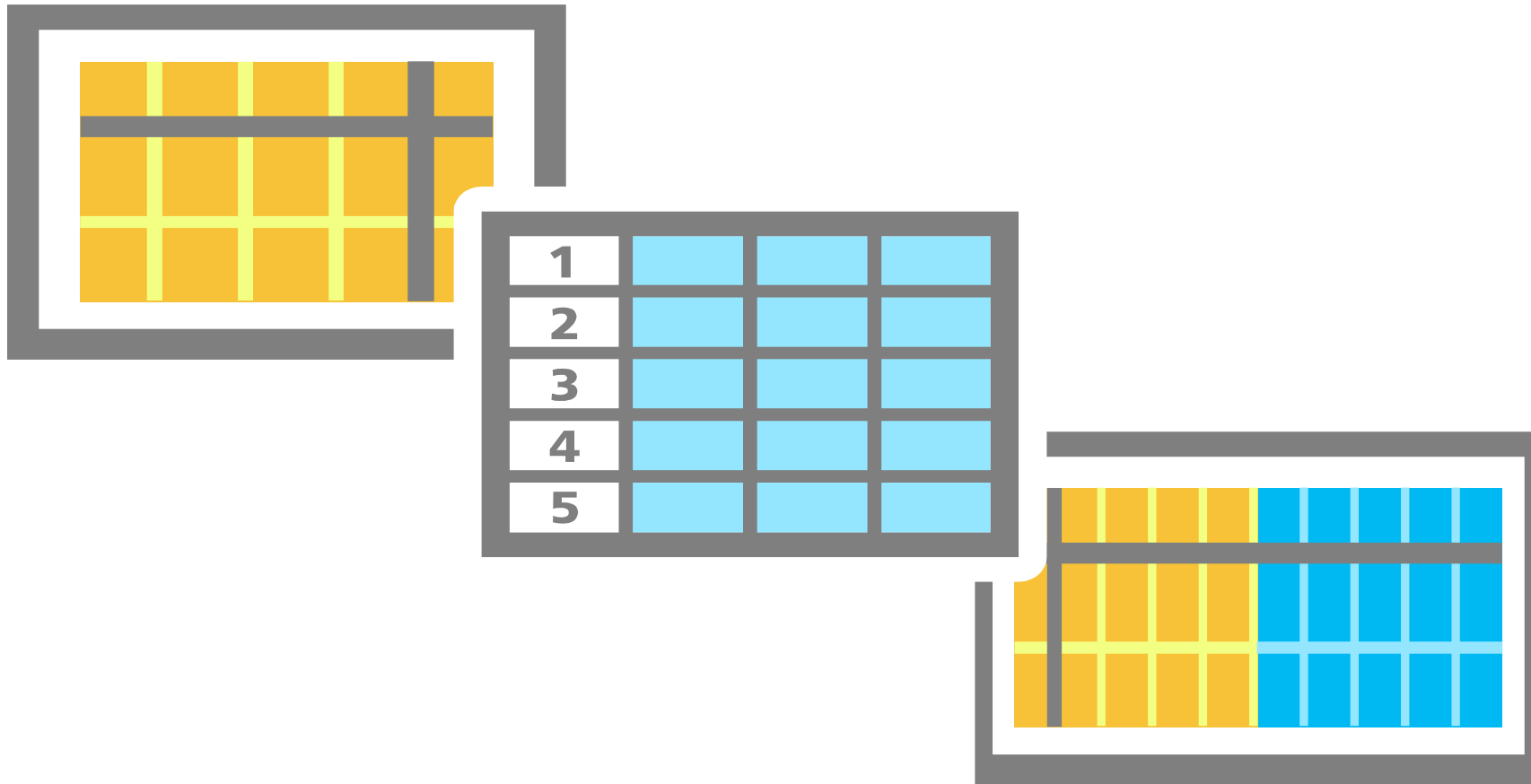
orientation length

direction



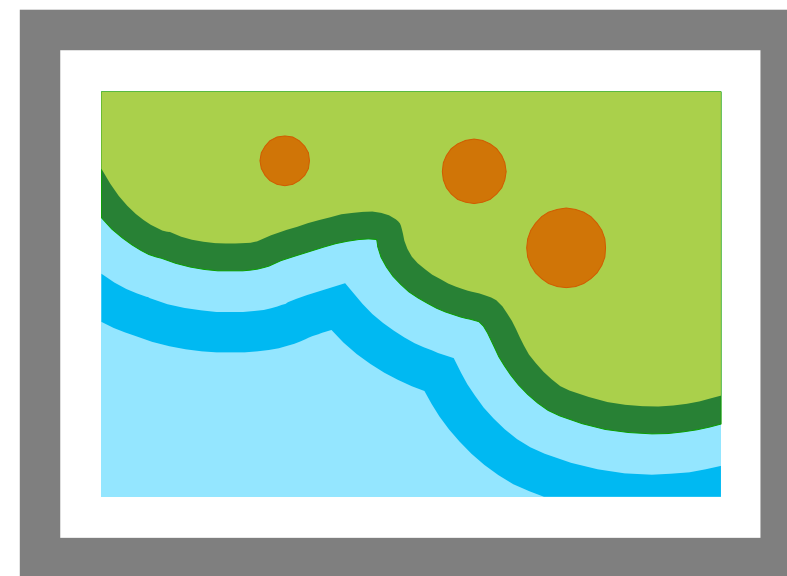
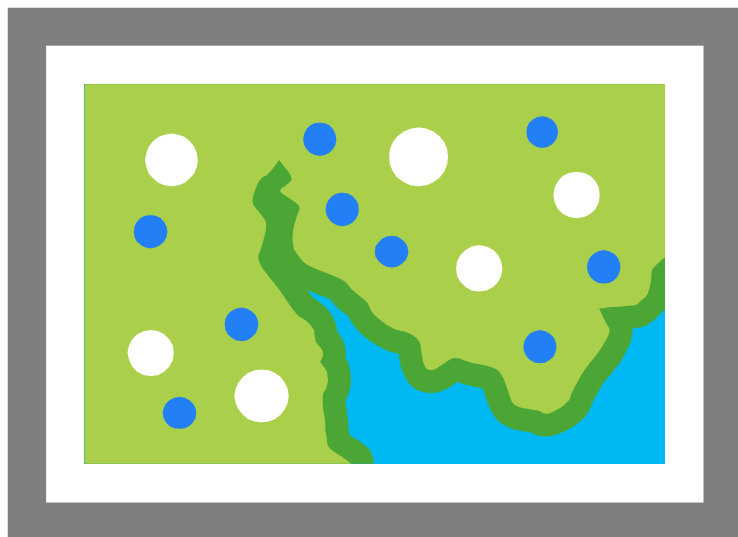
# Spreadsheets

## Data or Information?



# Maps

## Data or Information?



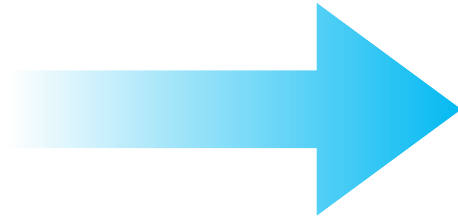
# When you look at a spreadsheet...

1			
2			
3			
4			
5			



# You ask for more

1			
2			
3			
4			
5			

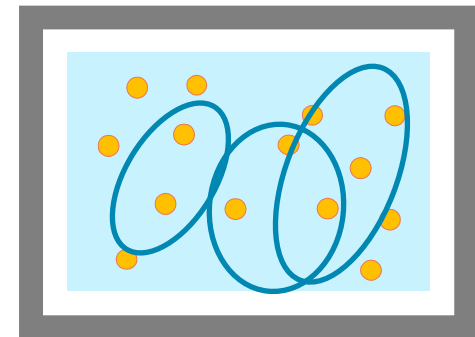
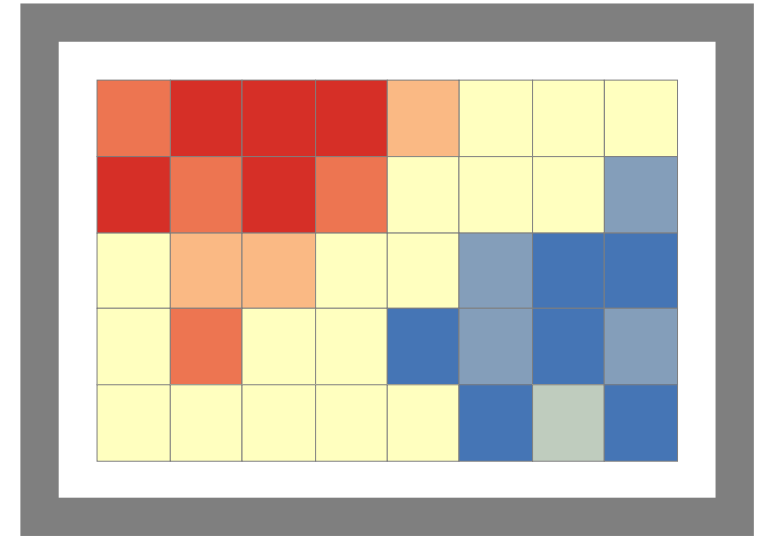
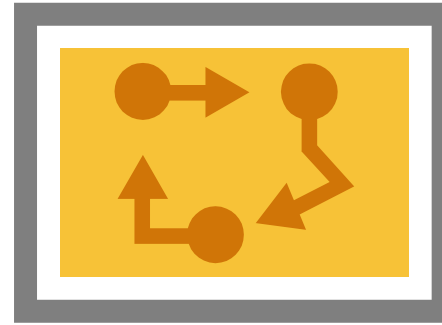
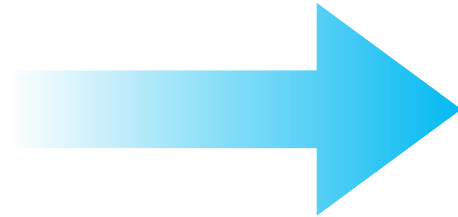


- Mean
- Standard Deviations
- Min and Max
- ...

Same goes for maps!



# We can do more



# Means and Medians

→ summarizing spatial distributions

# Machine Learning

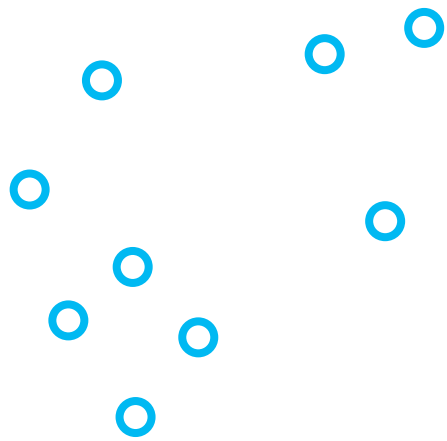
→ clustering methods

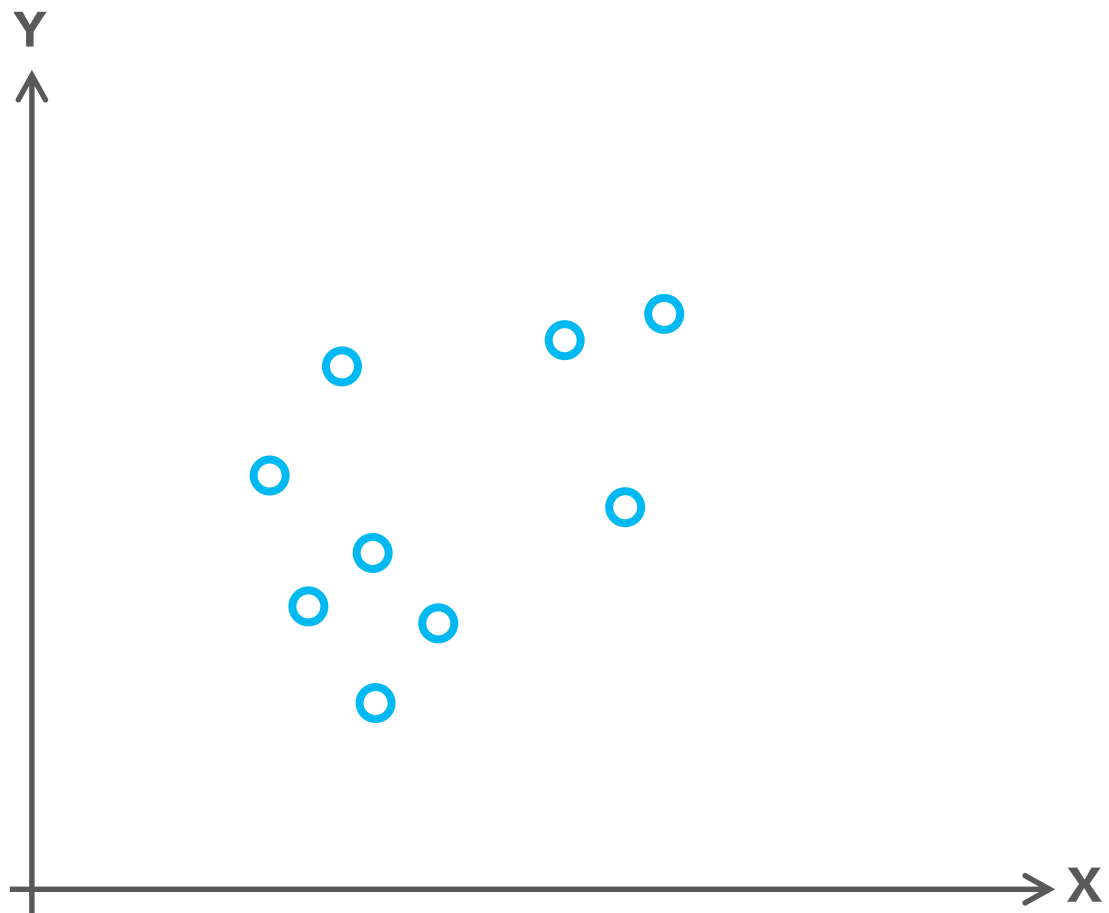
# Means and Medians

summarizing spatial distributions

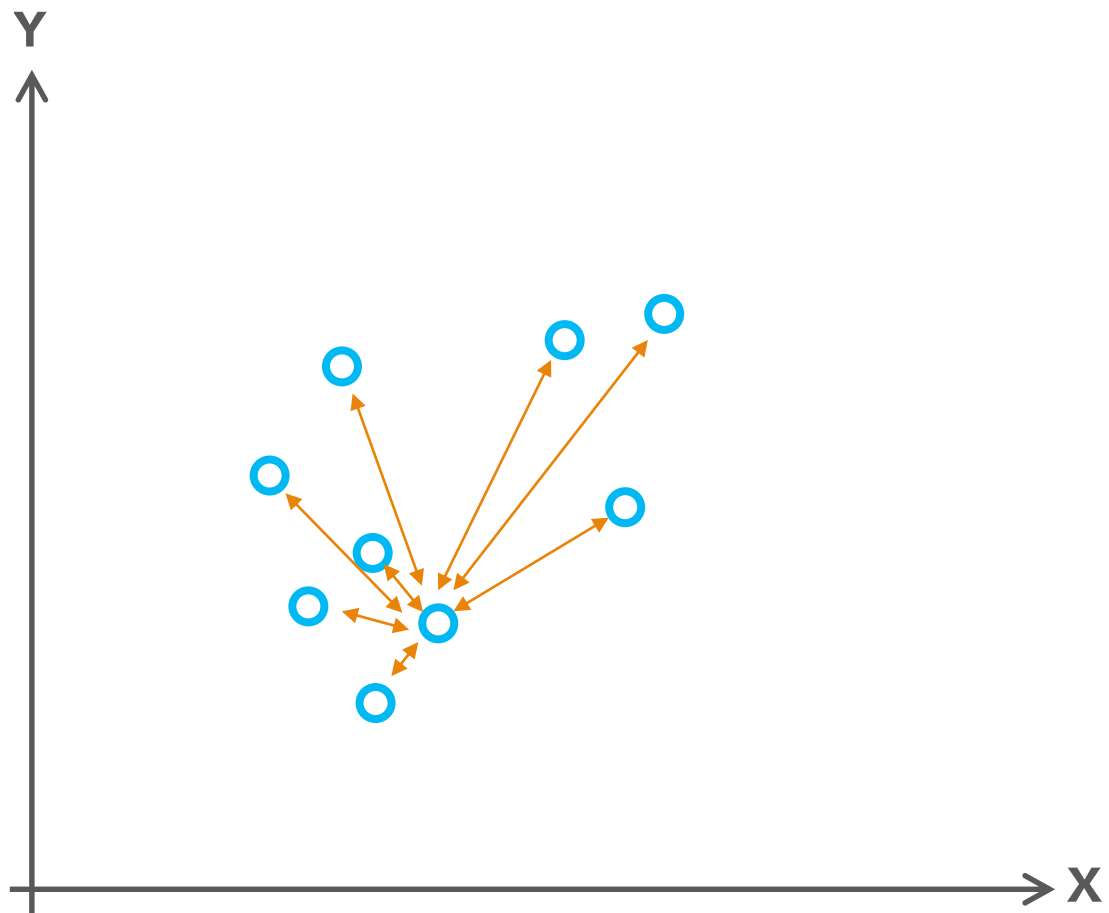
# Central Feature

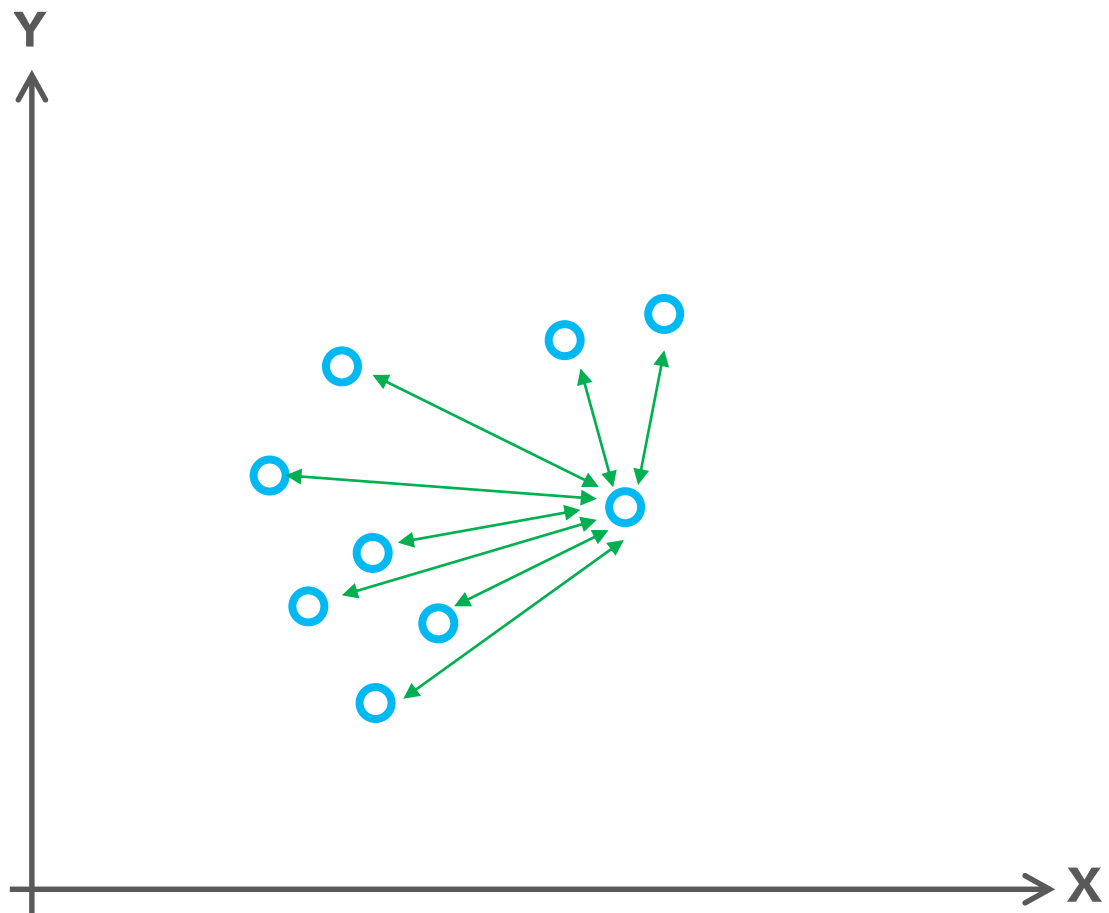
identifies the most centrally located feature  
in a point, line, or polygon feature class

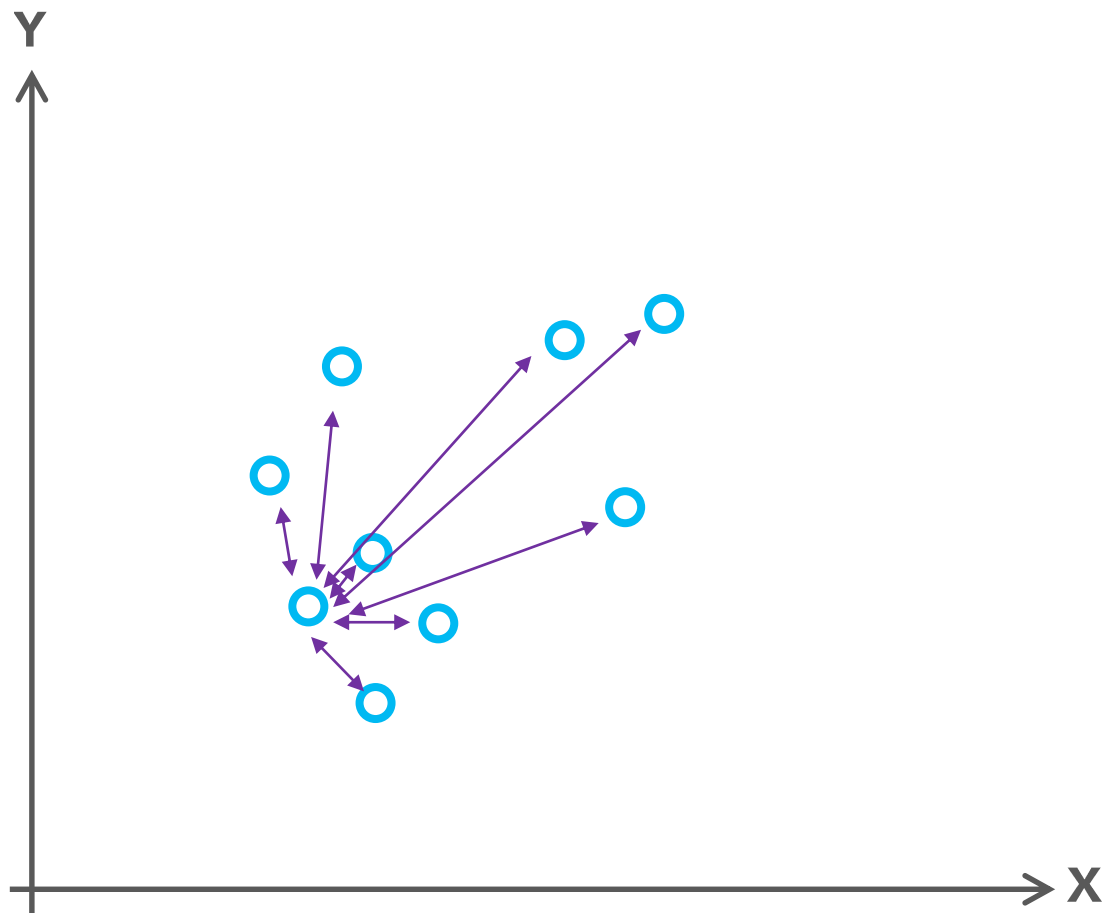


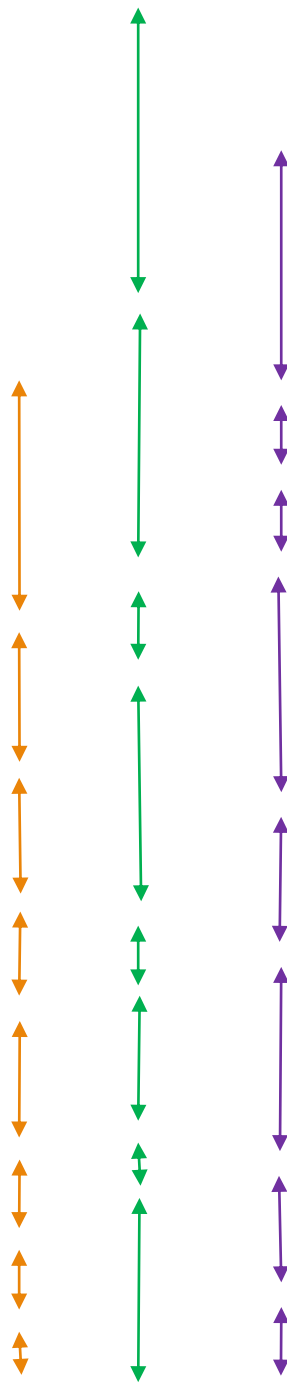
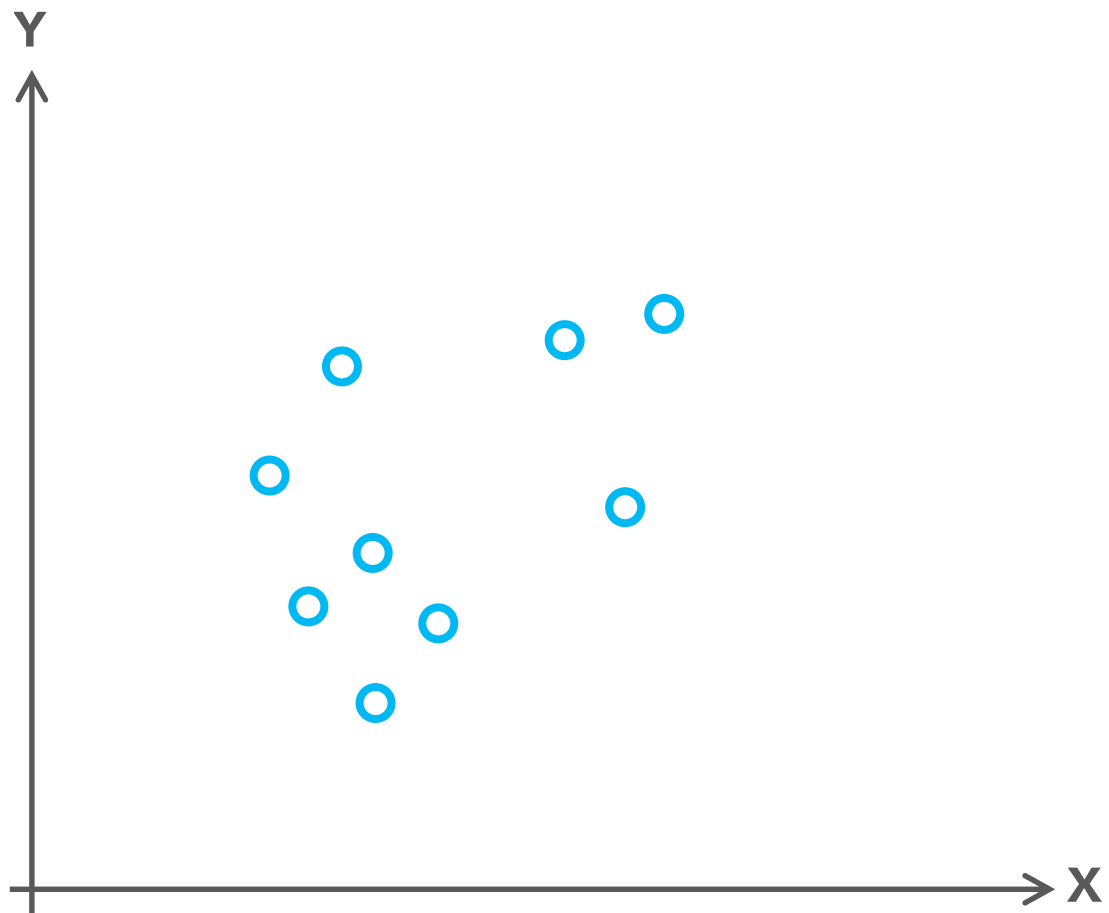


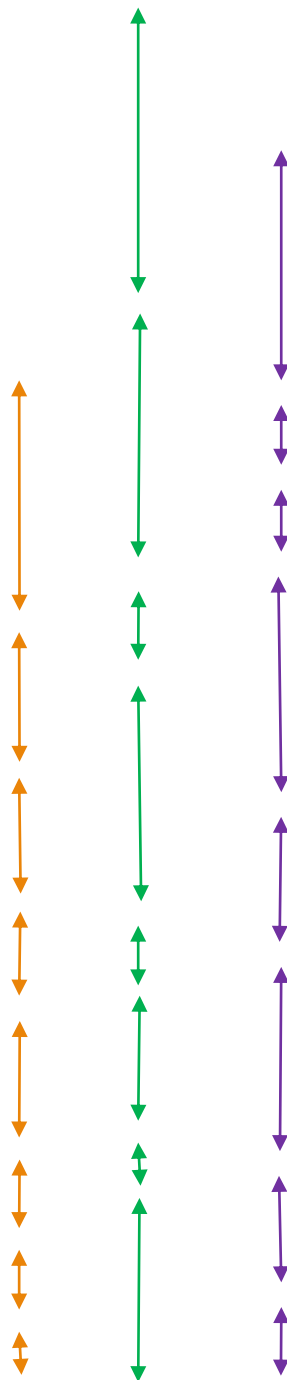
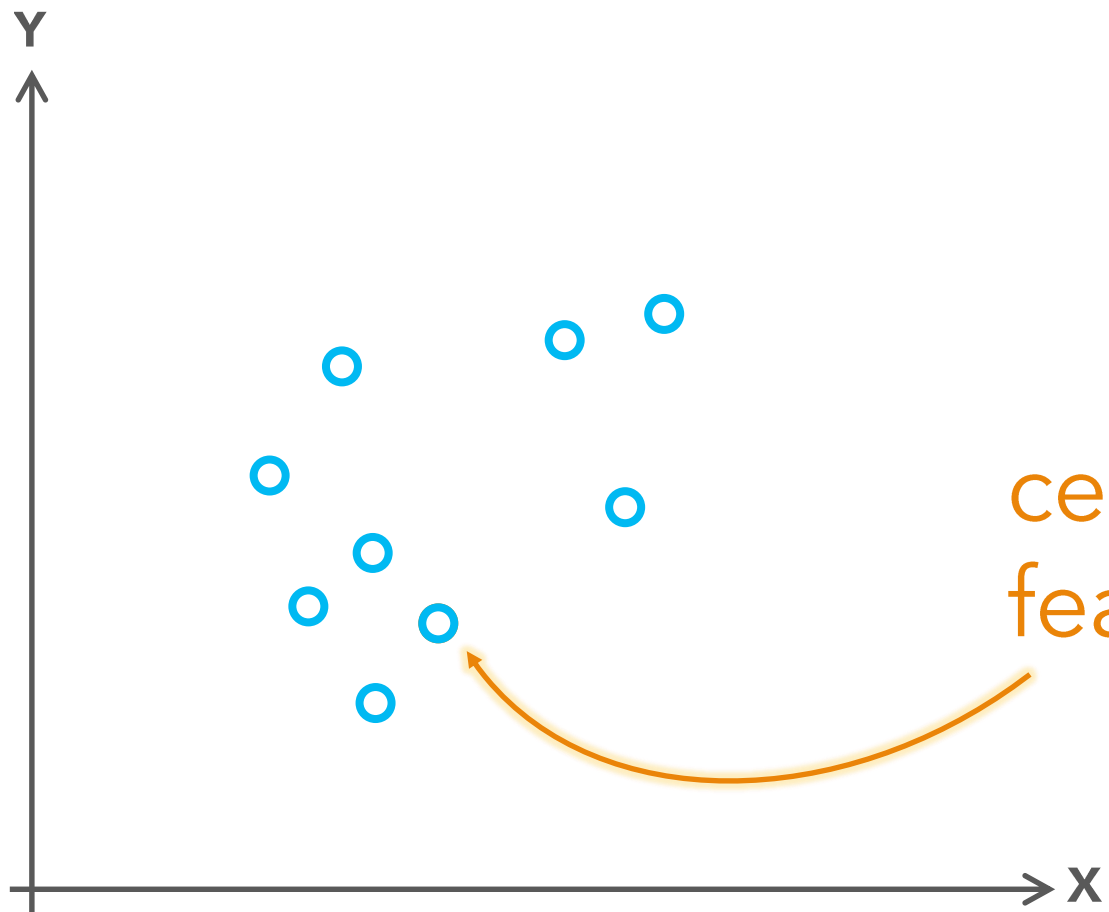






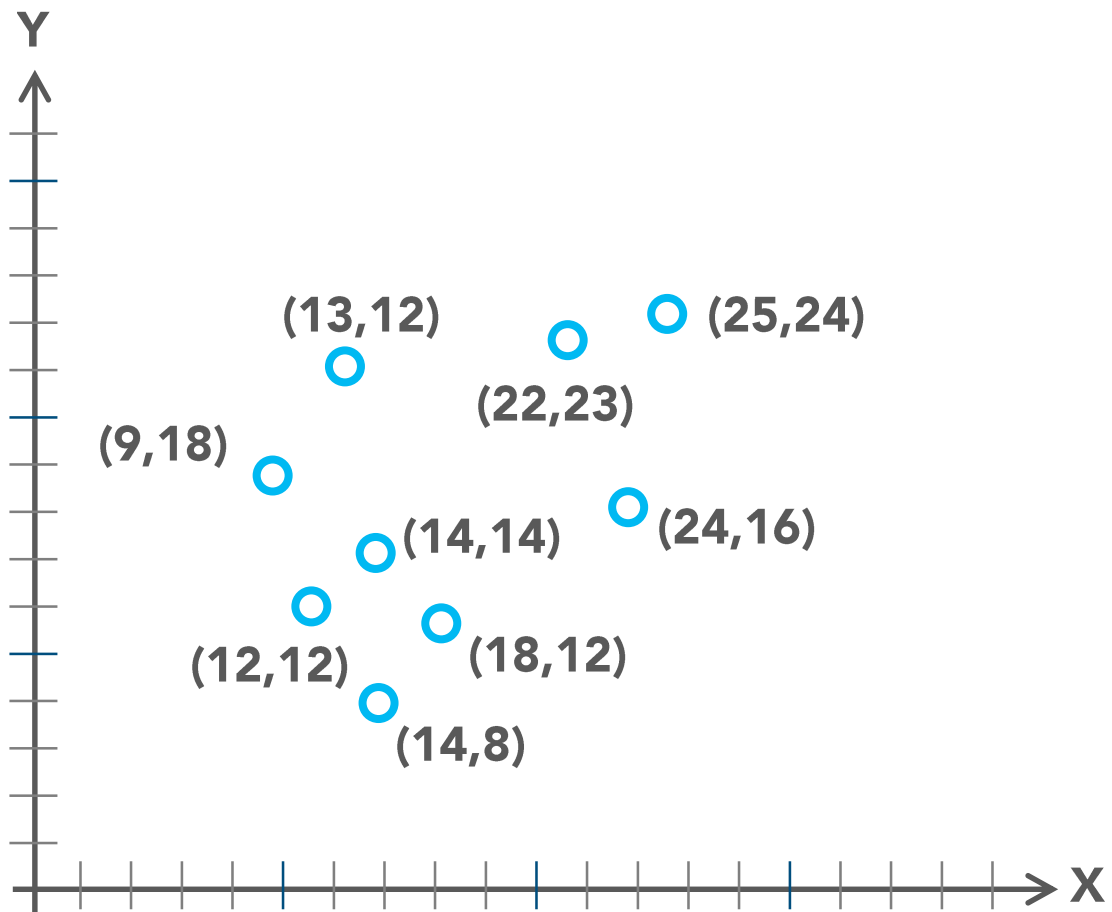


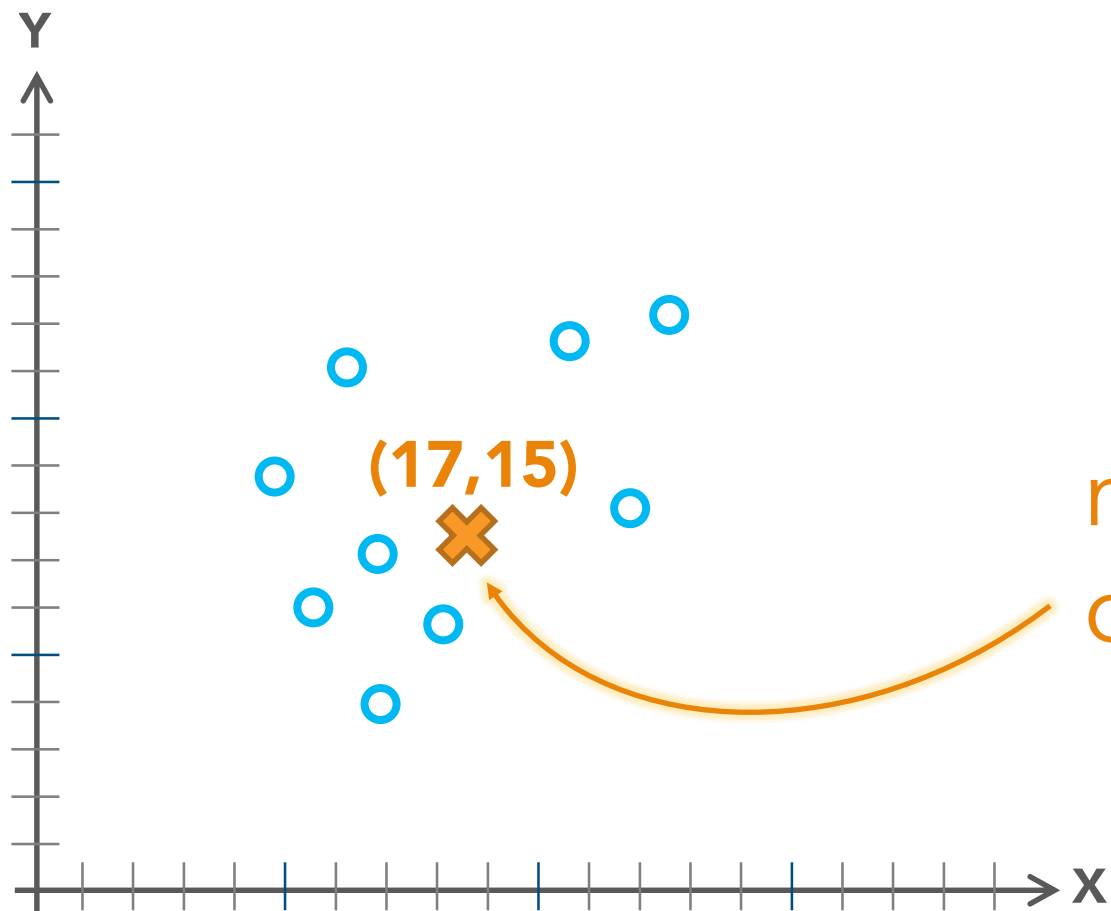




# Mean Center

identifies the geographic center (or the center of concentration) for a set of features





mean  
center

(14,14)

(13,12)

(25,24)

(24,16)

(22,23)

(18,12)

(12,12)

(14,8)

(9,18)

---

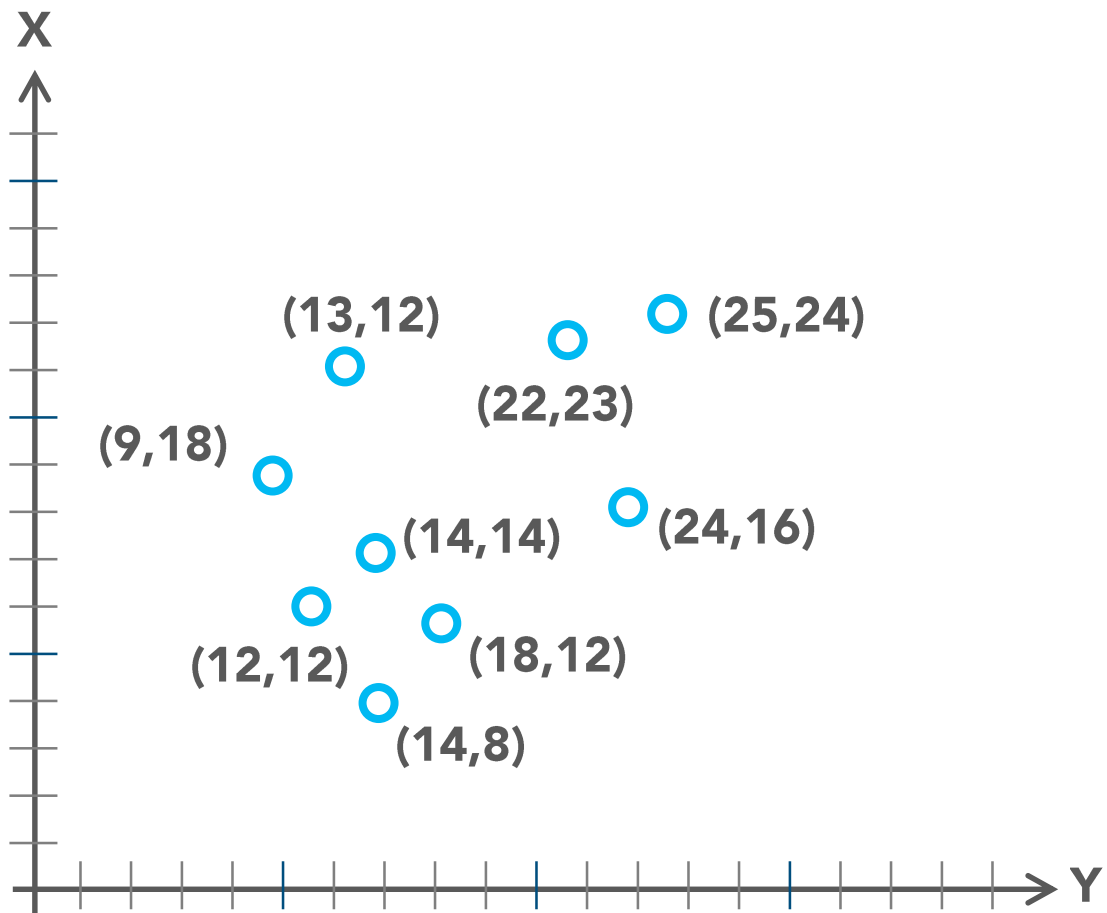
mean =

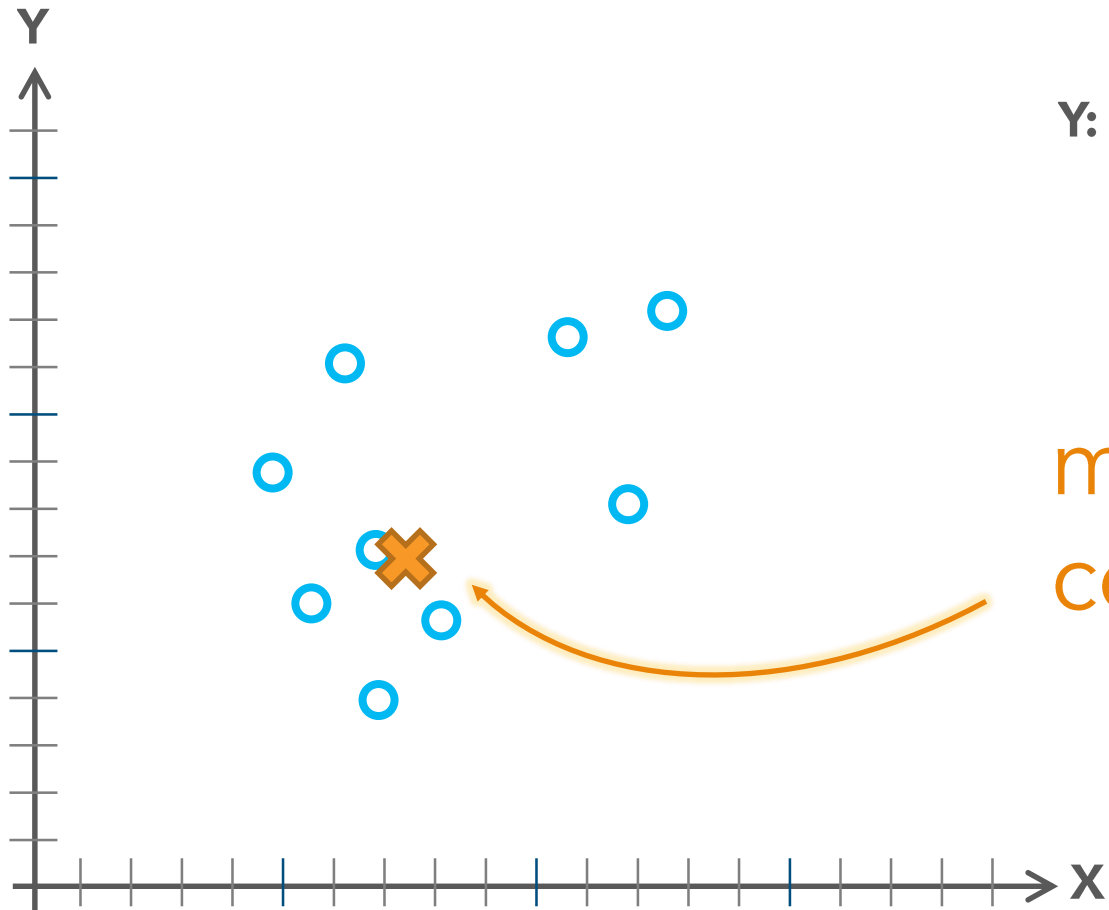
**(17,15)**



# Median Center

identifies the location that minimizes overall Euclidean distance to the features in a dataset





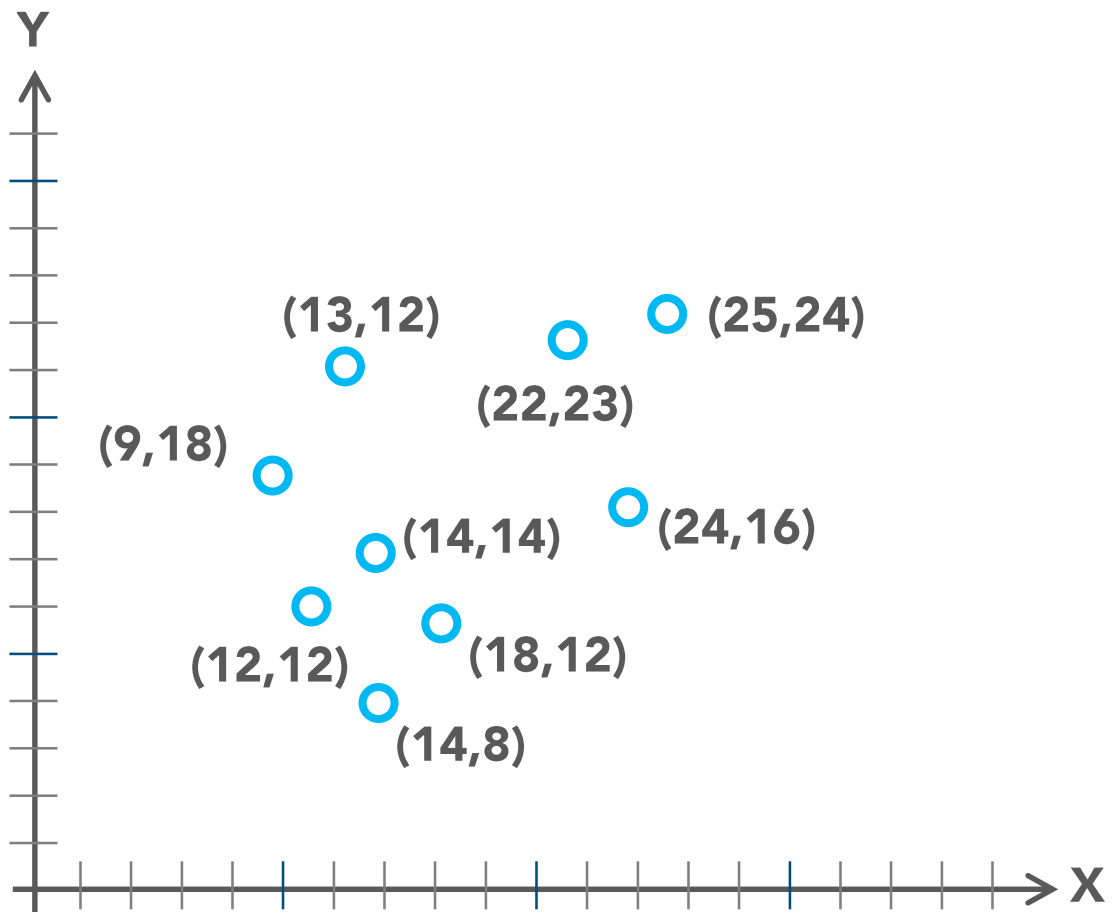
X: ~~25~~ . ~~24~~ . ~~22~~ . ~~18~~ . 14 . ~~14~~ . ~~13~~ . ~~12~~ . ~~9~~

Y: ~~24~~ . ~~23~~ . ~~18~~ . ~~16~~ . 14 . ~~12~~ . ~~12~~ . ~~12~~ . ~~8~~

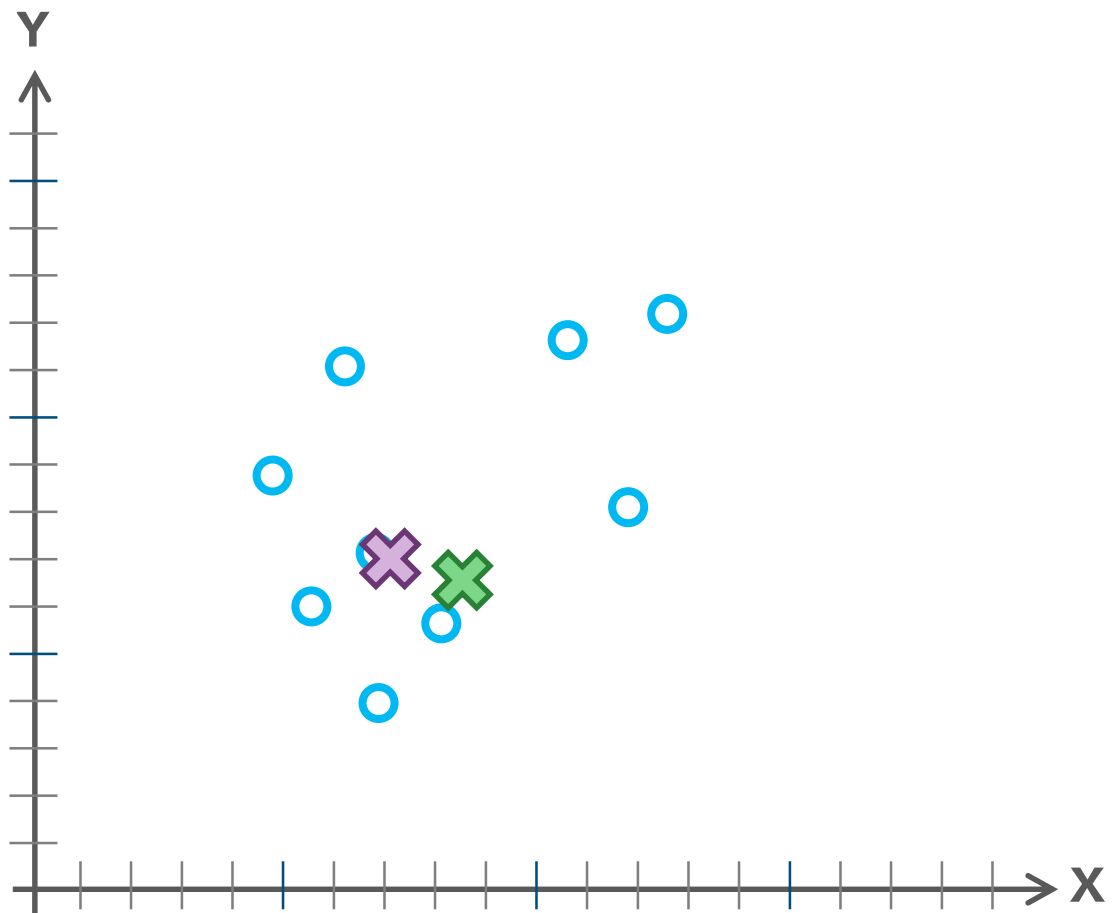
median = (14,14)

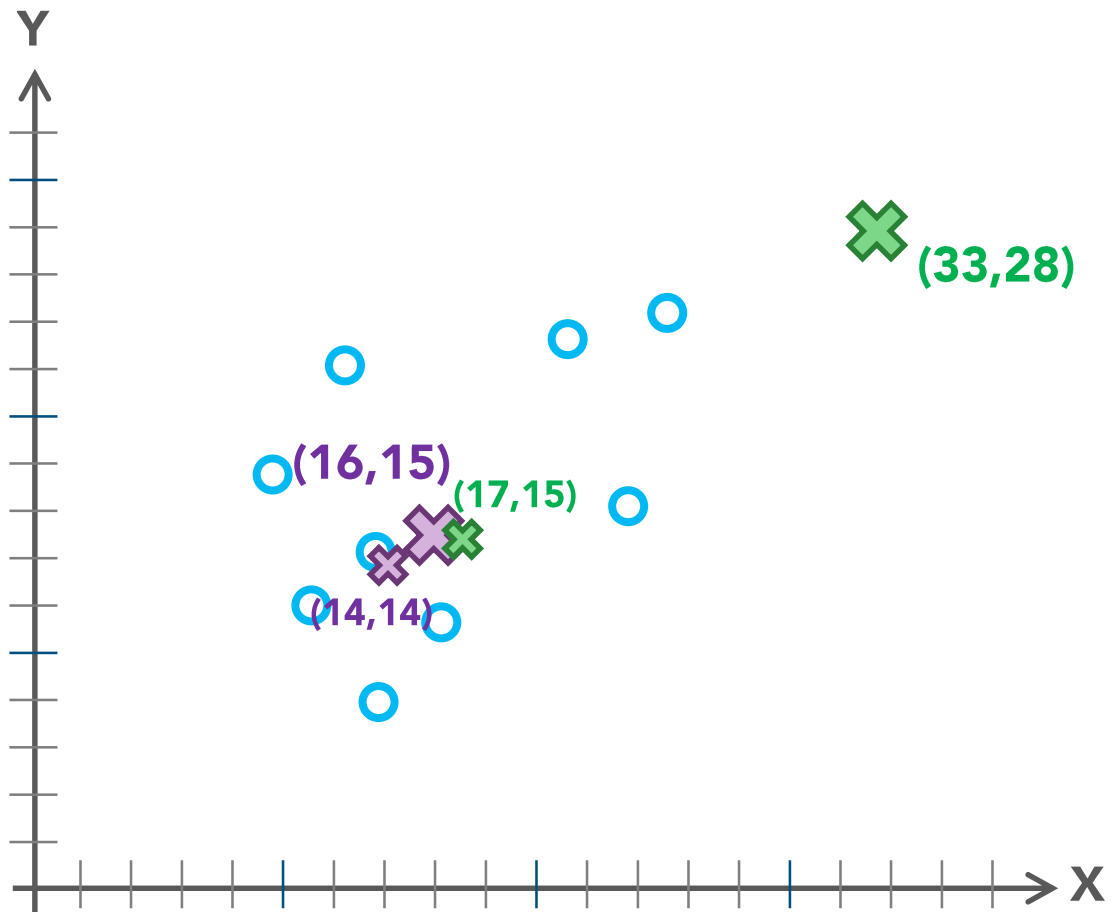
median  
center

# Mean vs Median?

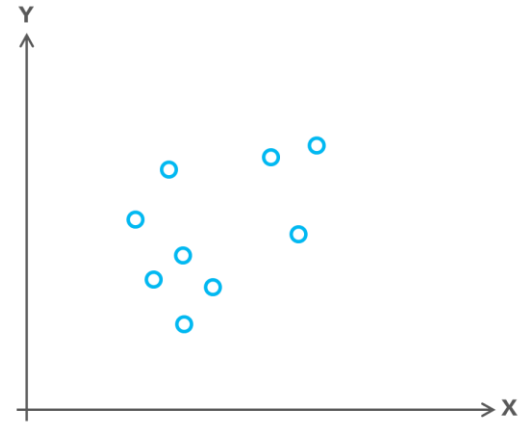


(176,138)





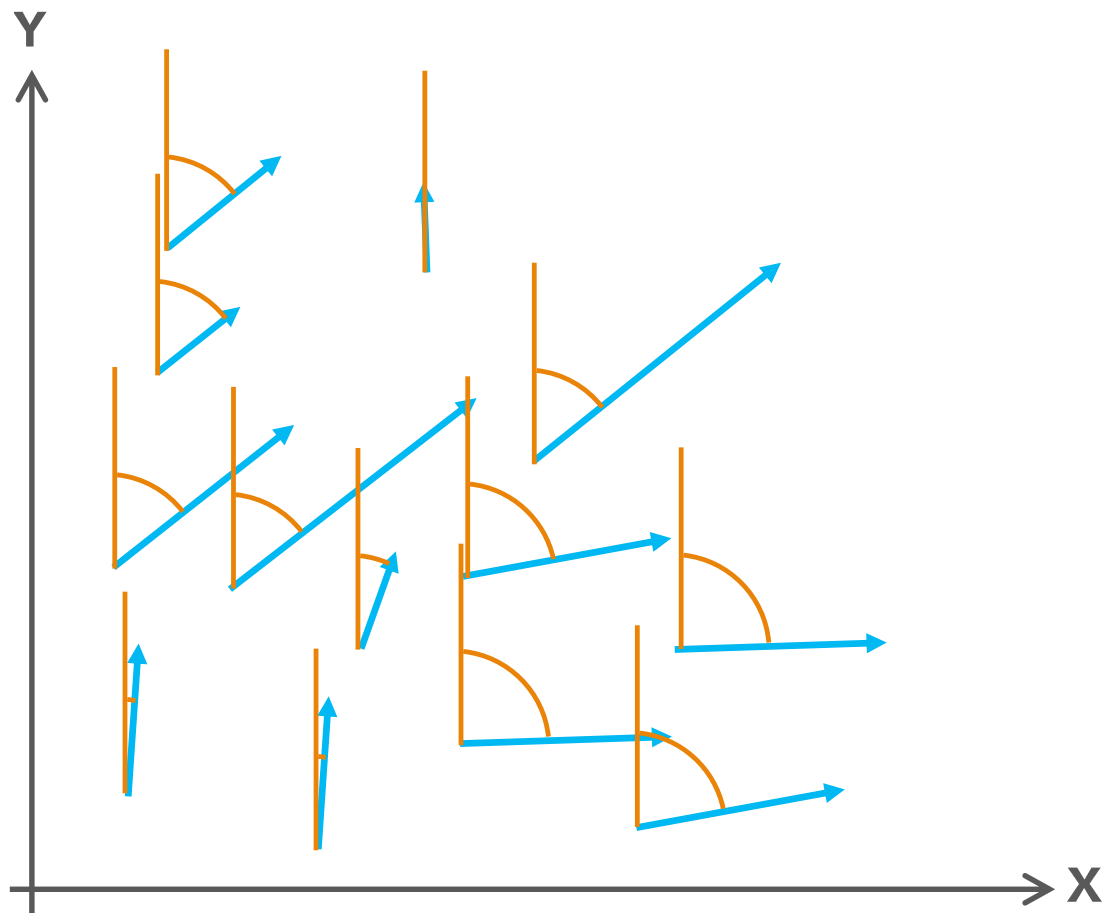
# Demo

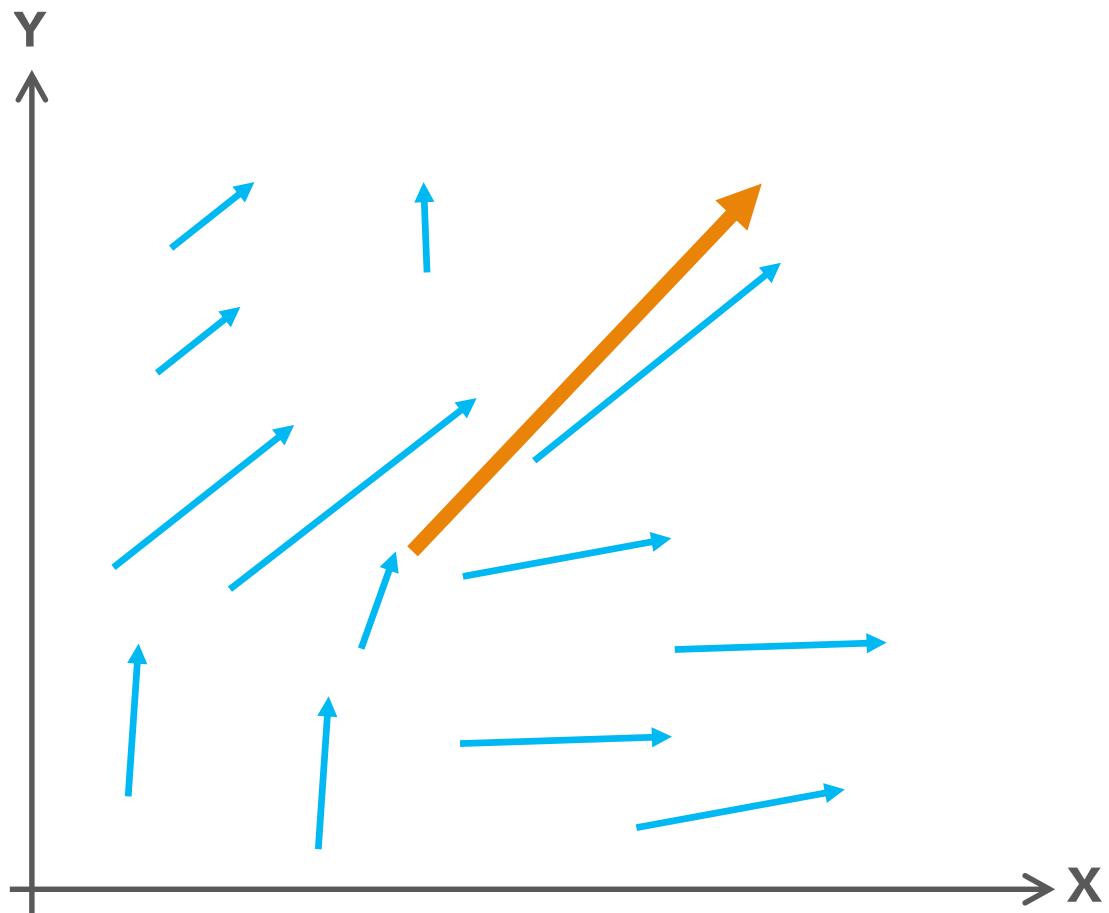




# Linear Directional Mean

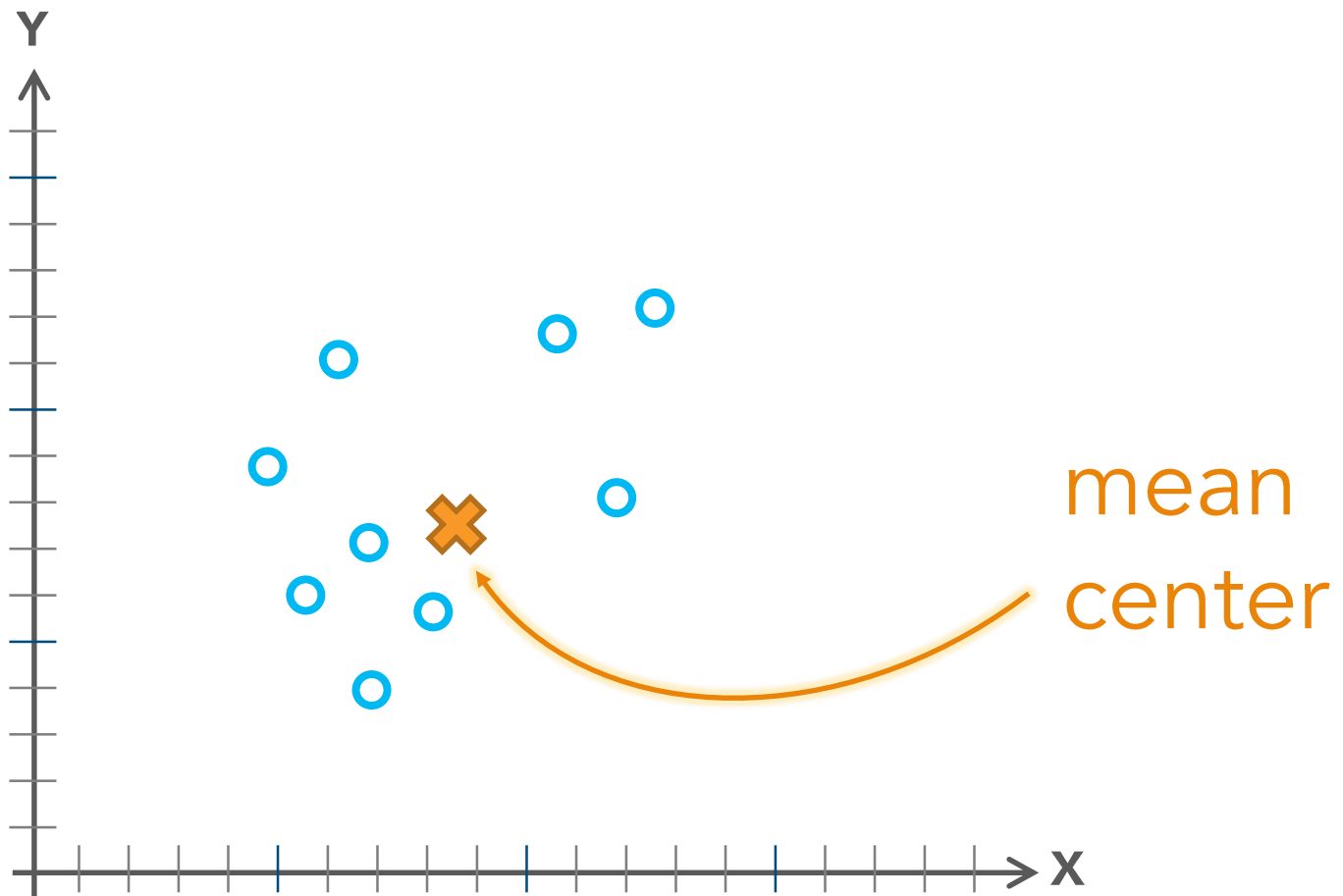
identifies the mean direction, length, and geographic center for a set of lines

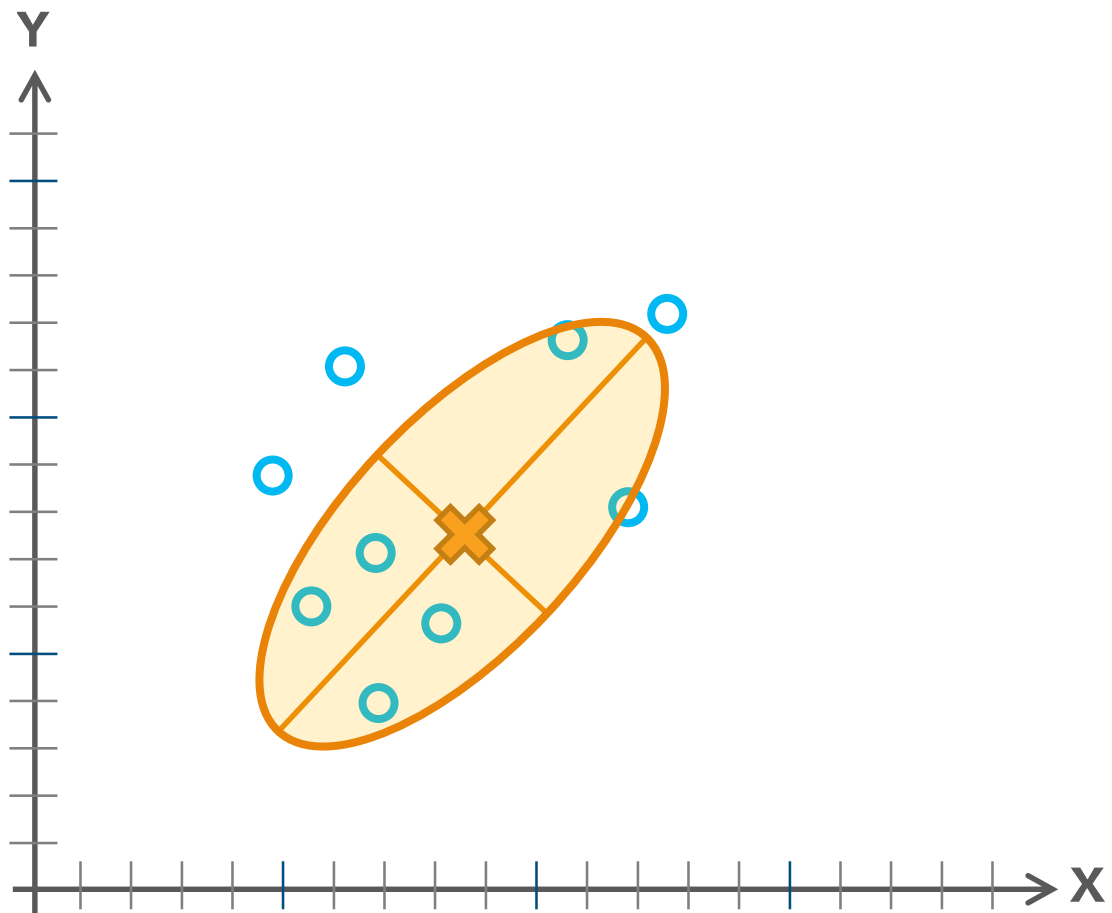




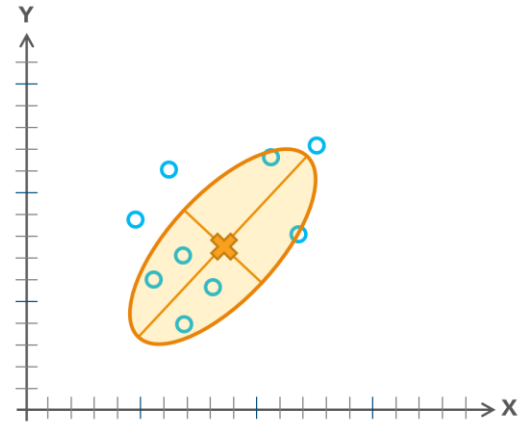
# Directional Distribution (Standard Deviational Ellipse)

creates standard deviational ellipses to summarize the spatial characteristics of geographic features: central tendency, dispersion, and directional trends





# Demo



# Similarity Search

identifies which candidate features are most similar or most dissimilar to one or more input features based on feature attributes





**potential  
store  
locations**

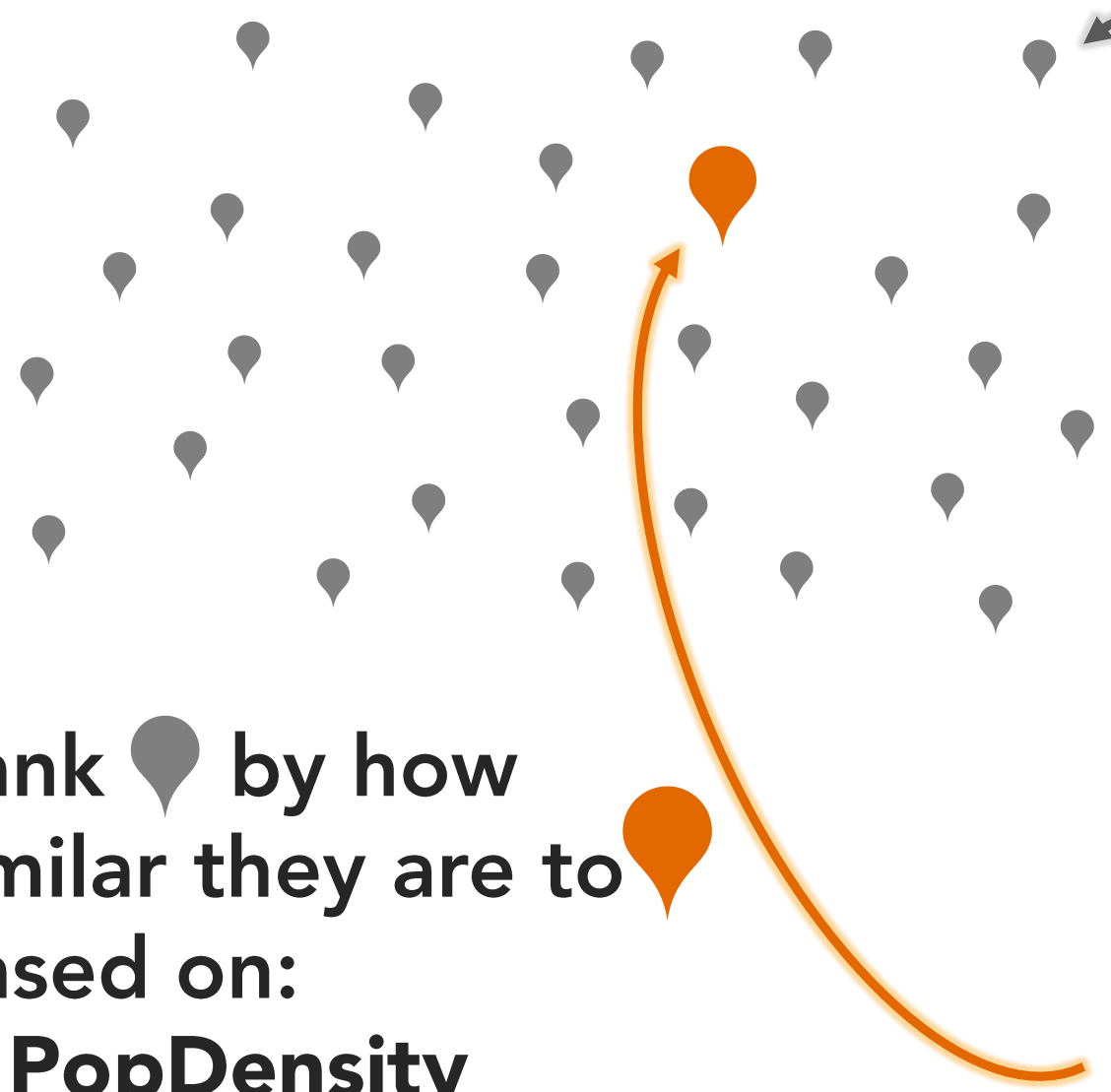


high  
performing  
store

potential  
store  
locations

Rank 📍 by how similar they are to 📍 based on:

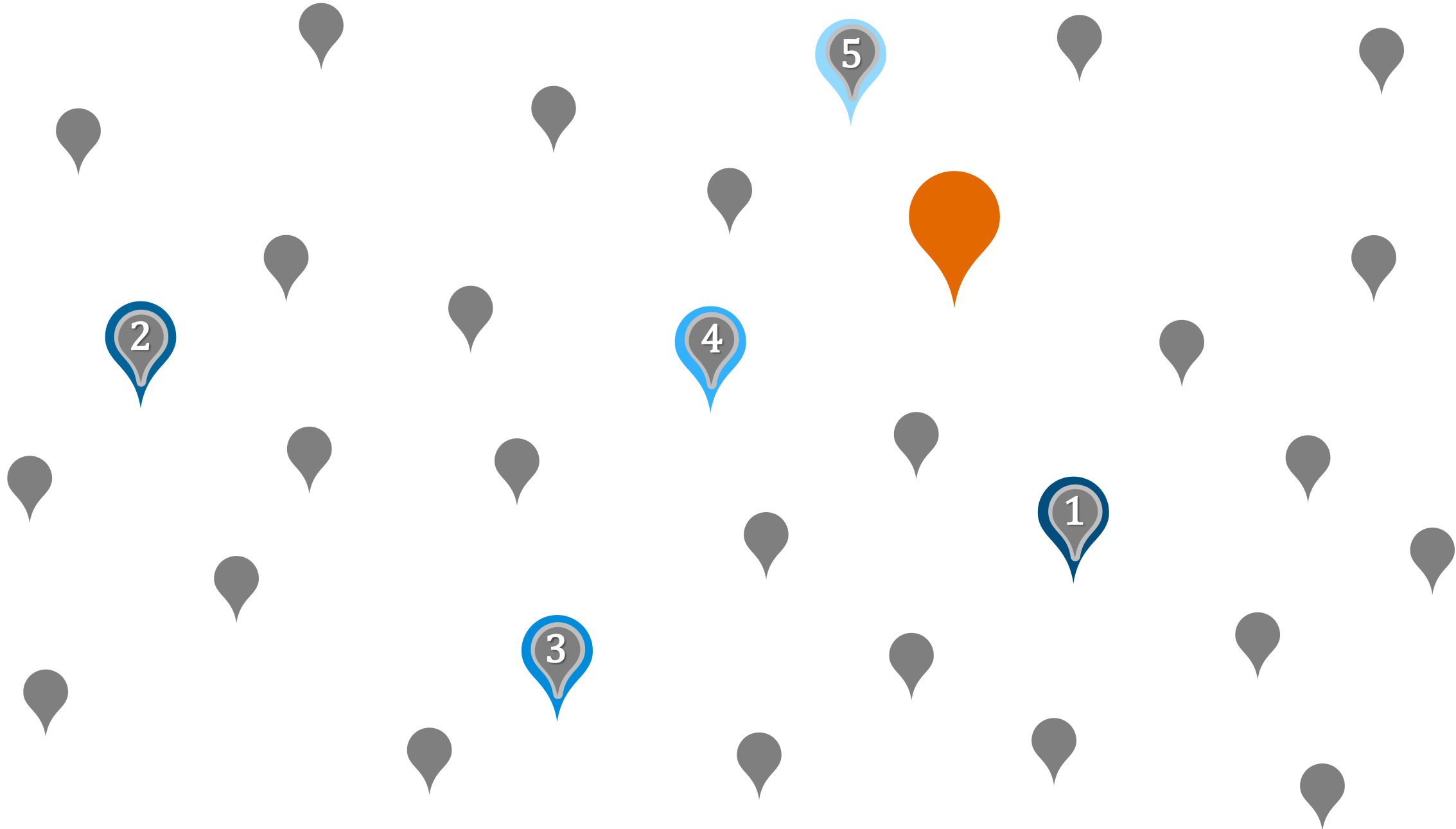
- **PopDensity**
- **AvIncome**
- **DistToCompetition**



LocID	PopDensity	AvIncome	DistToCompetition

LocID	PopDensity	AvIncome	DistToCompetition







standardize  
attributes

# Z-transform:

$$(x - \bar{x}) / SD$$

**standardize  
attributes**

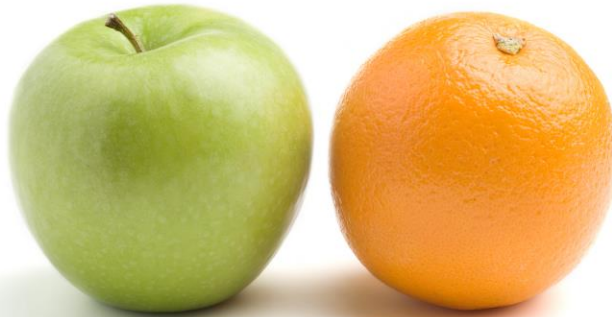


Population = 14,159

% Uninsured = .26

Distance (km) = 535.89

**standardize  
attributes**



Population =  $-.7932$

% Uninsured =  $3.8462$

Distance (km) =  $.6433$



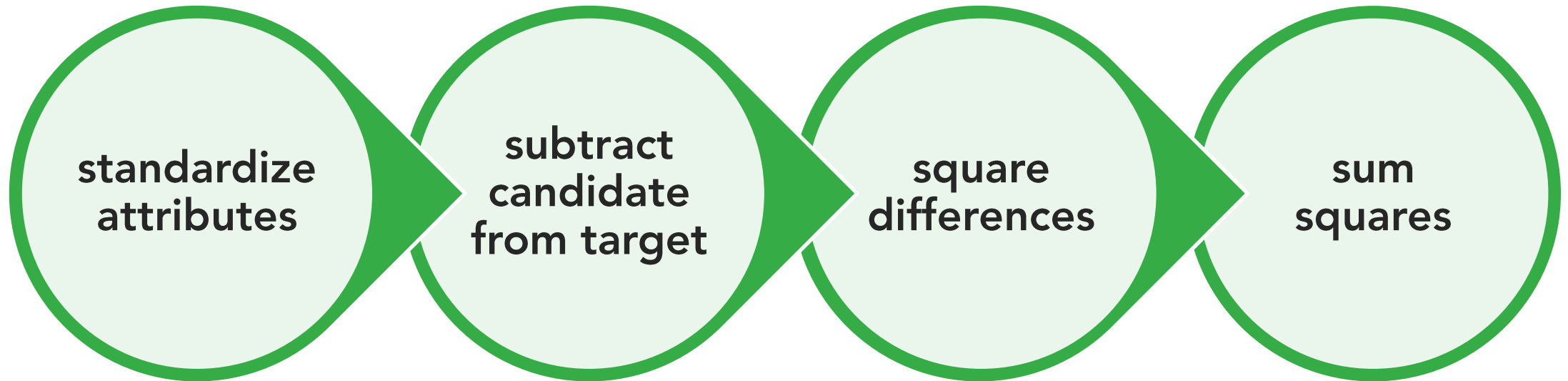
**standardize  
attributes**



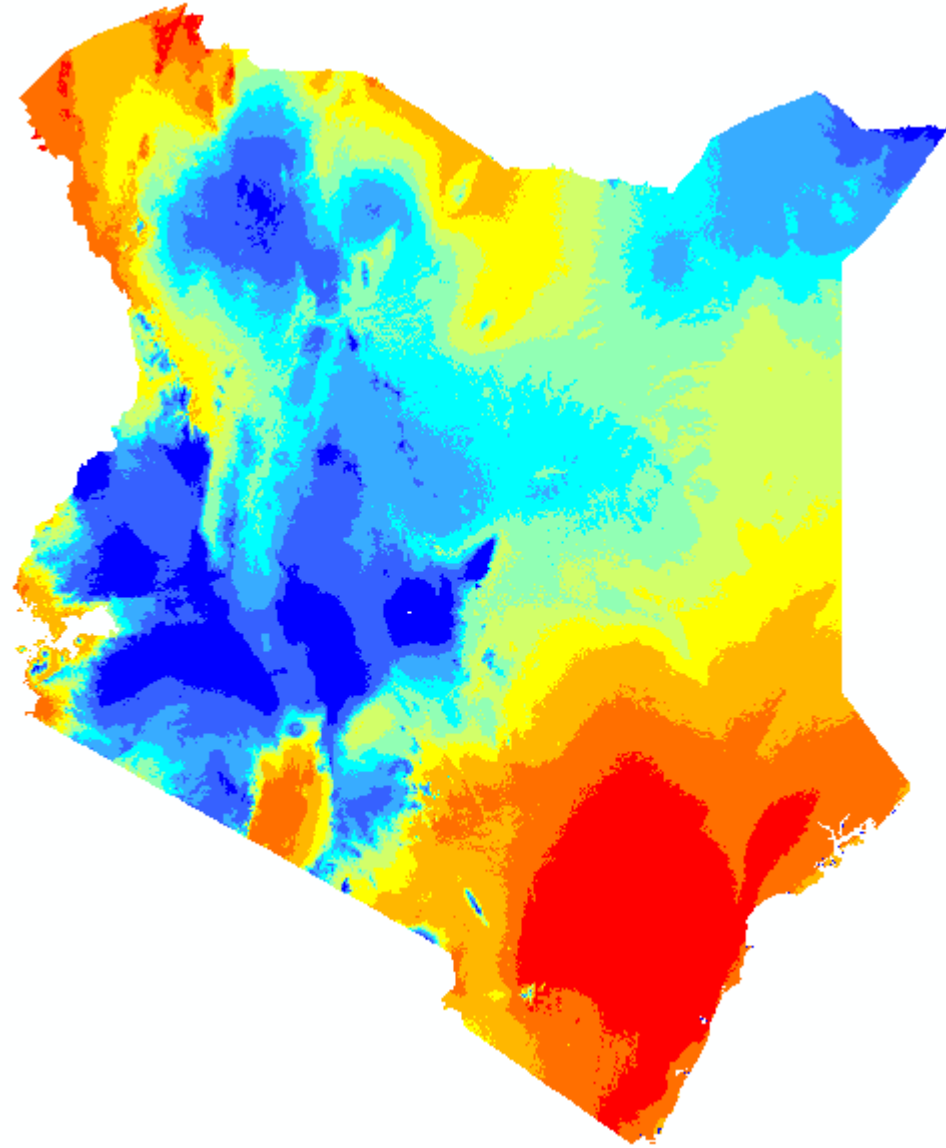
Population =  $-.7932$

% Uninsured =  $3.8462$

Distance (km) =  $.6433$



# Dengue Fever Risk in Kenya



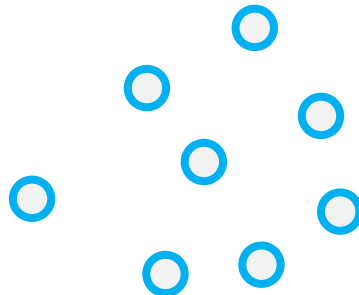
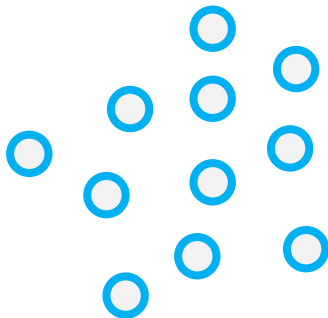
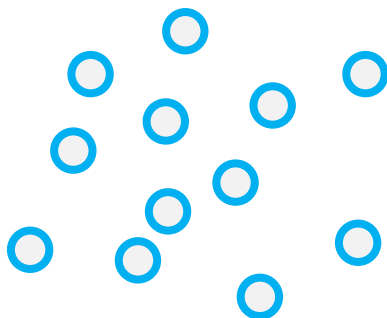
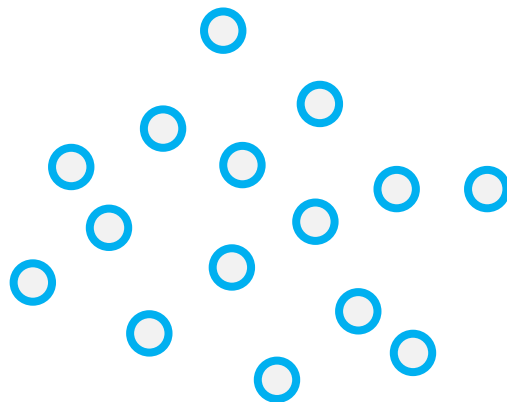
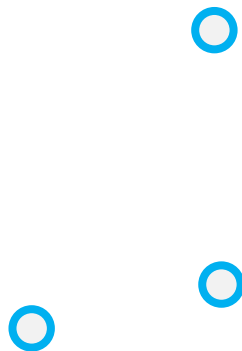
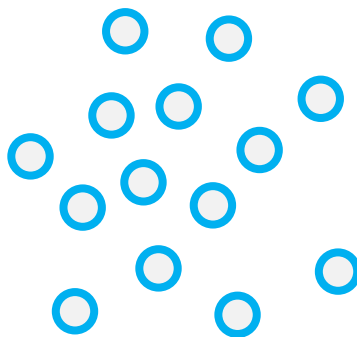


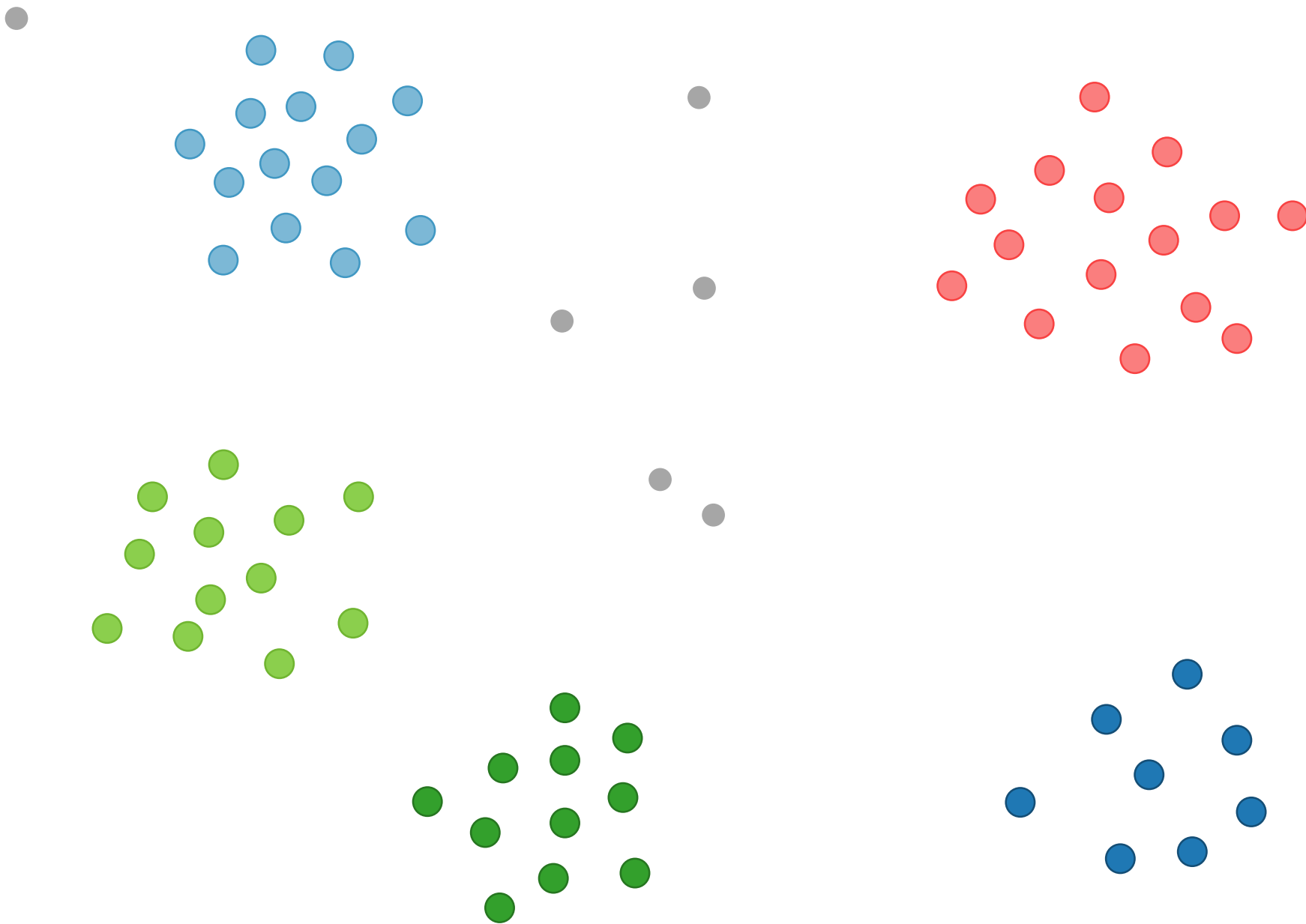
# Machine Learning

clustering methods

# Density-based Clustering

finds clusters based on feature locations





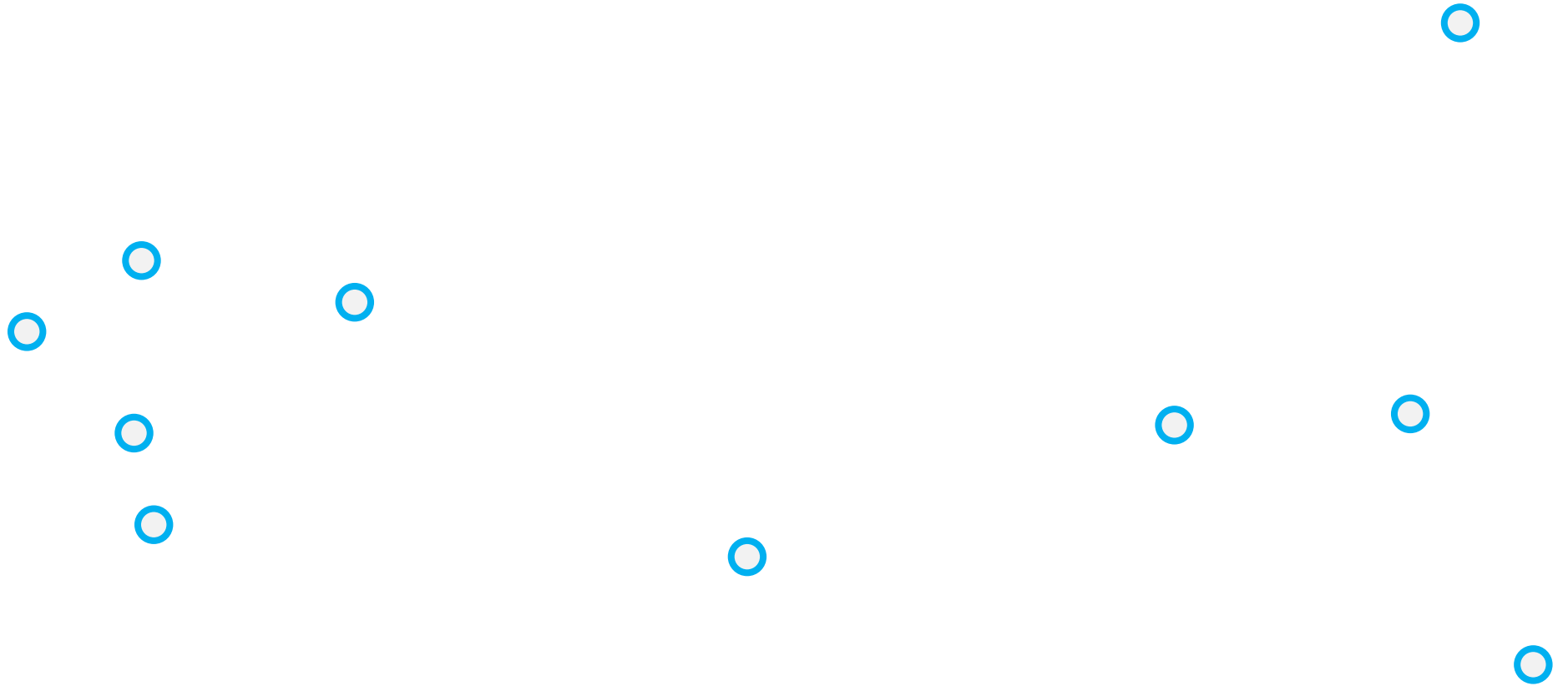
**DBSCAN** – defined distance

**HDBSCAN** – self adjusting

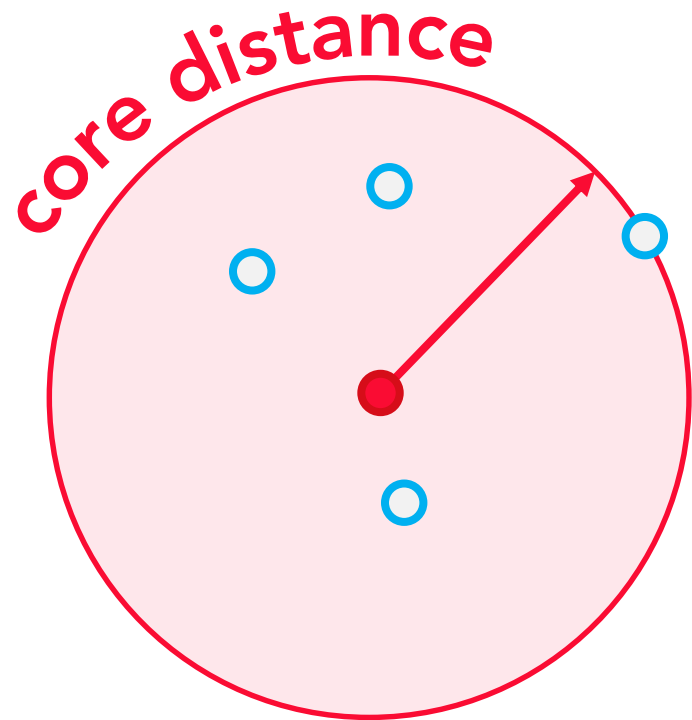
**OPTICS** – multi-scale



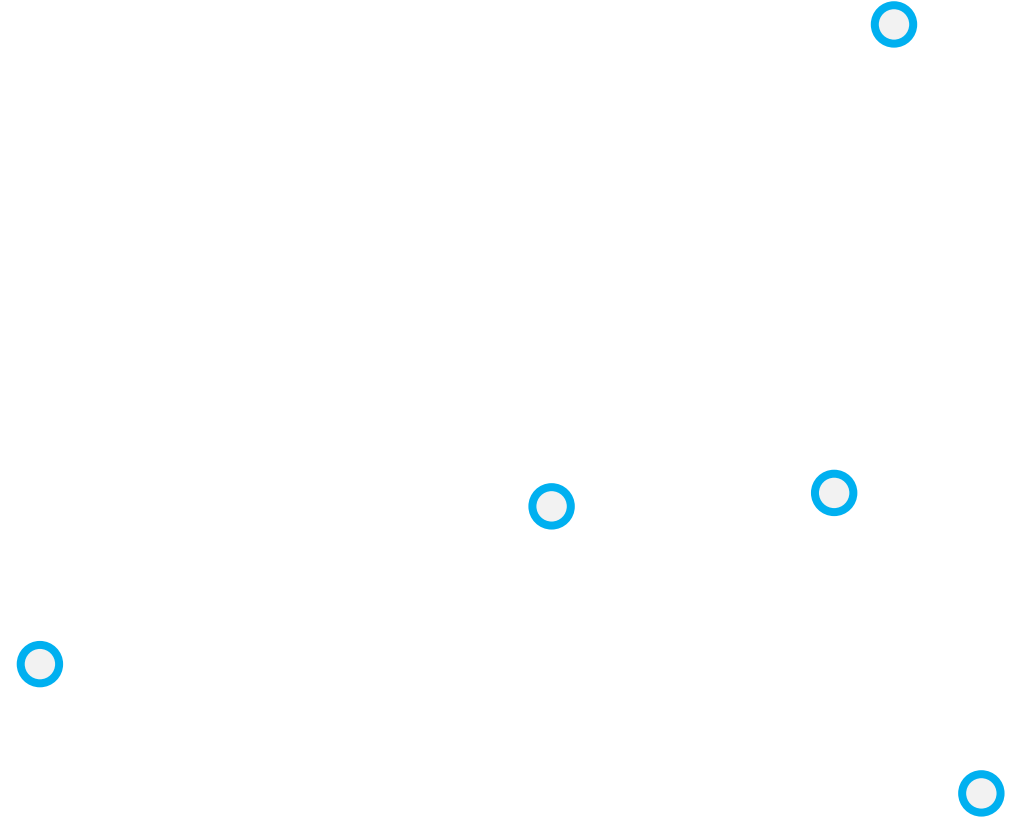
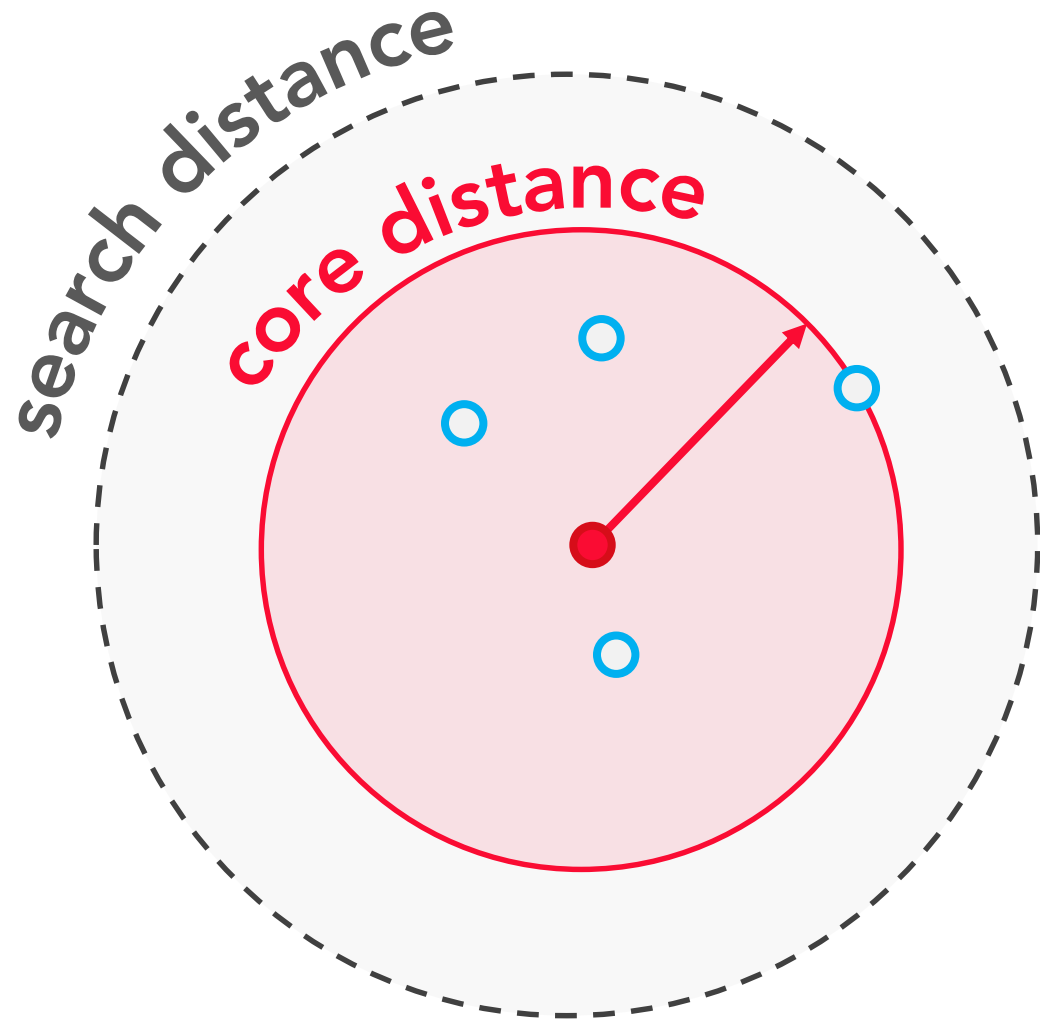
# DBSCAN – defined distance



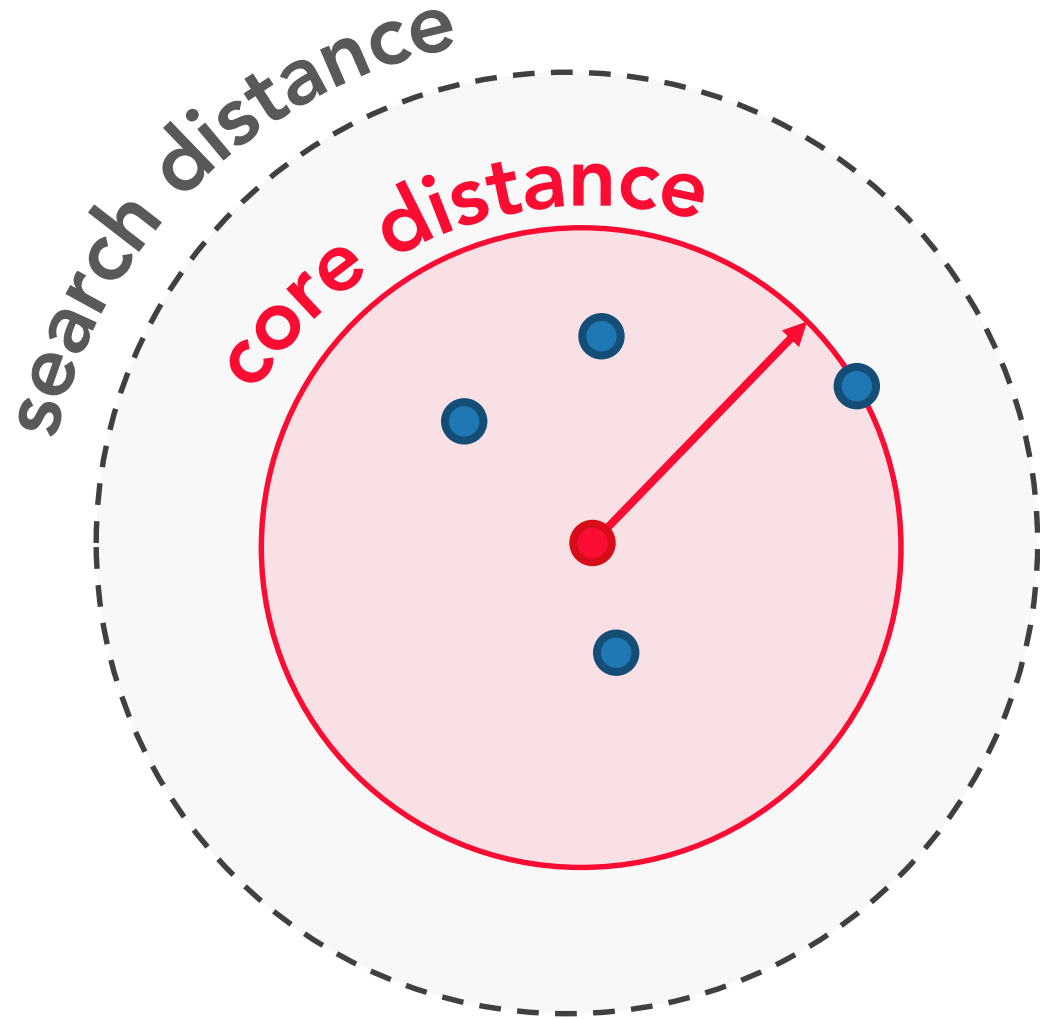
# DBSCAN – defined distance



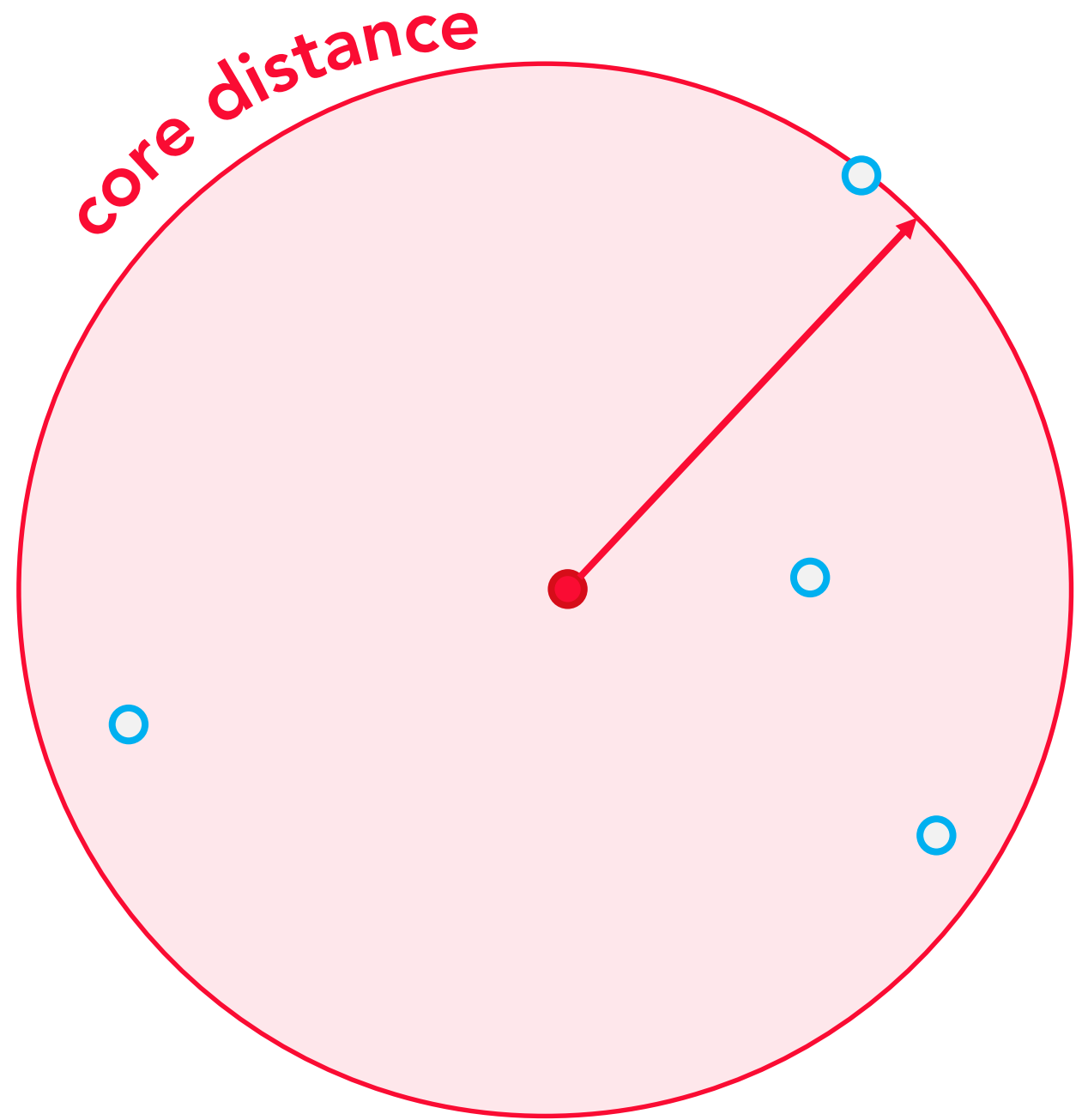
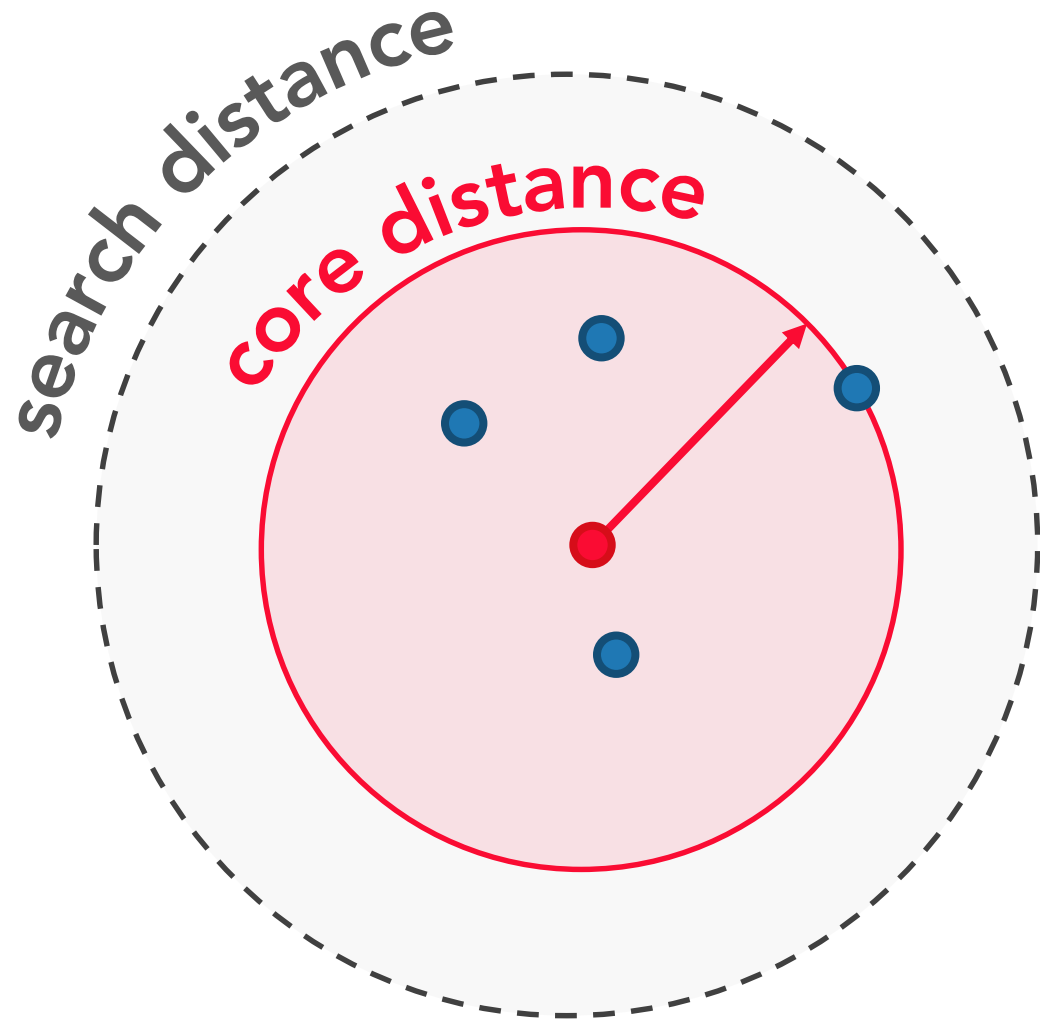
# DBSCAN – defined distance



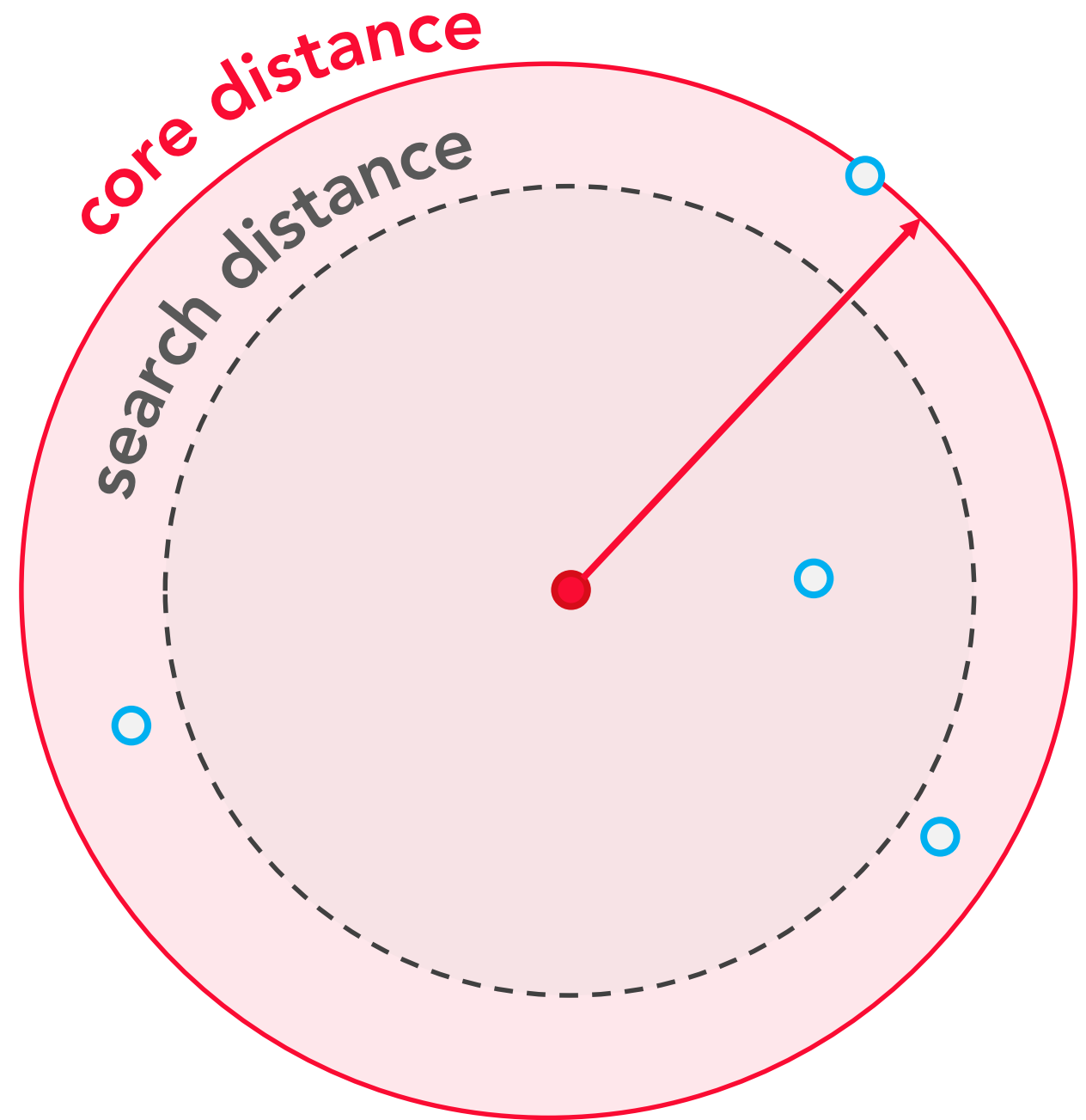
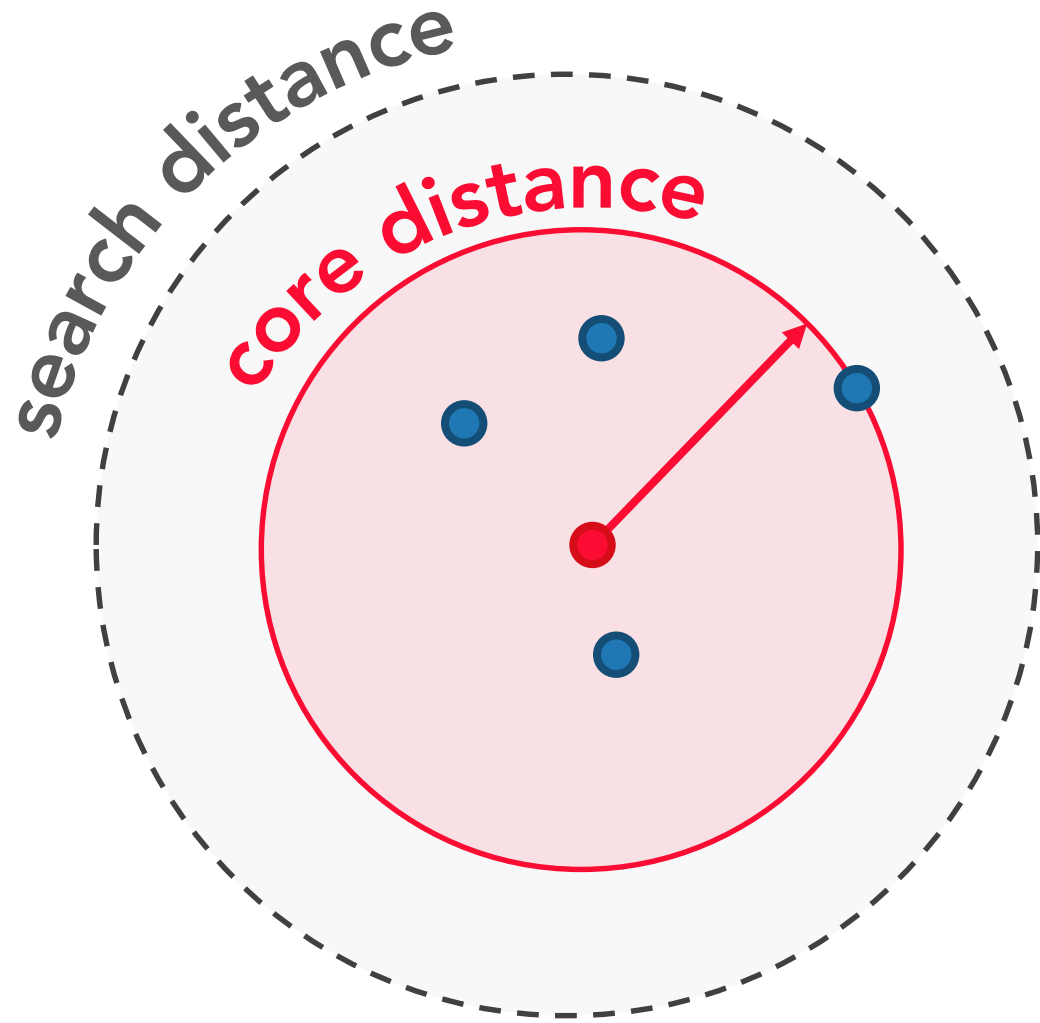
# DBSCAN – defined distance



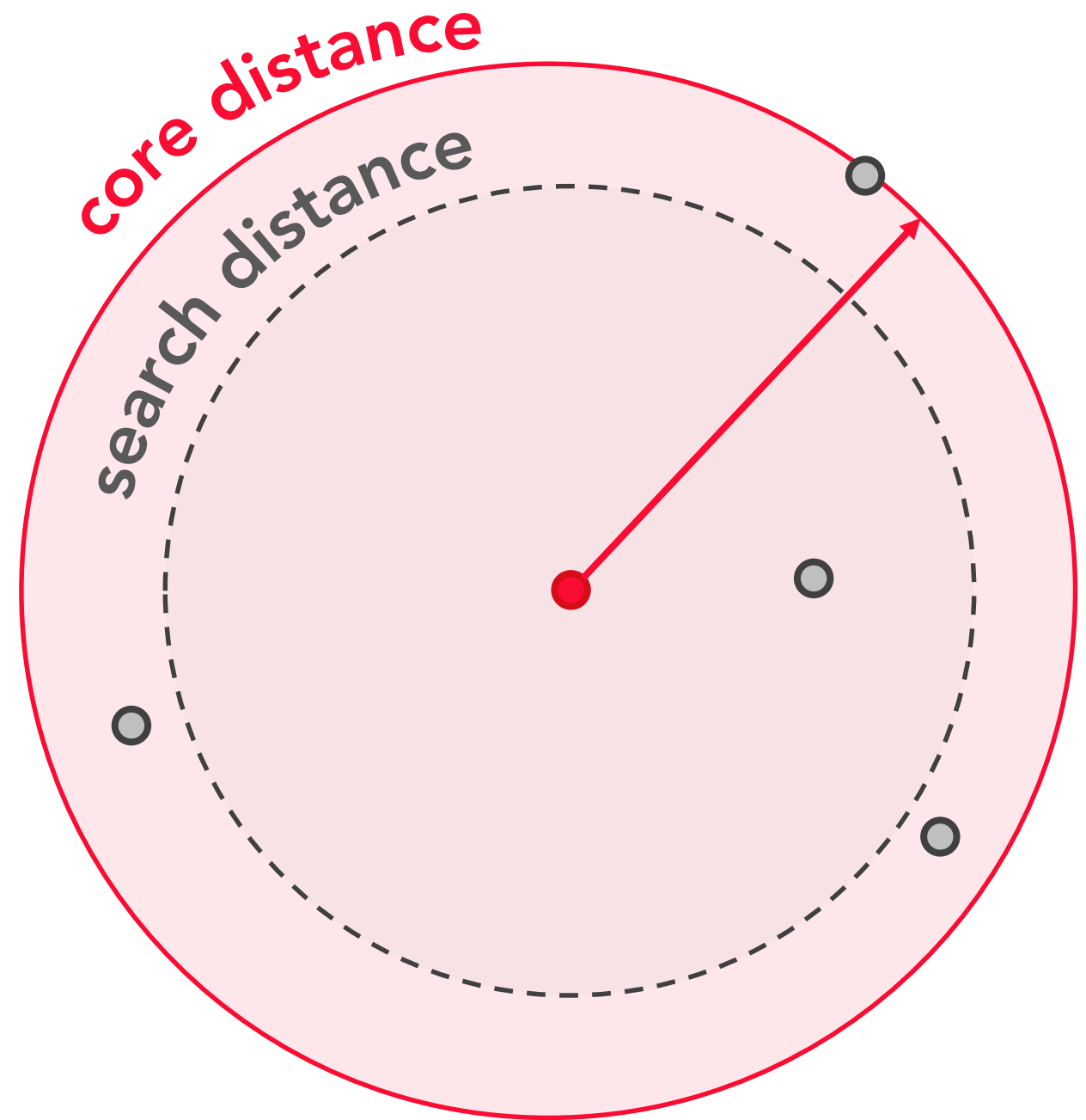
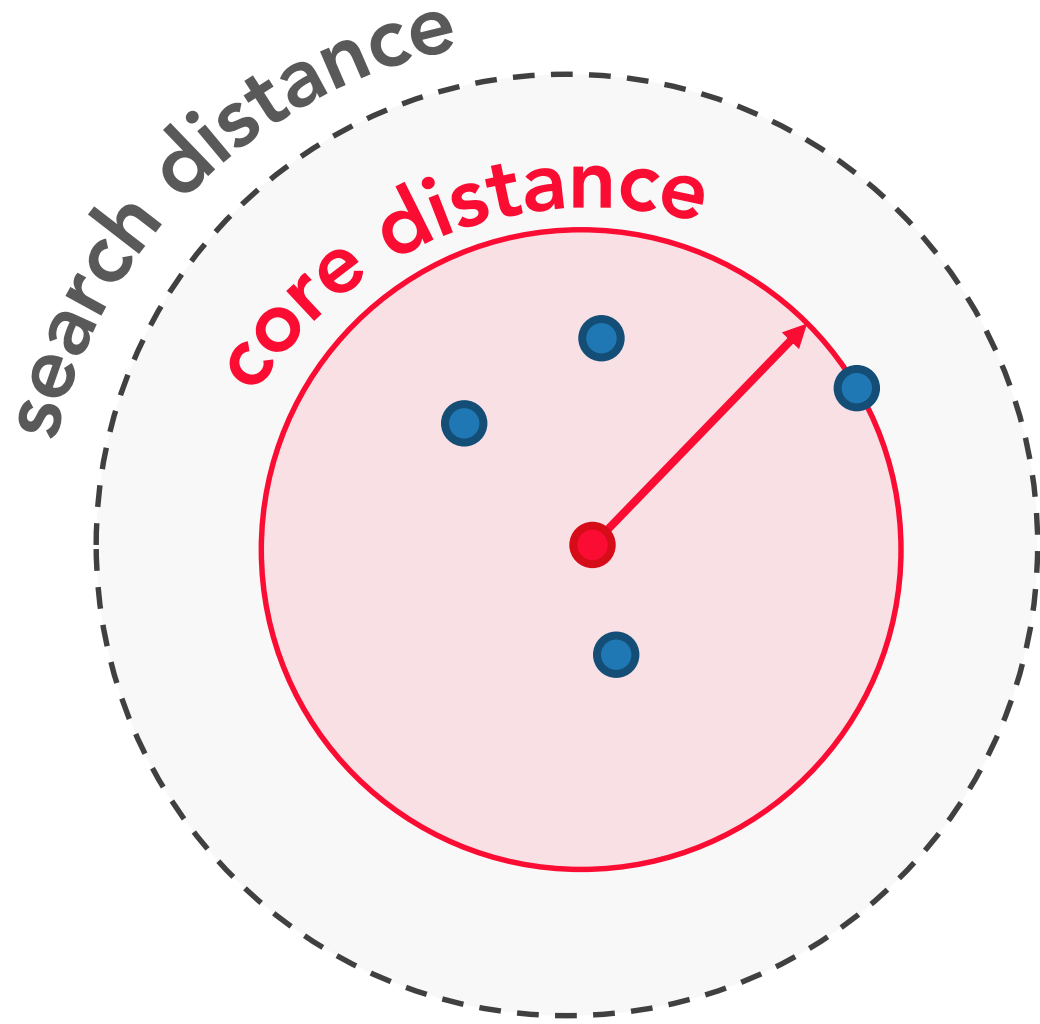
# DBSCAN – defined distance



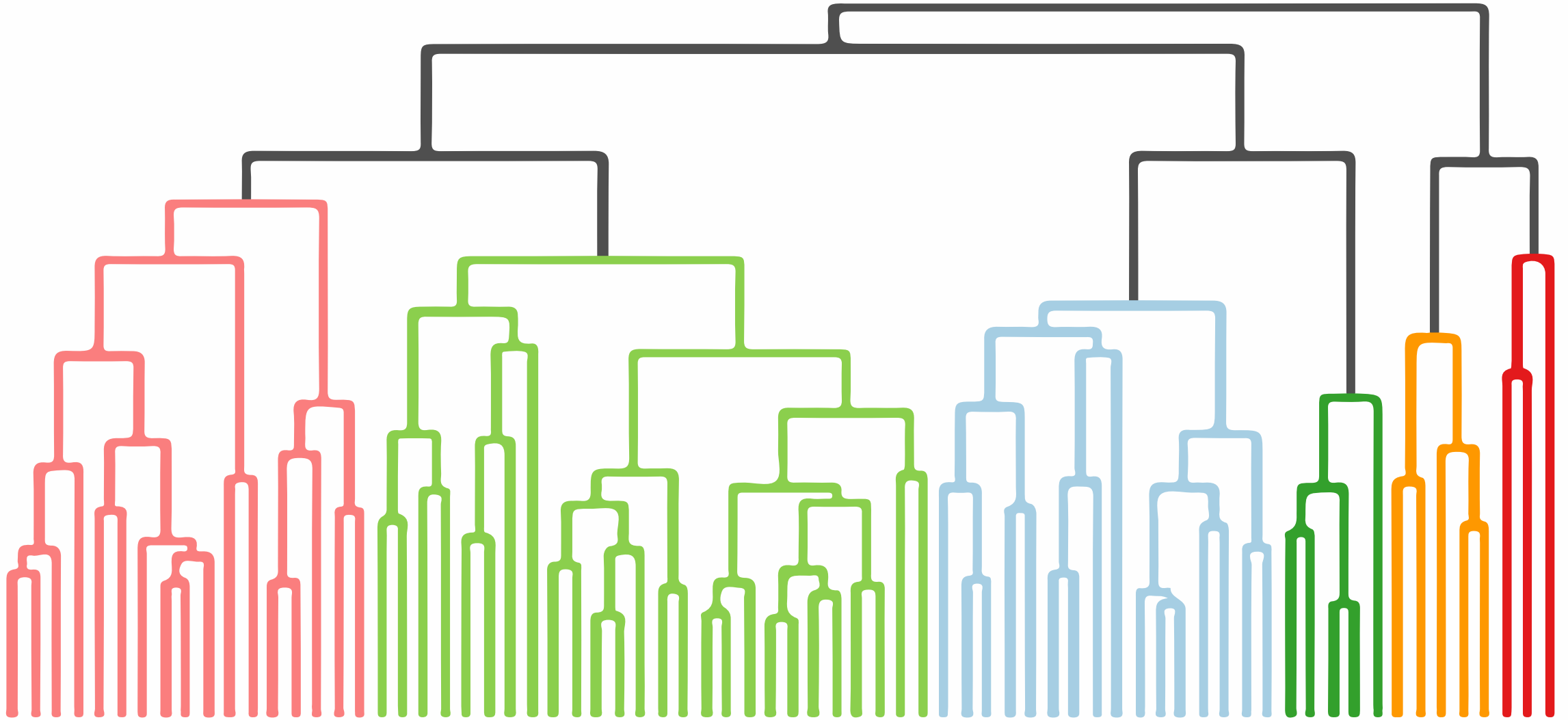
# DBSCAN – defined distance



# DBSCAN – defined distance

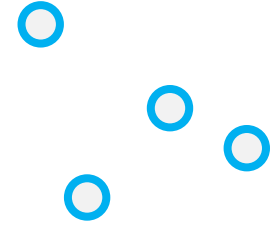
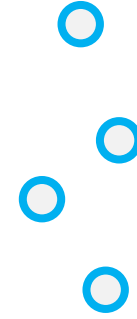
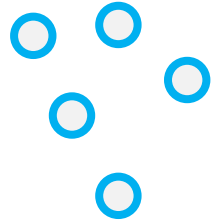
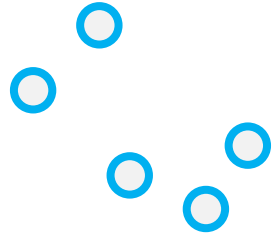


# HDBSCAN – self adjusting

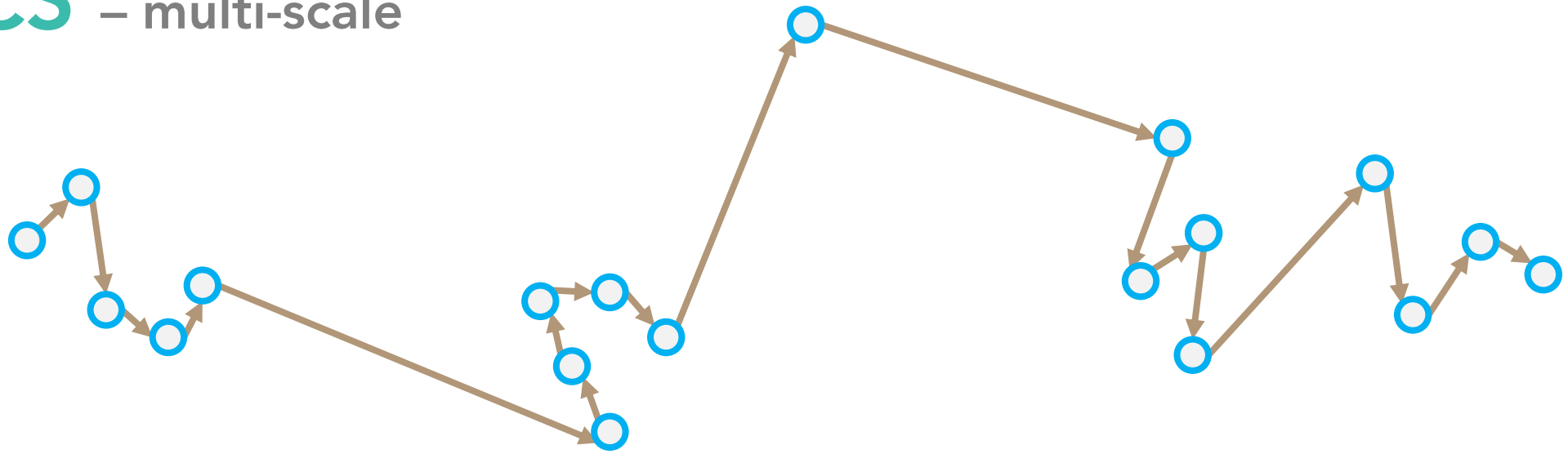




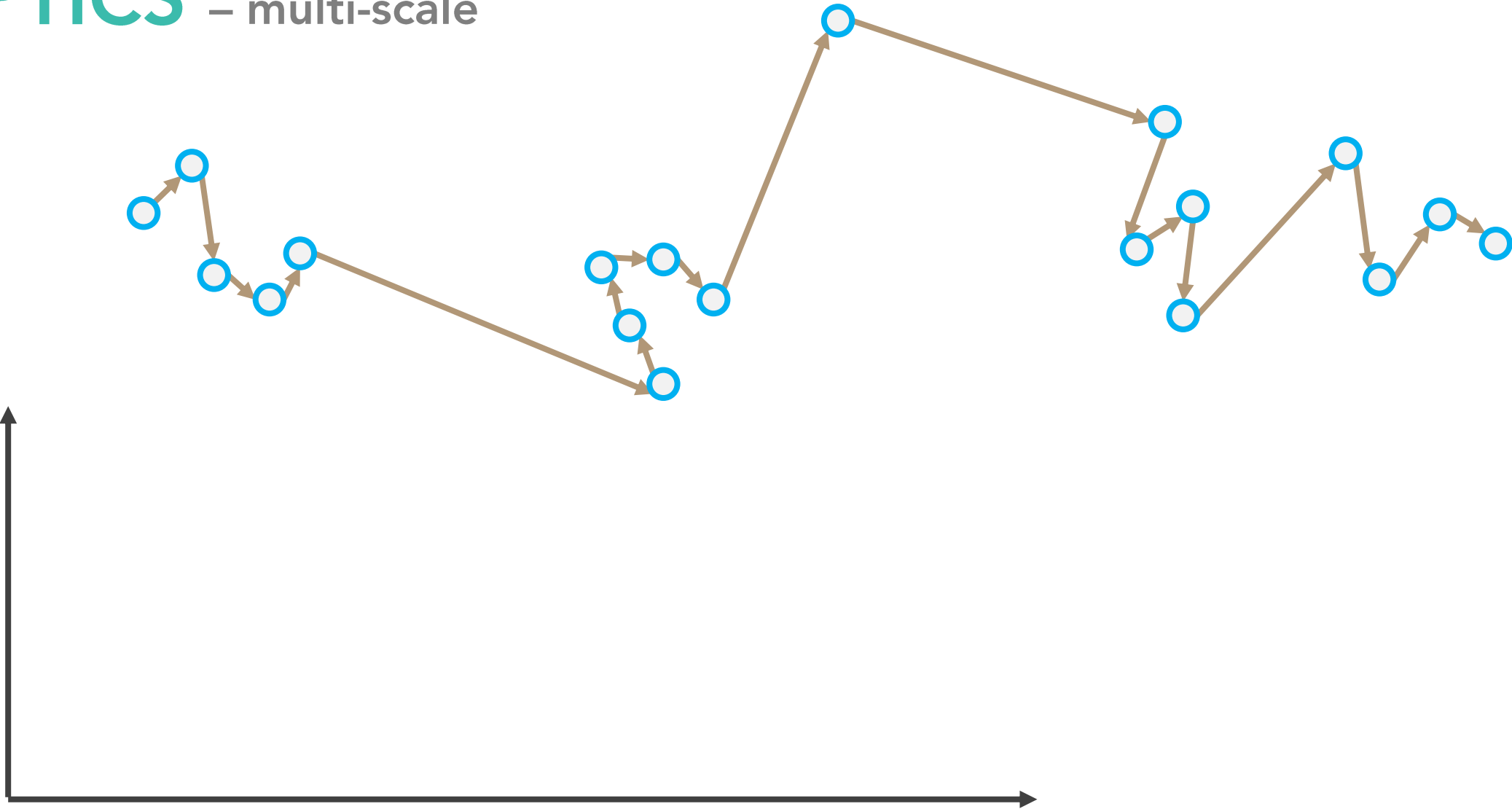
# OPTICS – multi-scale



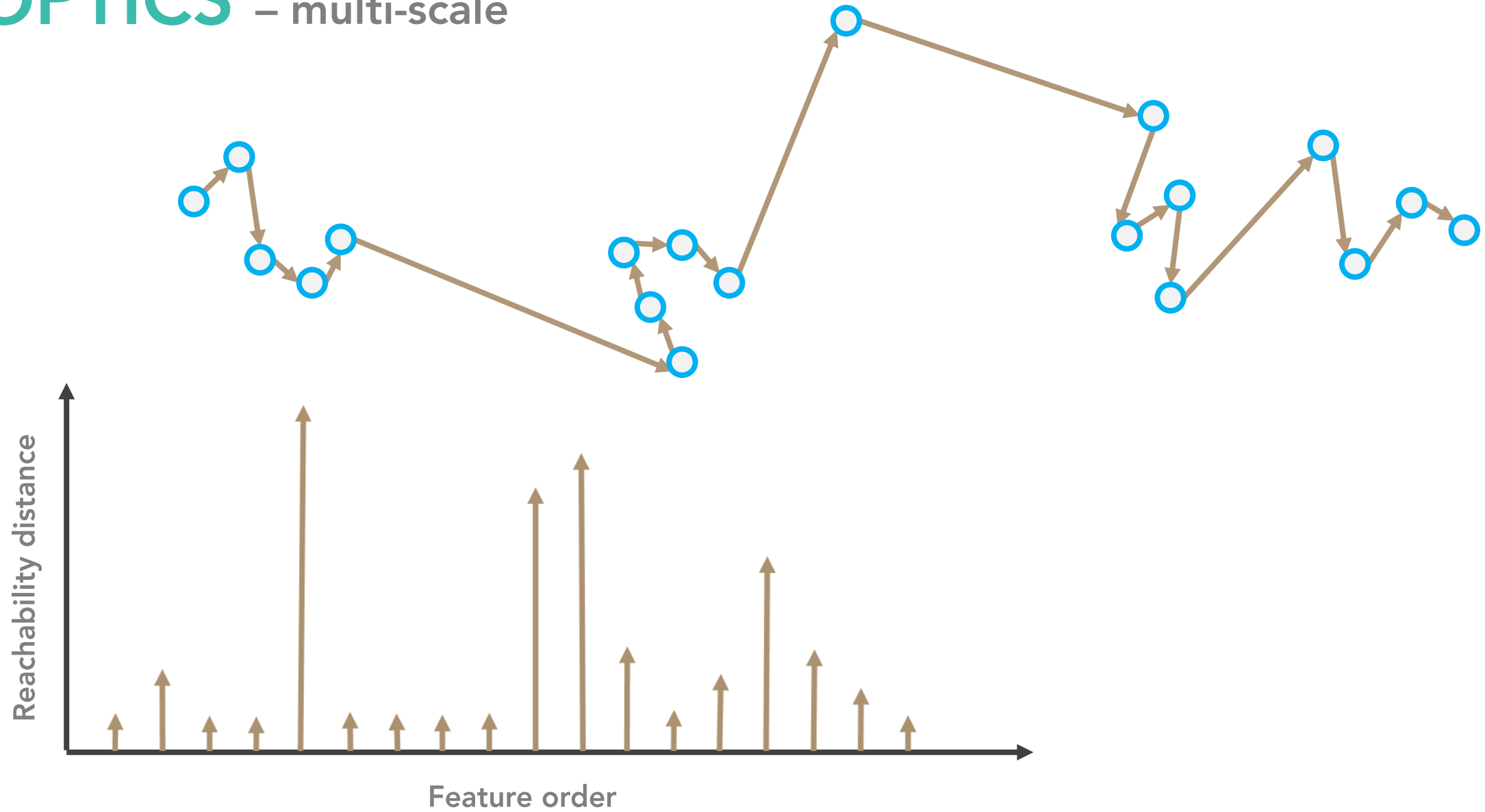
# OPTICS – multi-scale



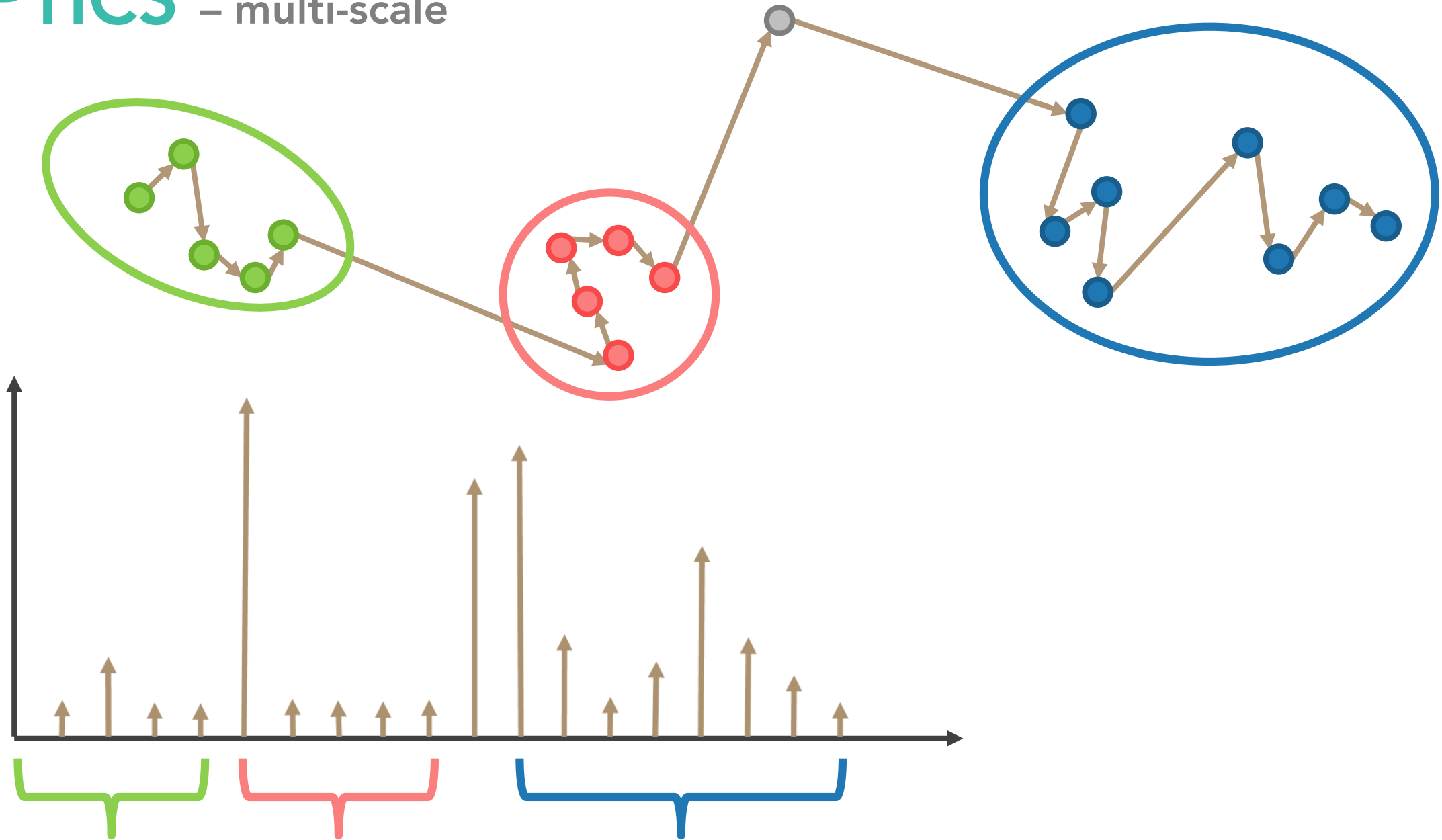
# OPTICS – multi-scale



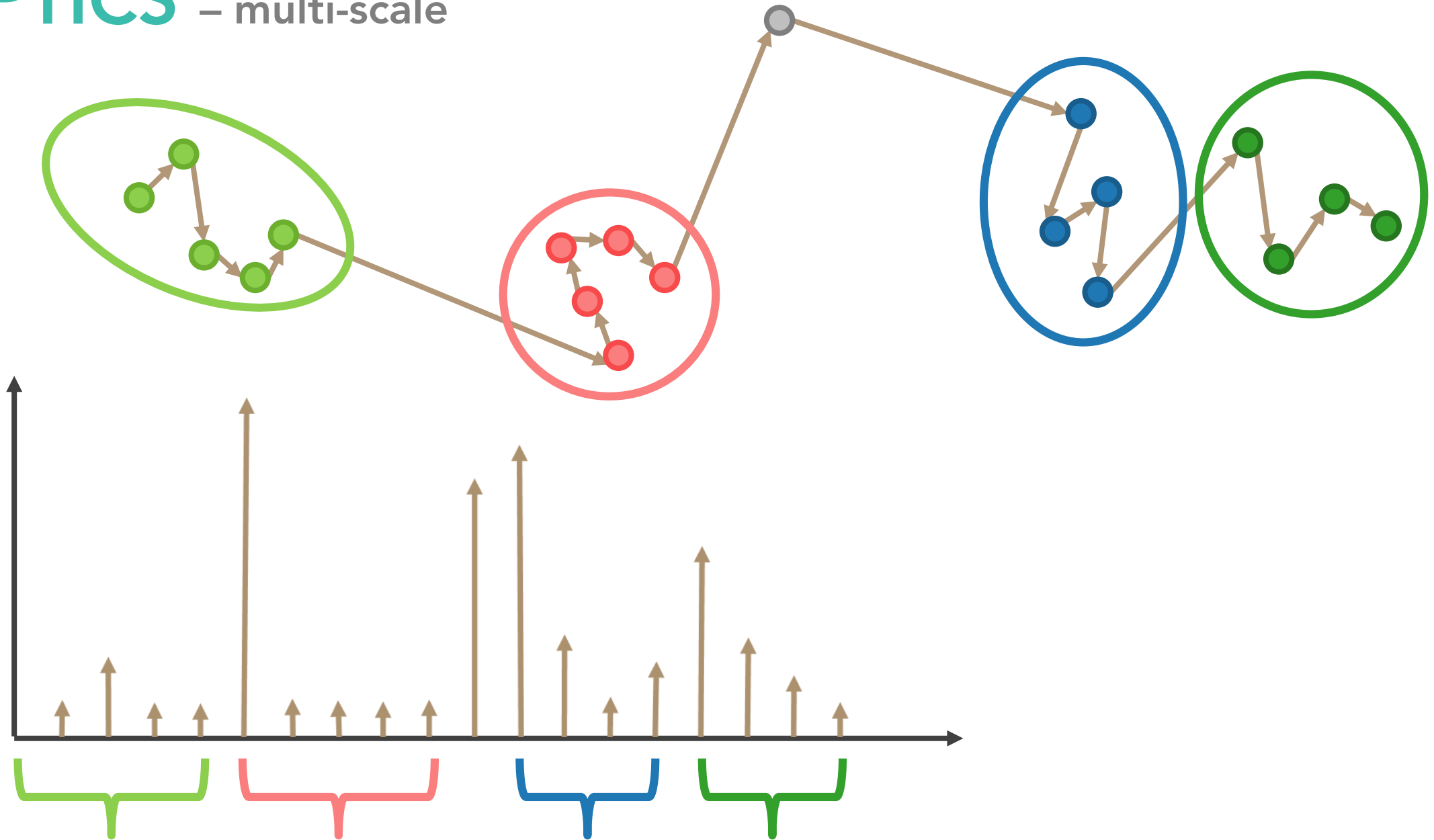
# OPTICS – multi-scale



# OPTICS – multi-scale



# OPTICS – multi-scale



## DBSCAN

- Uses fixed search distance
- Clusters of similar densities
- Fast

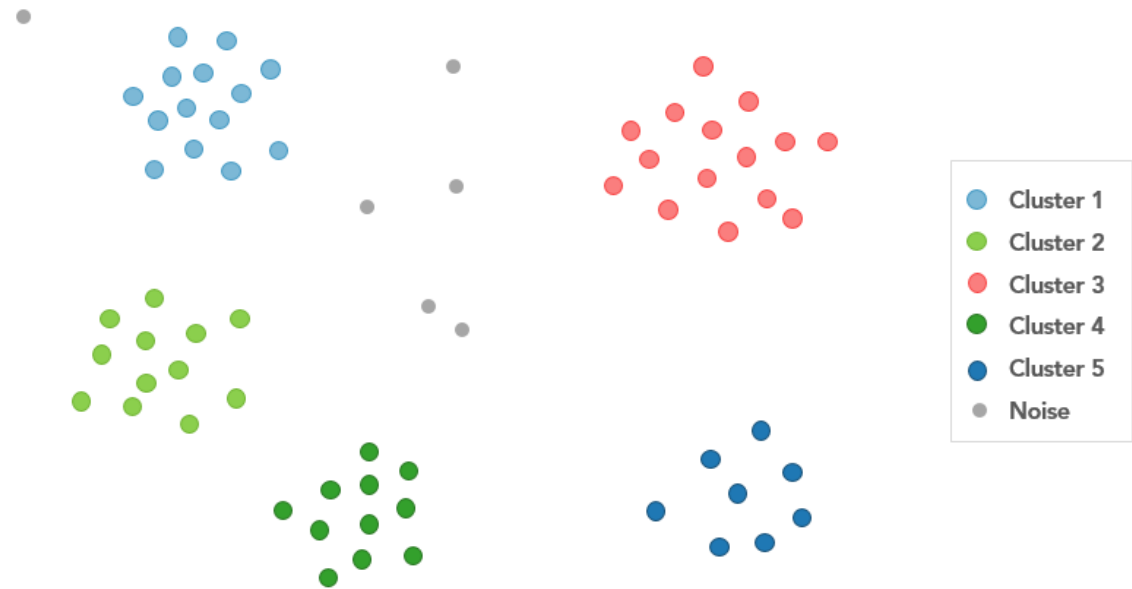
## HDBSCAN

- Uses range of search distances to find clusters of varying densities
- Data driven, requires least user input

## OPTICS

- Uses neighbor distances to create reachability plot
- Most flexibility for fine tuning
- Can be computationally intensive

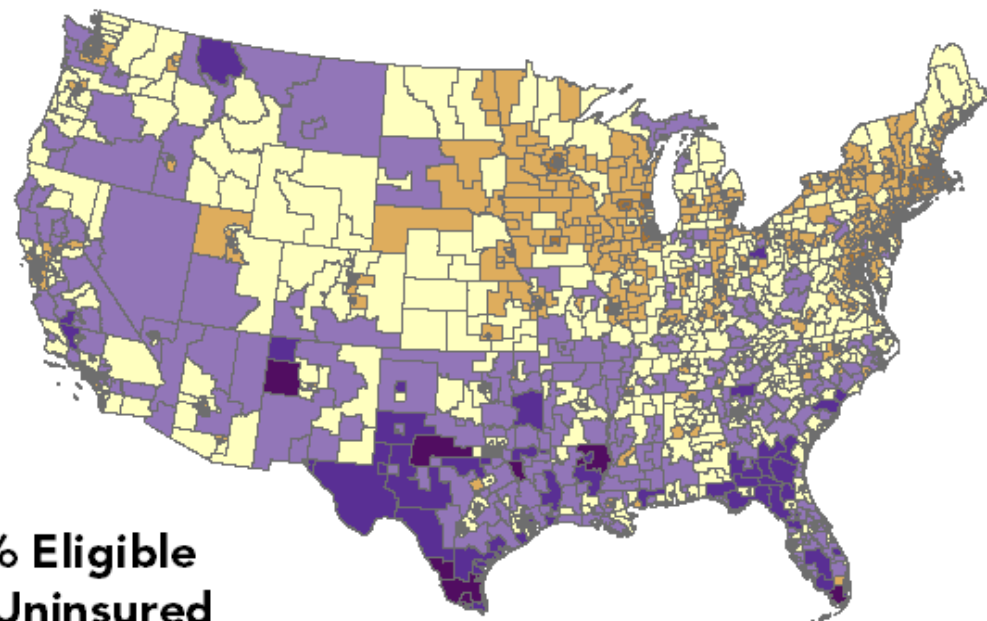
# Demo



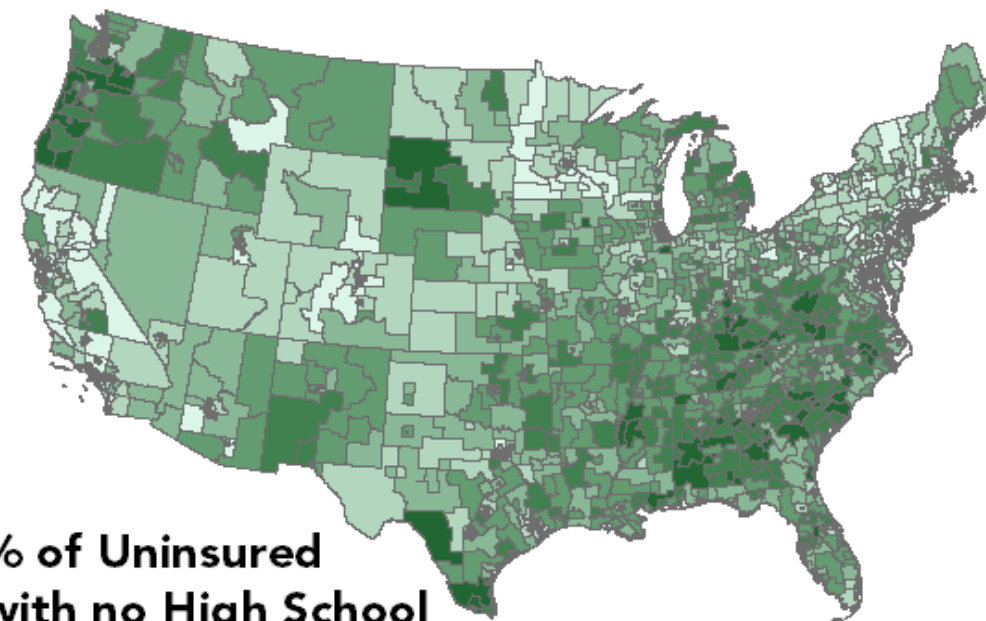


# Multivariate Clustering

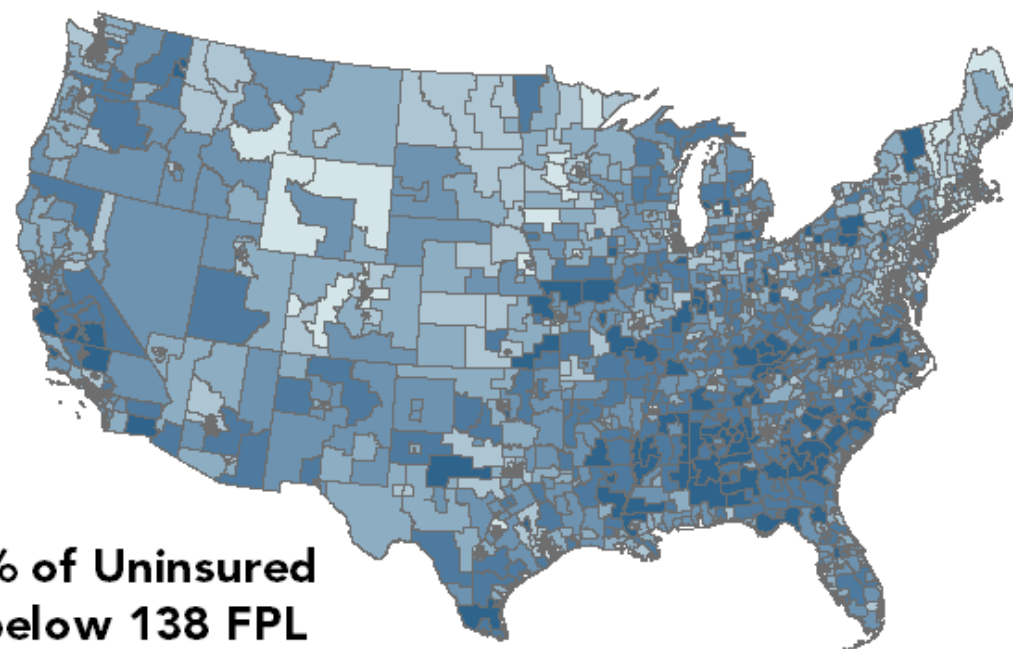
finds clusters based on feature attributes



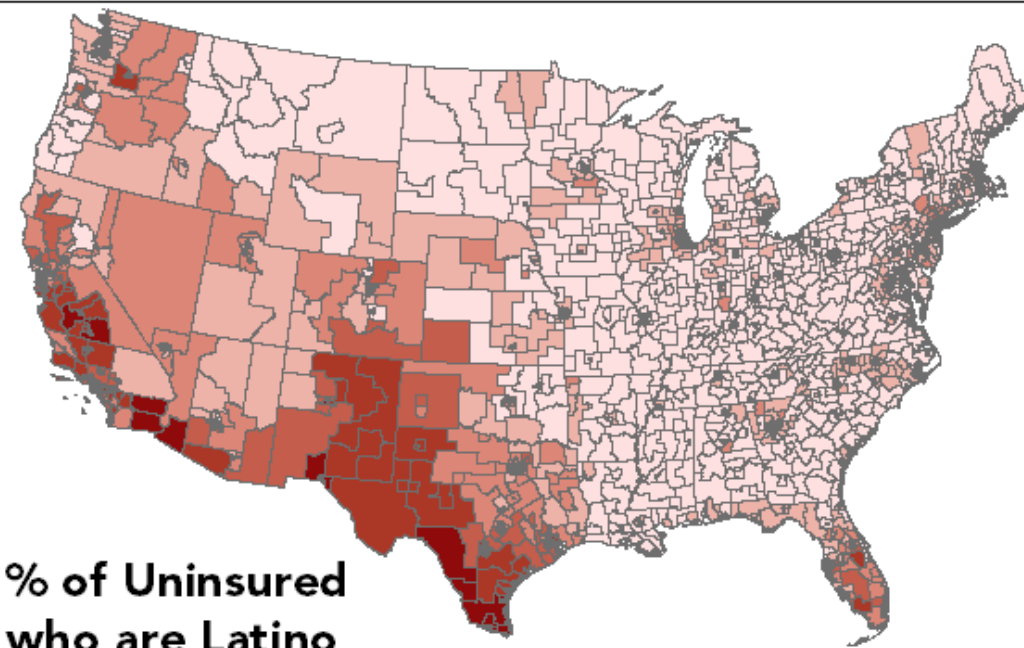
**% Eligible  
Uninsured**



**% of Uninsured  
with no High School**

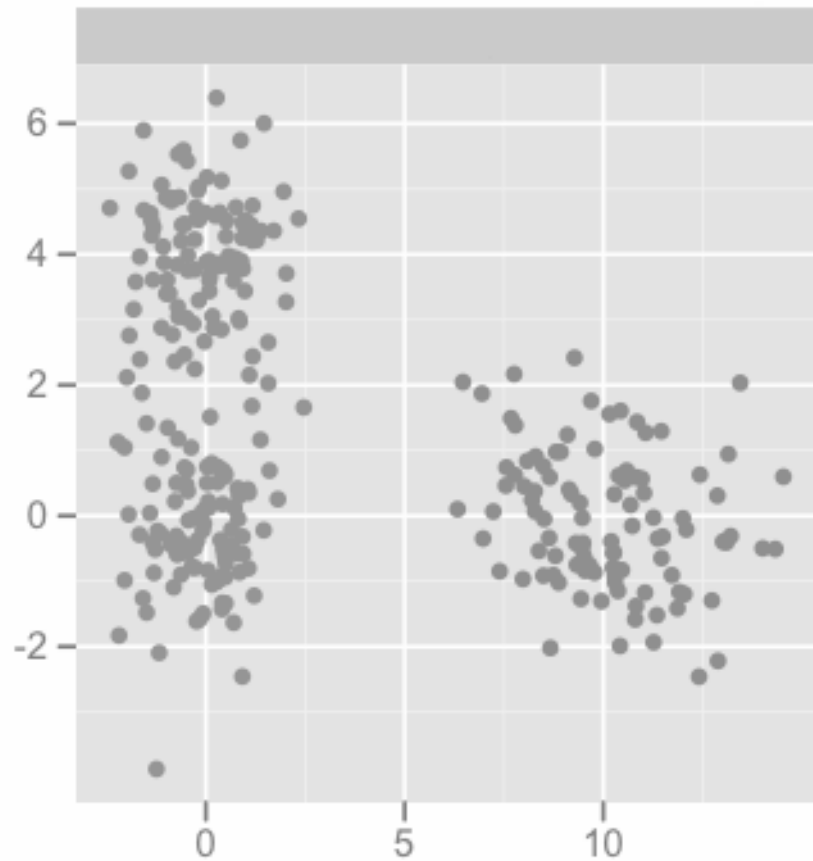


**% of Uninsured  
below 138 FPL**



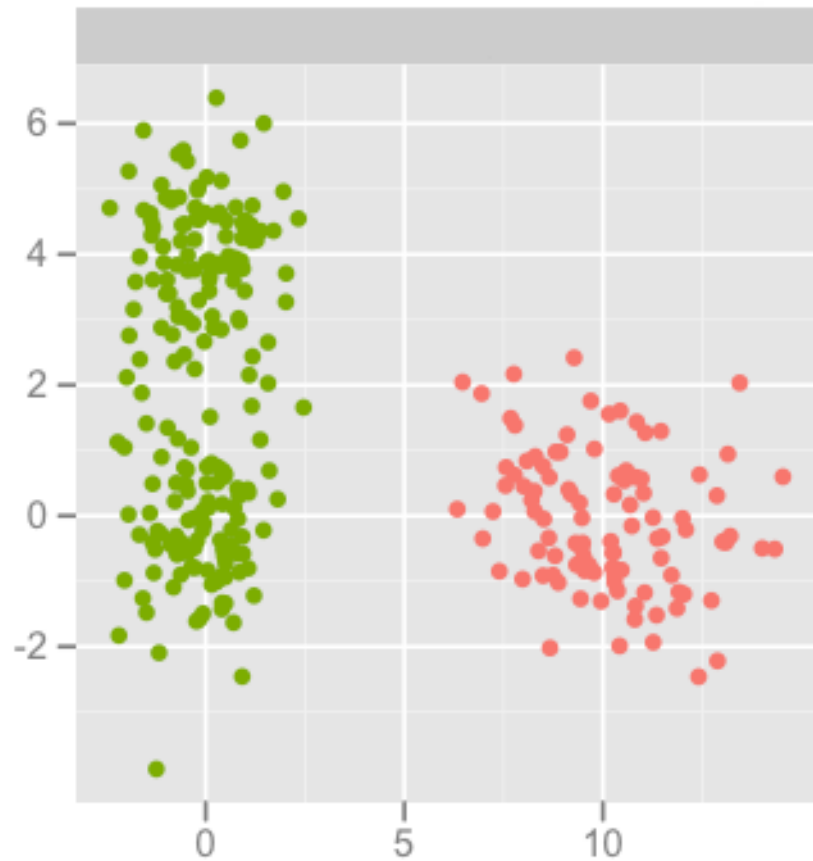
**% of Uninsured  
who are Latino**

# K Means



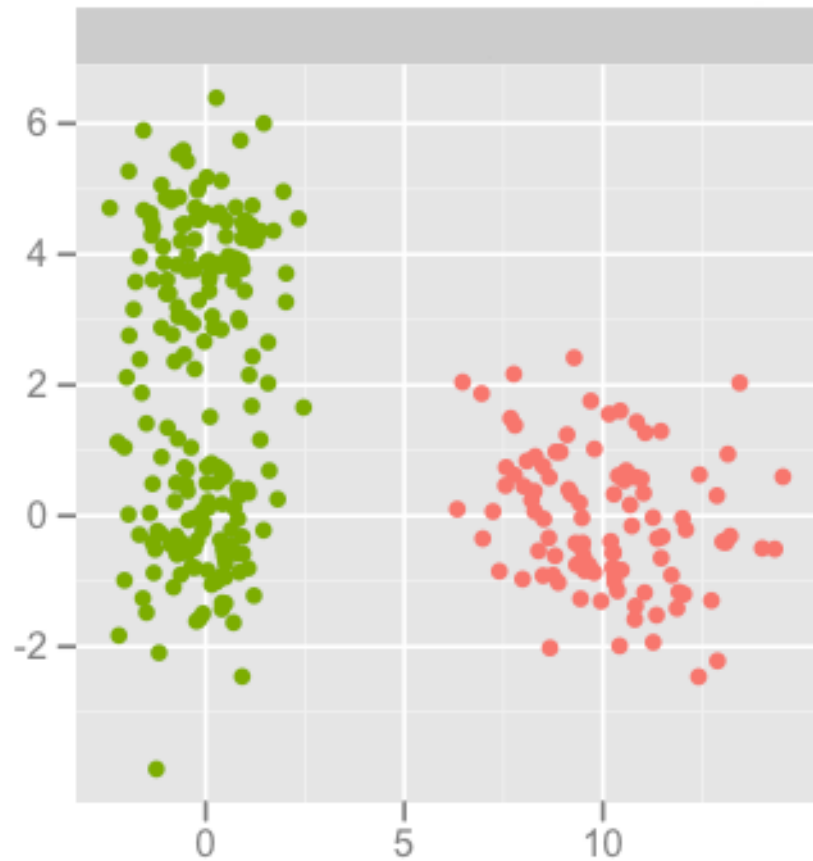
# K Means

2 groups

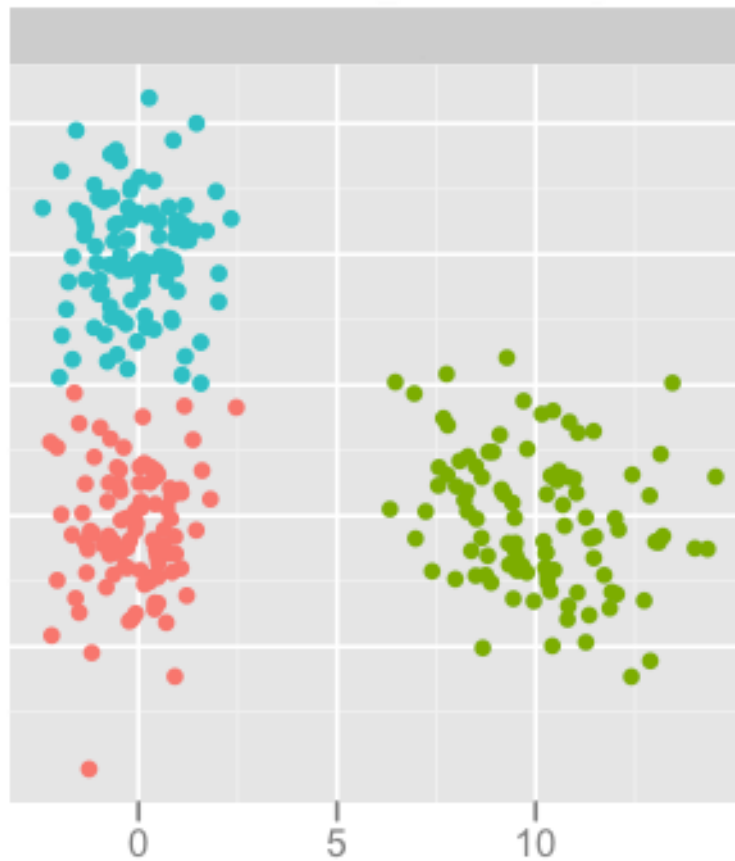


# K Means

2 groups

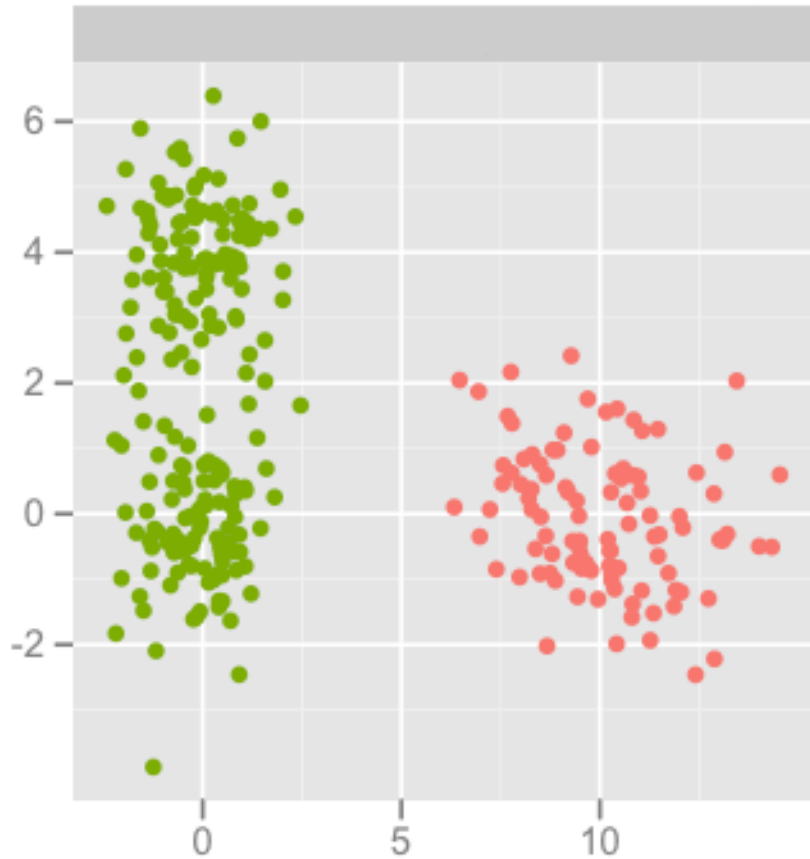


3 groups

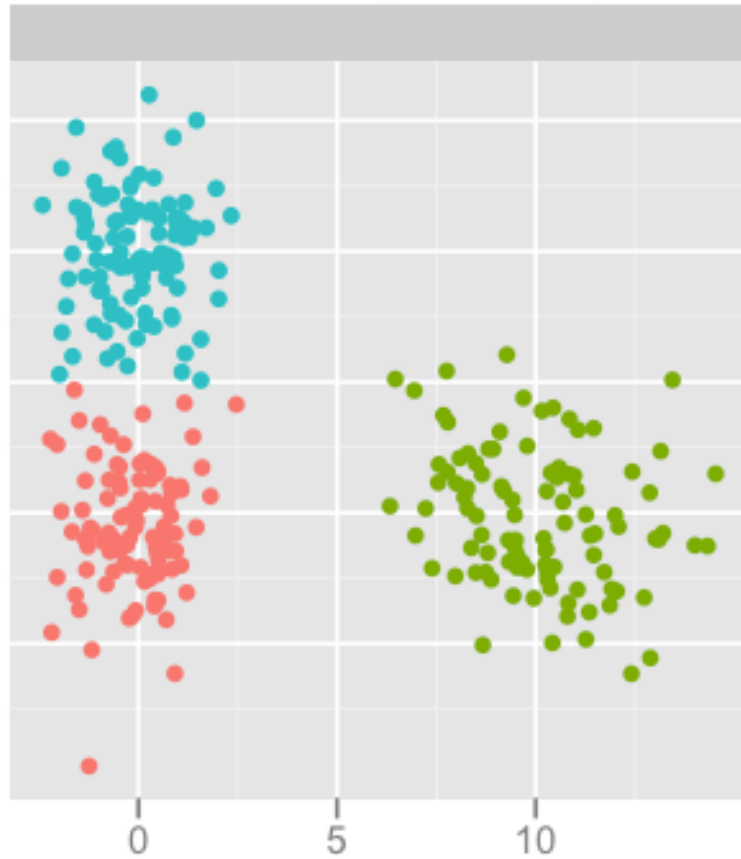


# K Means

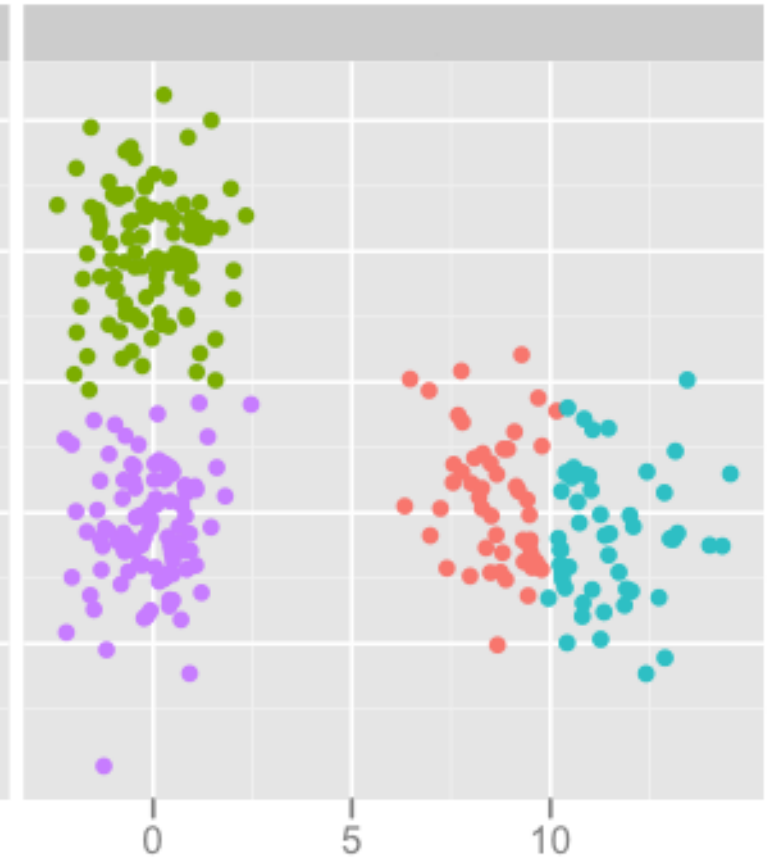
2 groups



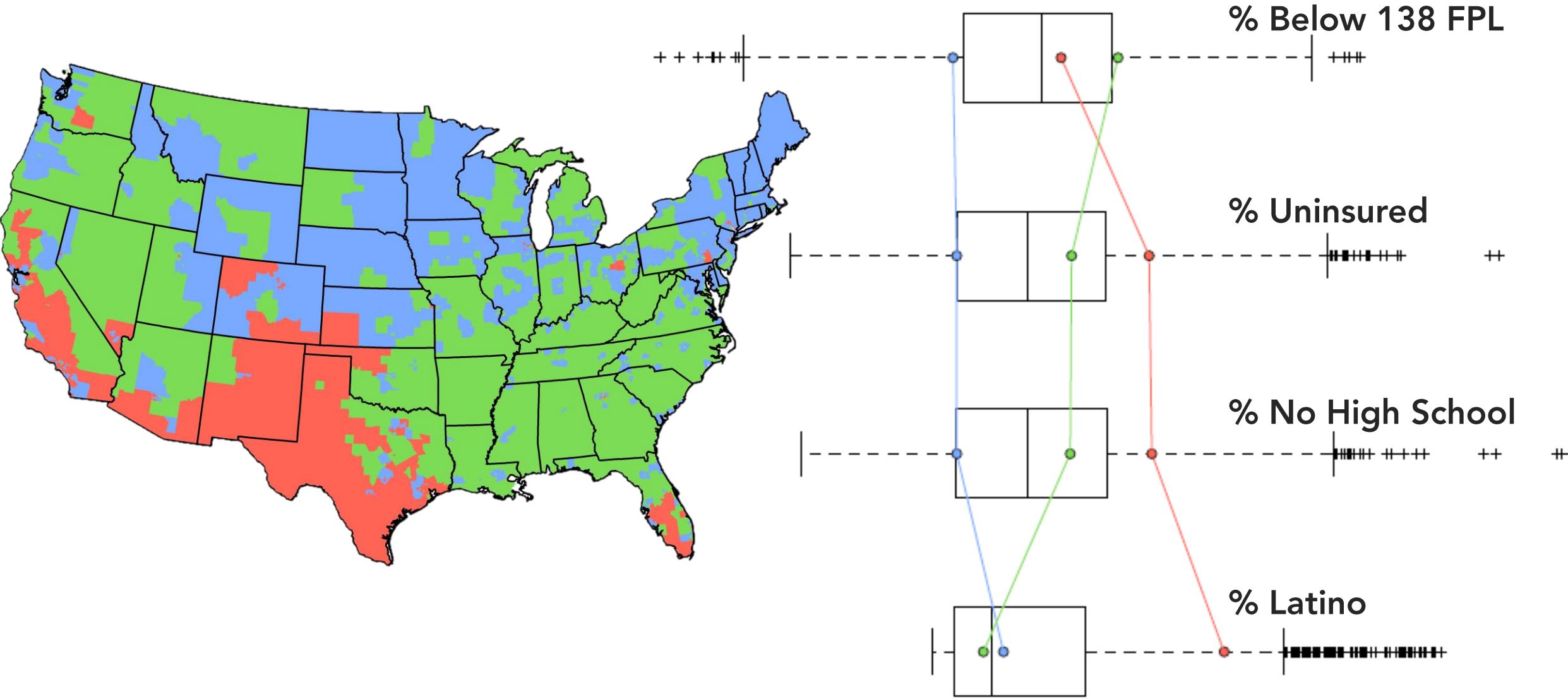
3 groups



4 groups



# Eligible Uninsured Americans



# Spatially Constrained Multivariate Clustering

finds clusters based on feature attributes  
and proximity

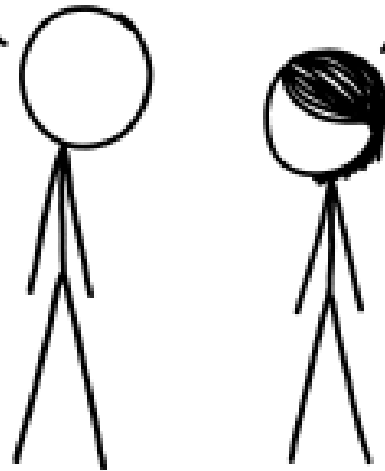


WHAT'VE YOU BEEN UP TO?

DOING TONS OF  
MATH FOR MY THESIS.

CAN YOU EXPLAIN  
IT LIKE I'M FIVE?

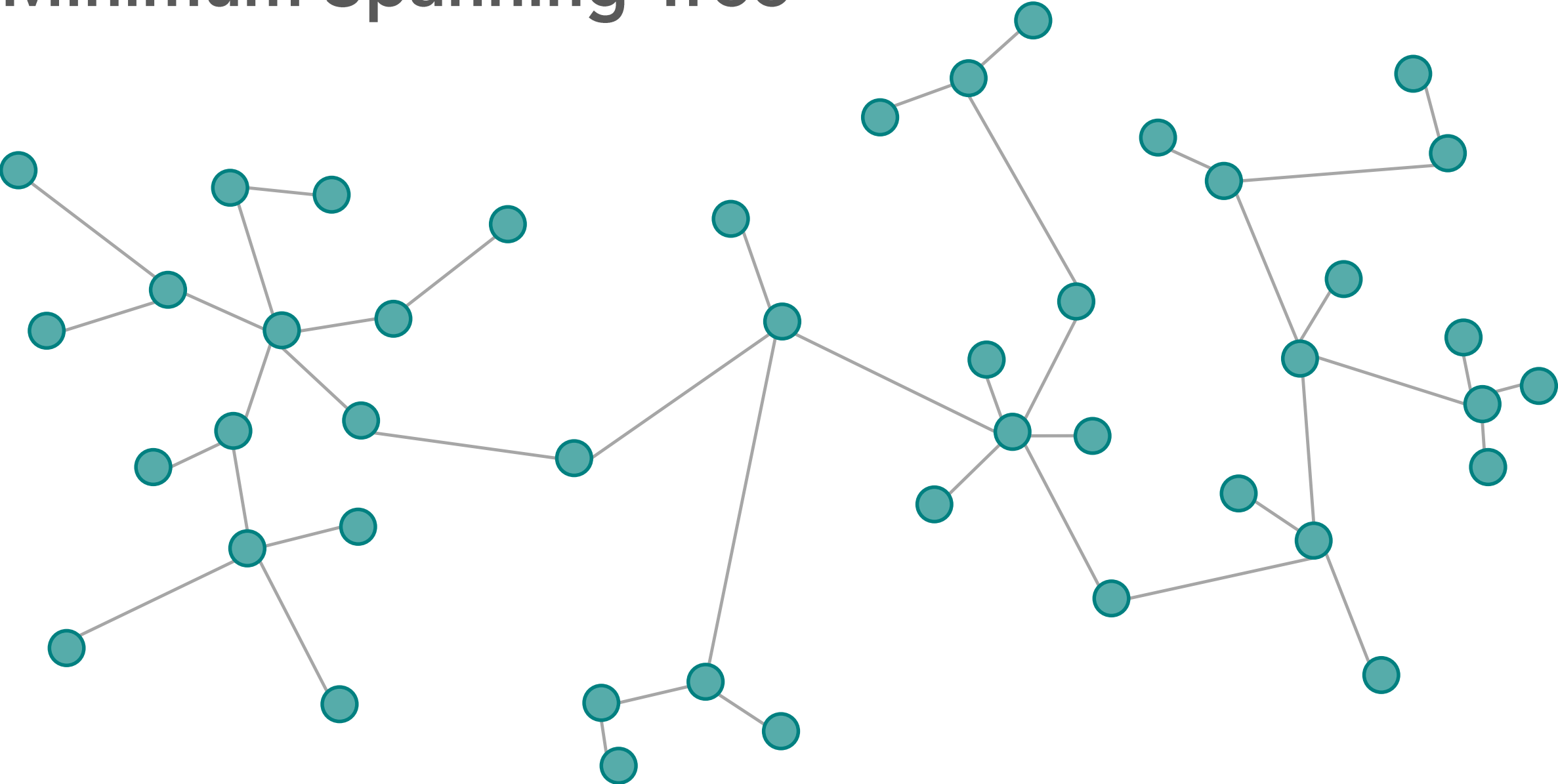
"OH MY GOD, WHERE  
ARE YOUR PARENT5?"



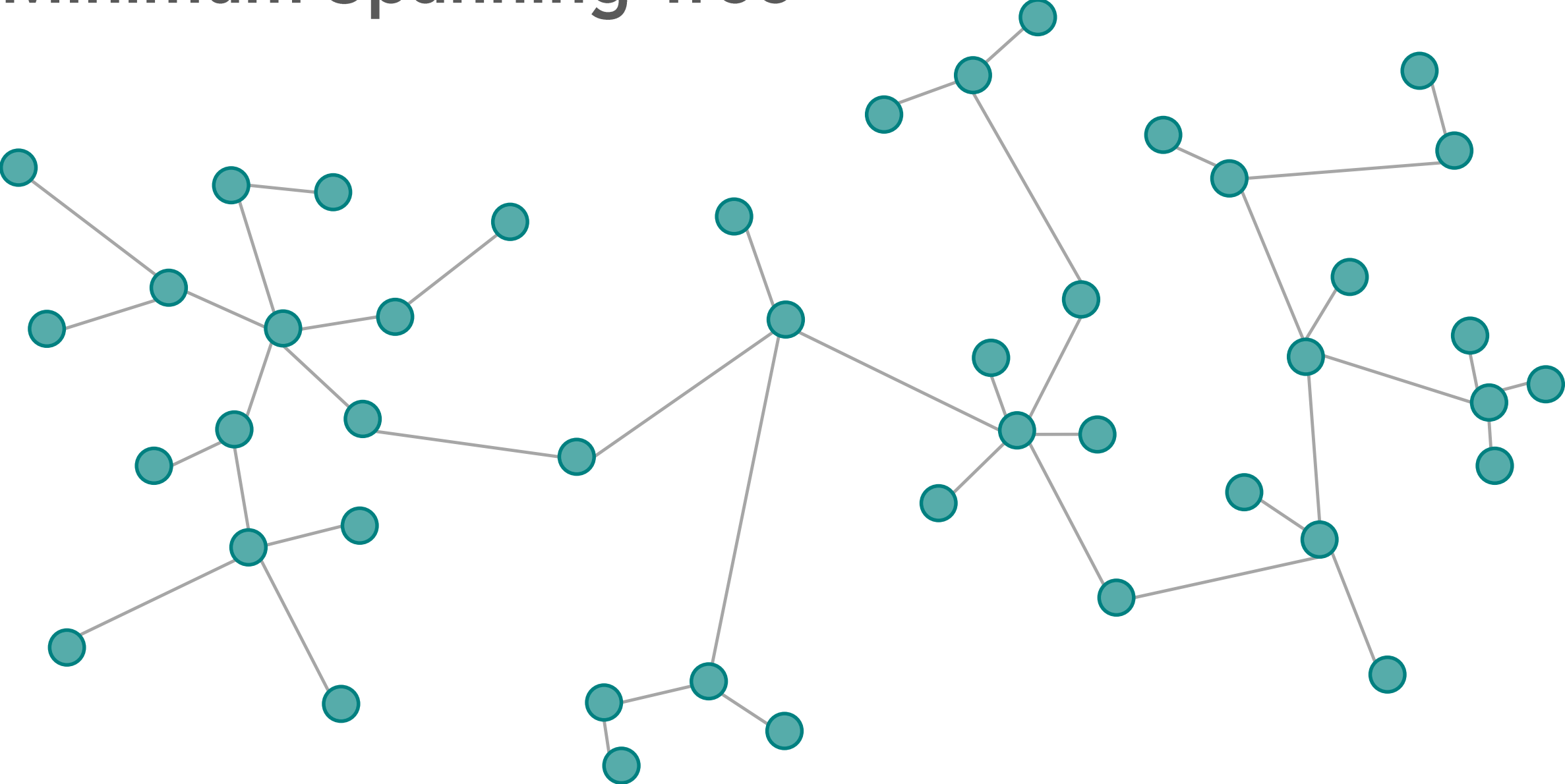
# Minimum Spanning Tree



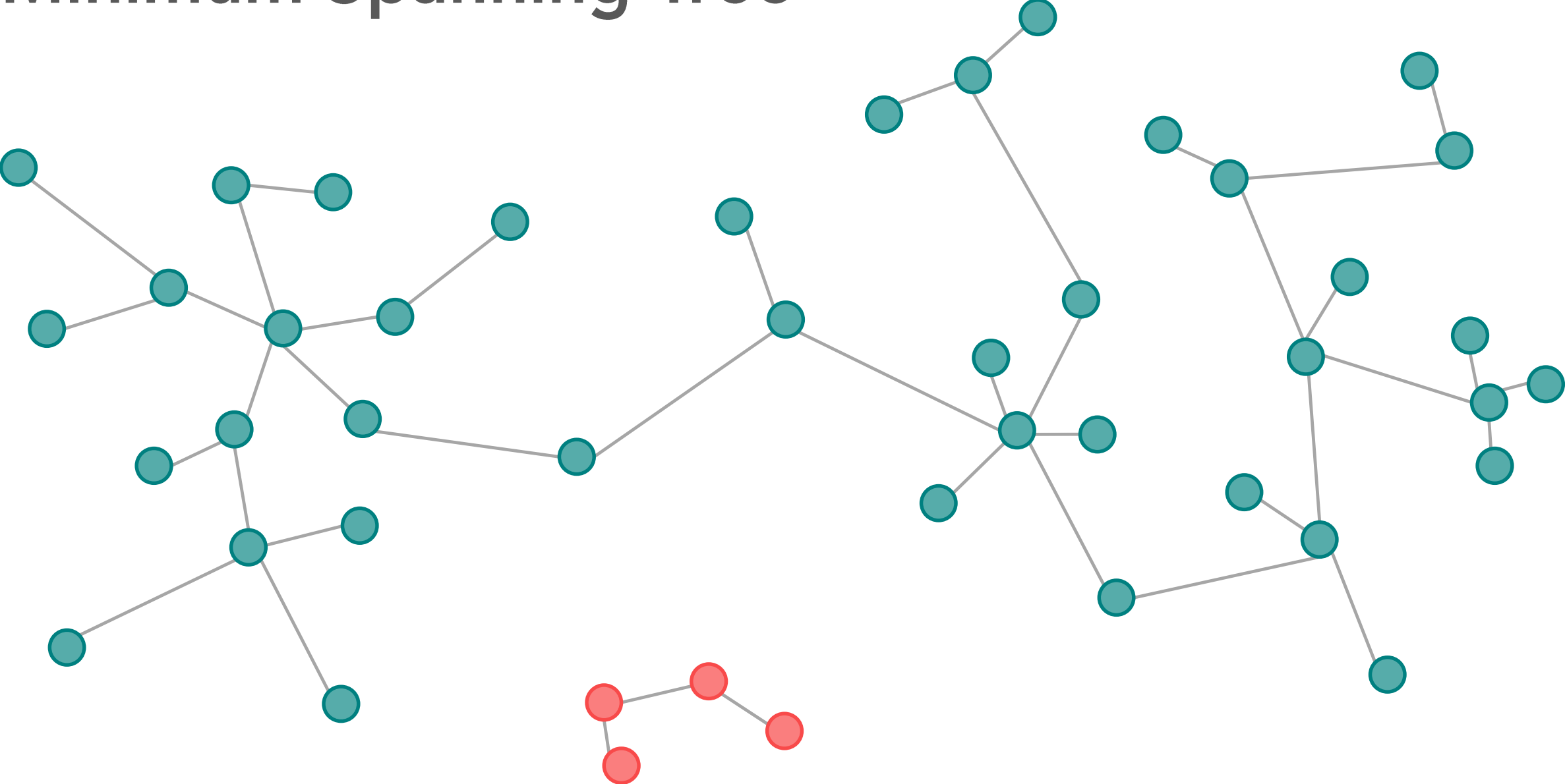
# Minimum Spanning Tree



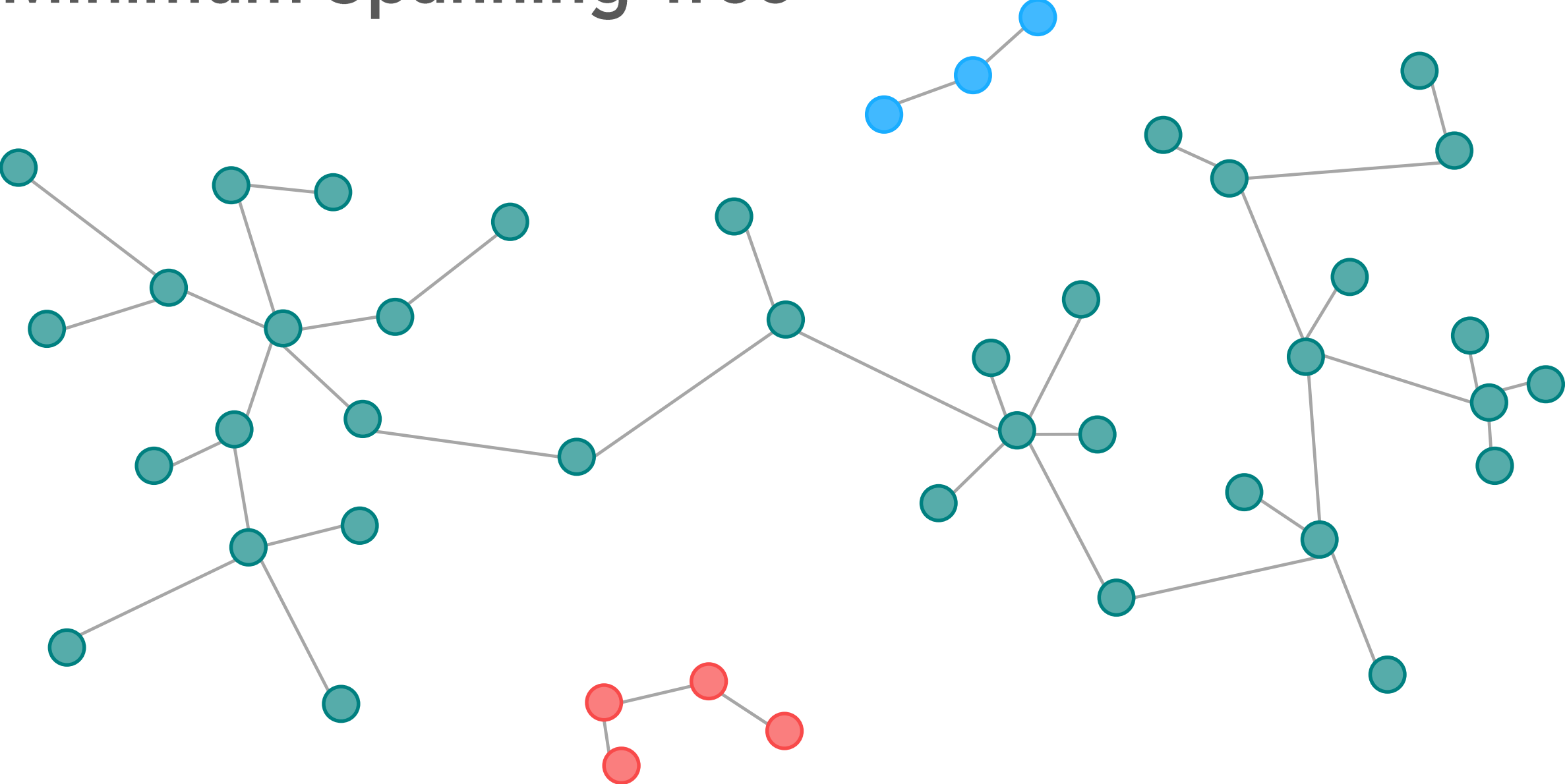
# Minimum Spanning Tree



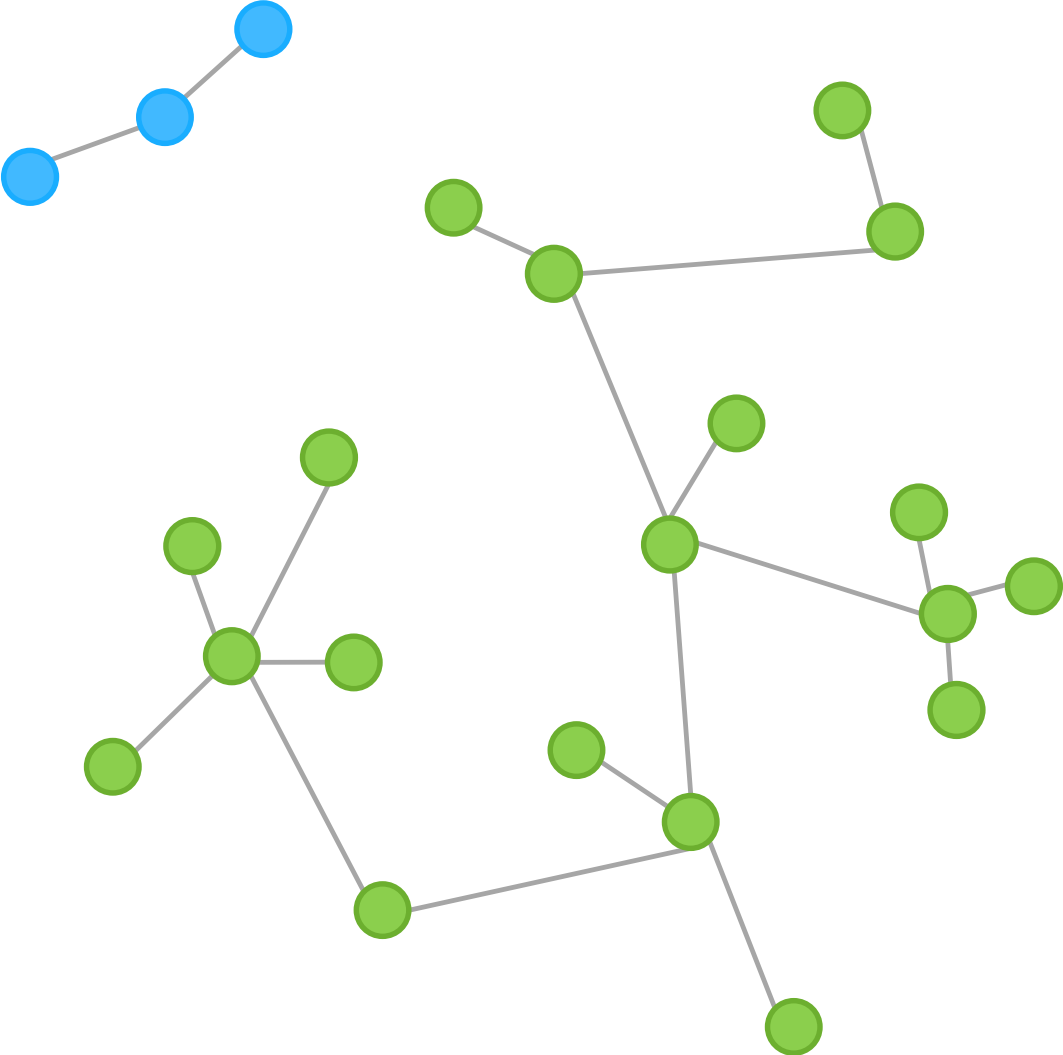
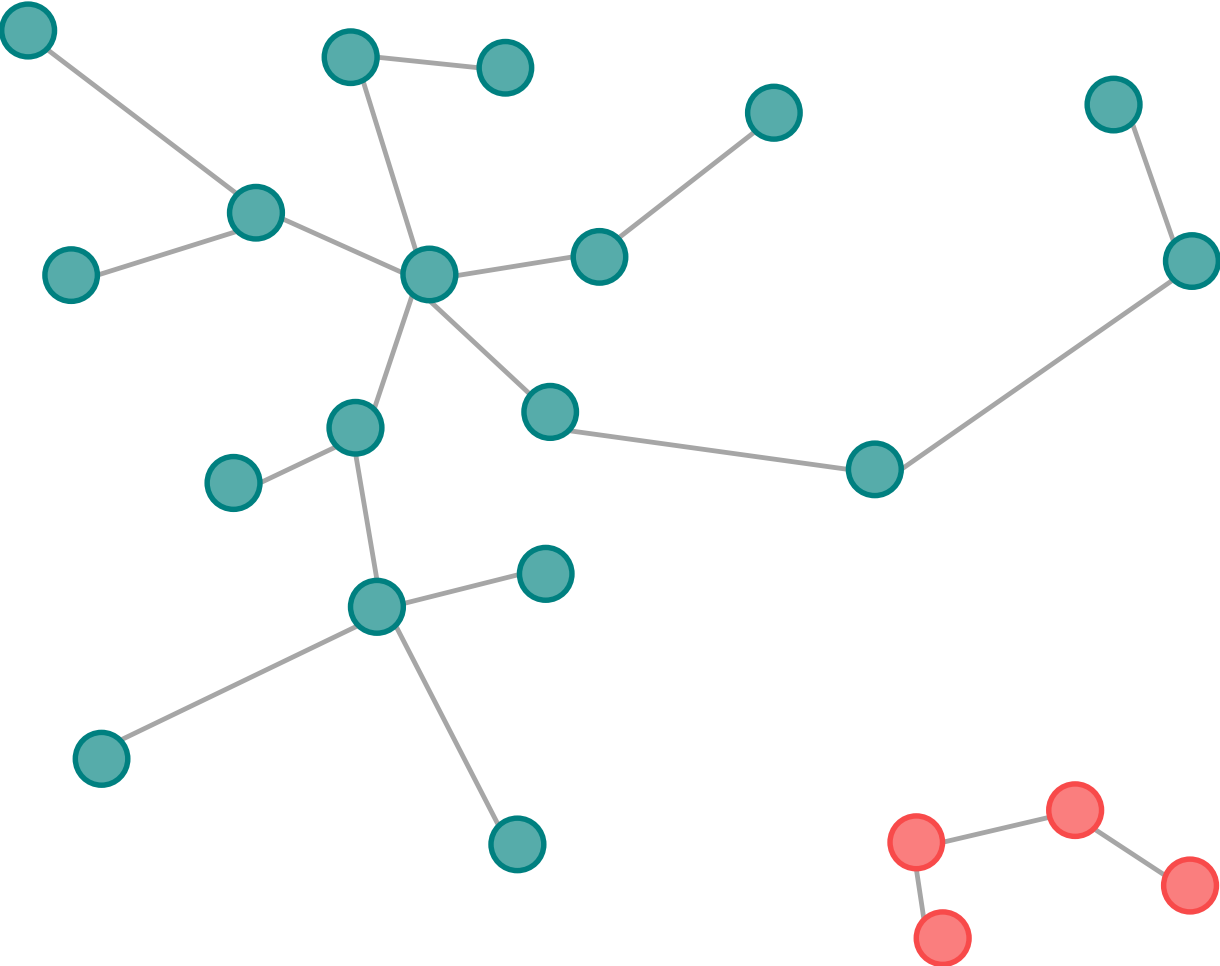
# Minimum Spanning Tree



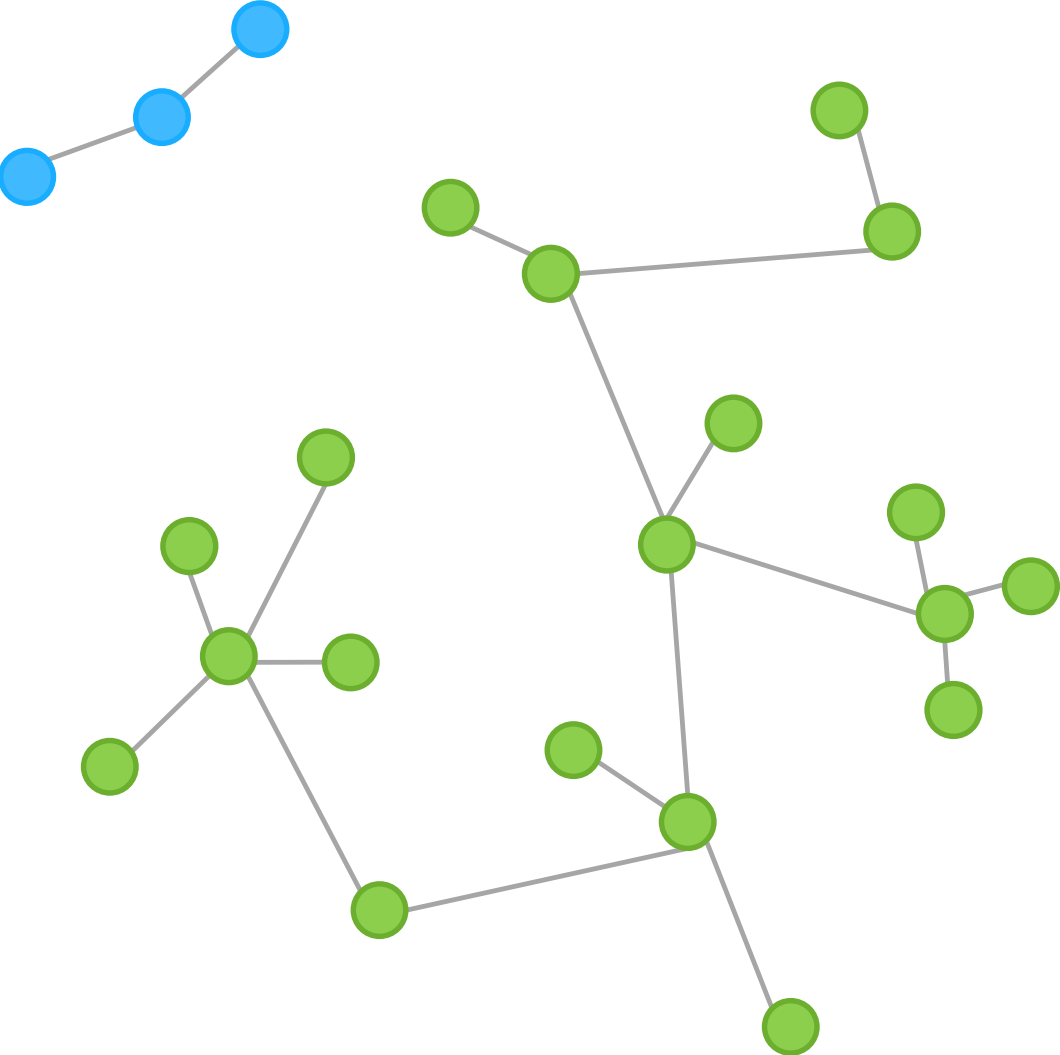
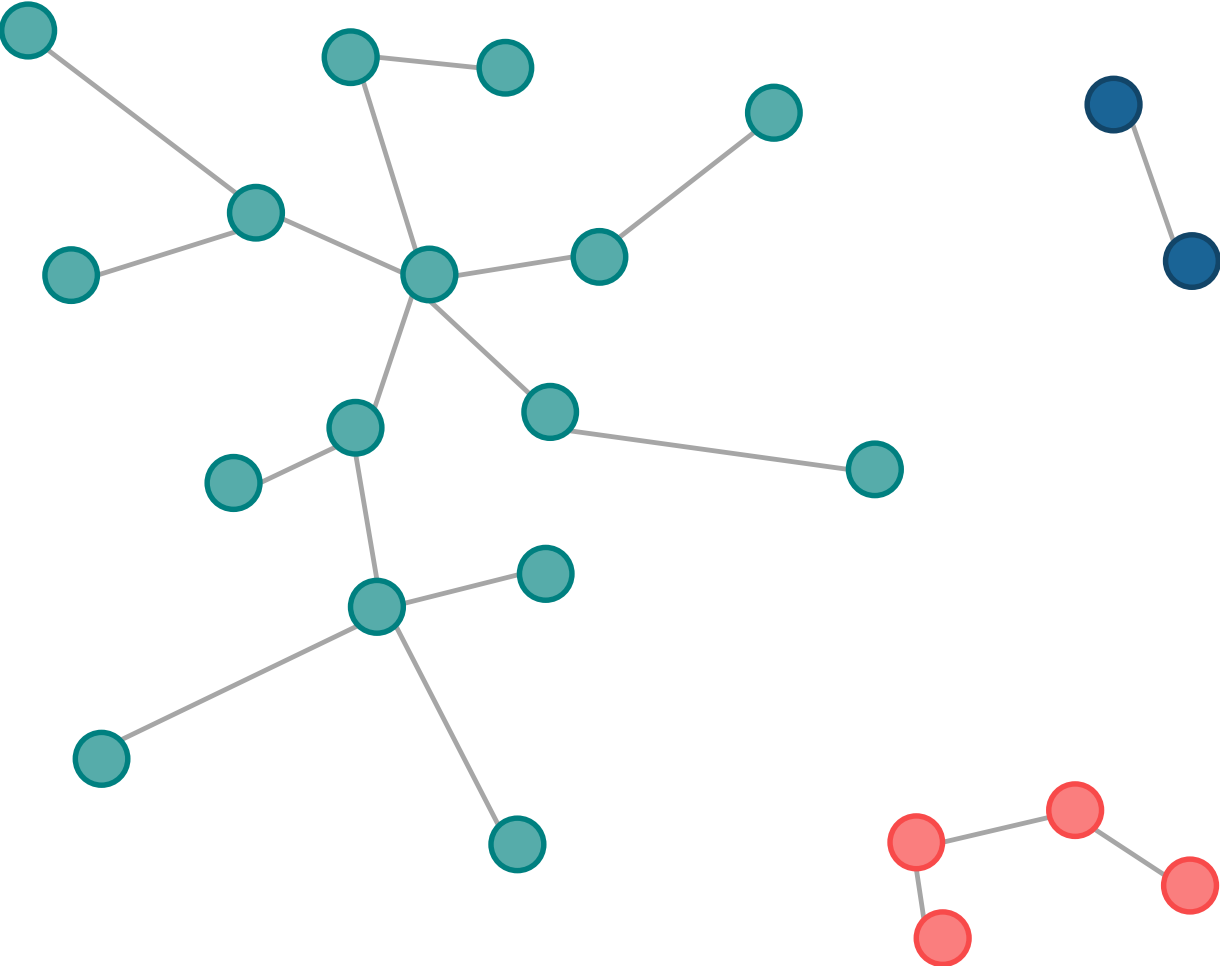
# Minimum Spanning Tree



# Minimum Spanning Tree

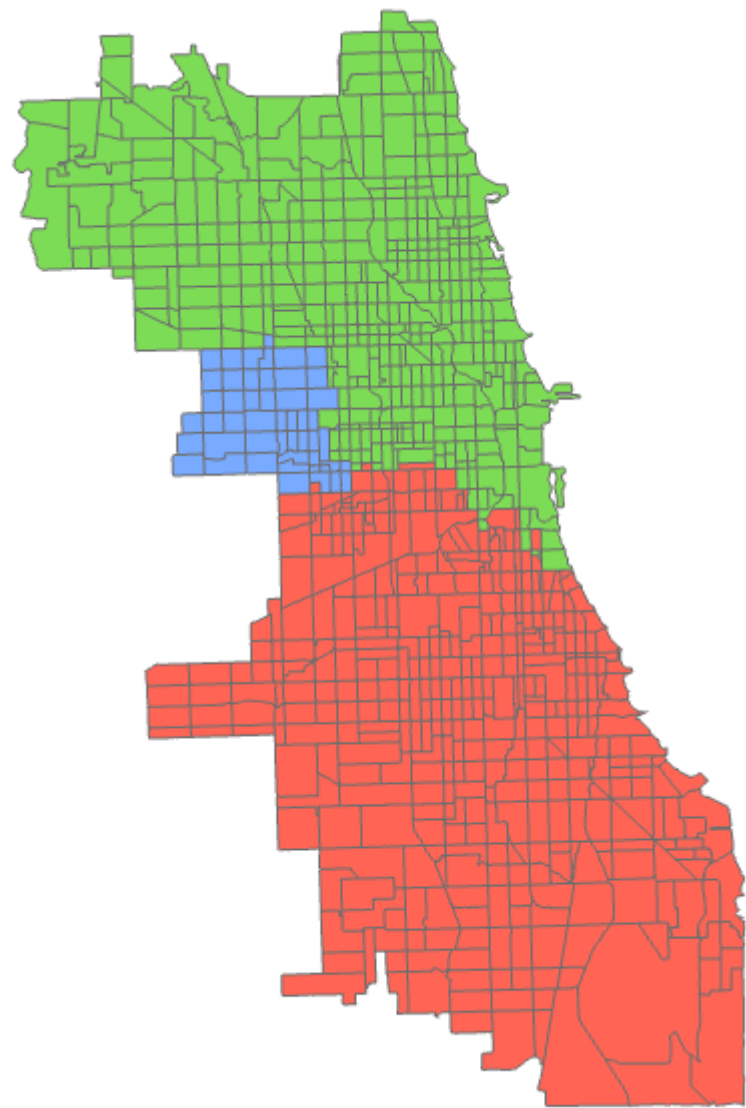


# Minimum Spanning Tree





# Crime in Chicago



Median Income



HS Dropout Rate



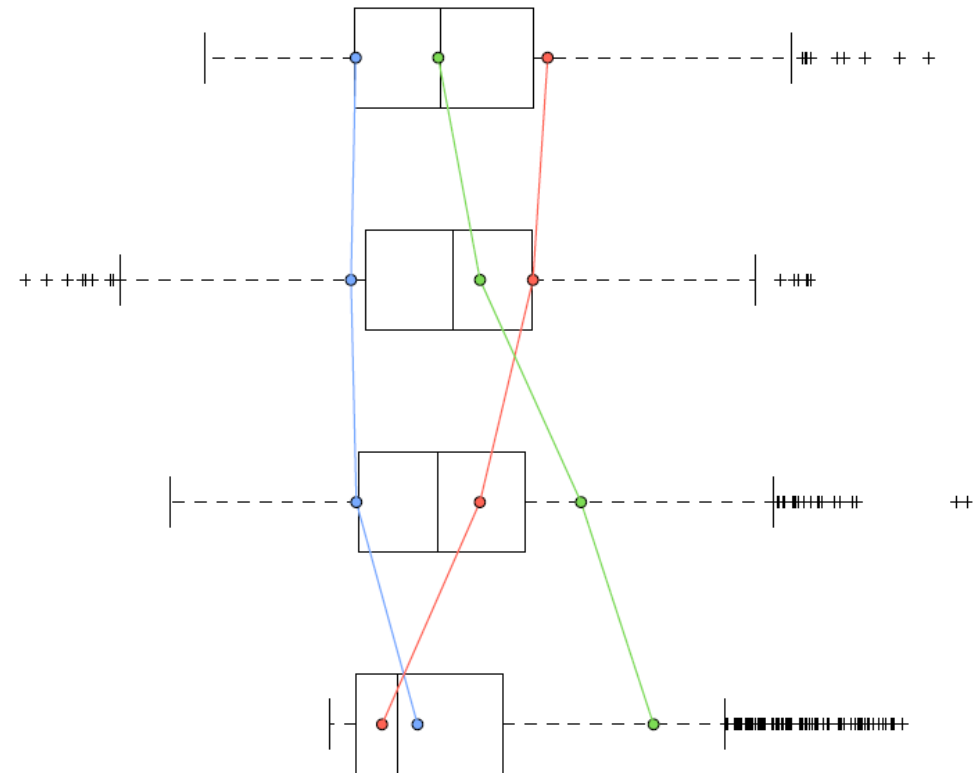
Unemployment



Crime Count



# Demo



Want to learn more???

[esriurl.com/spatialstats](http://esriurl.com/spatialstats)

## TUESDAY

8:30a ~~From Means and Medians to Machine Learning: Spatial Statistics Basics and Innovations~~ 15B

10a ~~Data Visualization for Spatial Analysis~~ 10

2:30p ~~Spatial Data Mining I: Essentials of Cluster Analysis~~ 15B

4p ~~From Means and Medians to Machine Learning: Spatial Statistics Basics and Innovations~~ 14B

## WEDNESDAY

10a **Spatial Data Mining II: A Deep Dive Into Space-Time Analysis** Room 29C

2:30p **Spatial Data Mining I: Essentials of Cluster Analysis** Room 15A

4p **Spatial Data Mining II: A Deep Dive Into Space-Time Analysis** Room 31B

## THURSDAY

10a **Data Visualization for Spatial Analysis** 07A/B

1p **Beyond Where: Modeling Spatial Relationships and Making Predictions** 17B

4p **Beyond Where: Modeling Spatial Relationships and Making Predictions** 17A



[lbennett@esri.com](mailto:lbennett@esri.com)  
[rruthart@esri.com](mailto:rruthart@esri.com)  
[fvale@esri.com](mailto:fvale@esri.com)

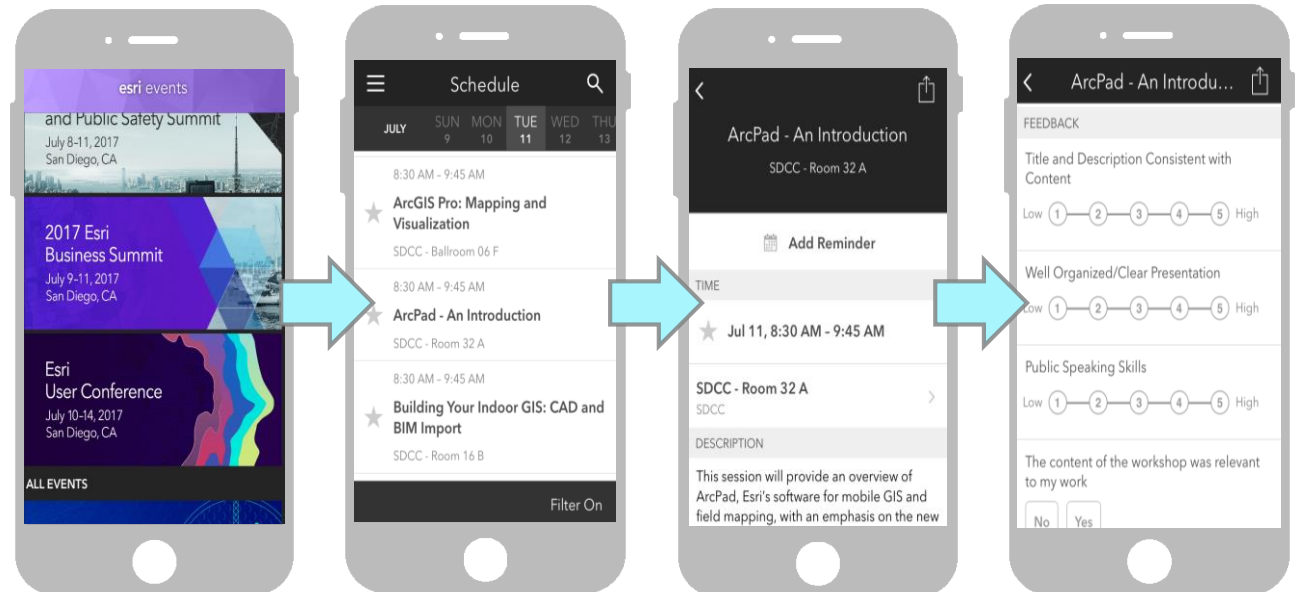
# Please fill out a course survey!!

Download the Esri Events app and find your event

Select the session you attended

Scroll down to find the survey

Complete Answers and Select "Submit"



Want to learn more???

[esriurl.com/spatialstats](http://esriurl.com/spatialstats)

## TUESDAY

8:30a From Means and Medians to Machine Learning: Spatial Statistics Basics and Innovations 15B

10a Data Visualization for Spatial Analysis 10

2:30p Spatial Data Mining I: Essentials of Cluster Analysis 15B

4p From Means and Medians to Machine Learning: Spatial Statistics Basics and Innovations 14B

## WEDNESDAY

10a Spatial Data Mining II: A Deep Dive Into Space-Time Analysis Room 29C

2:30p Spatial Data Mining I: Essentials of Cluster Analysis Room 15A

4p Spatial Data Mining II: A Deep Dive Into Space-Time Analysis Room 31B

## THURSDAY

10a Data Visualization for Spatial Analysis 07A/B

1p Beyond Where: Modeling Spatial Relationships and Making Predictions 17B

4p Beyond Where: Modeling Spatial Relationships and Making Predictions 17A



[lbennett@esri.com](mailto:lbennett@esri.com)  
[rruthart@esri.com](mailto:rruthart@esri.com)  
[fvale@esri.com](mailto:fvale@esri.com)

# Please fill out a course survey!!

Download the Esri Events app and find your event

Select the session you attended

Scroll down to find the survey

Complete Answers and Select "Submit"

